

THE GROUNDS OF ARTS:

TEACHING

The perfect work and practice of Arithmetick
both in whole Numbers and Fractions, shewes more
easie and exact forme then is formerly used, for such
Made by Mr. Robert Recorde, Master of the Art.

Afterwards augmented by Mr. Thomas Digges.

And since enlarged with a third part of Rules of Practice,
abridged into a bricker method then hitherto hath been published,
with diverse necessary Rules incident to the Trade of Merchandise:
with Tables of the valuation of all Coynes, that are
are current at this present time.

By *John Wallis.*

And now diligently perused, corrected, illustrated and enlarged,
with an Appendix of several Questions and the resolution of
their Roots, according to the method of *Simon Stevin*, with
Tables of *Logarithms*, and *Trigonometrie*, and also Tables of *Interest*
upon Interest, and a new and more easie way of translating of
Antiquities to be taught in our schools, and used in our Universities, the first
calculated by *A. C.* but corrected, and the latter originally calculated
by *Re. Henry Briggs*.

Fide _____

LONDON.

Printed by *Miles Fletcher* for J. H. and are to be sold by
Nath. Brooks, at the signe of the *Anchor* in *St. Dunstons Church*.

1649.

That which my friend hath well begun
For very love to Common weale,
Need not all whole to be new done,
But now encrease I doe reveale.

Something herein I once redrest,
And now again for thy behoof,
Of real I doe, and at request,
Both mend and adde, fit for all proof.

Of numbers use the endlesse might,
No wit nor language can expresse,
Apply and try both day and night,
And then this truth thou wilt confesse.

J. Dec.

The Books Verdict.

TO please or displease sure I can
But not of one sort to every man:
To please the best sort would I faine,
The forward displease shall I certain,
Yet wish I will though not with hope,
All eares or mouths to please or hope.

To the Most mighty Prince, Edward
the sixth, by the grace of God, King of
England, France, and Ireland, &c.



The Excellency of mans nature being
such, as it is by Gods diuine fauour
(most mighty Prince) not only created
in highnesse of degree far aboue all o-
ther corporall things, but by perfecti-
on, reason, and search of wit, much
approaching toward the image of God, as not onely
the holy Scriptures do testifie, but also those naturall
Philosophers, which exactly did consider the nature of
man, and namely the far reach and infinite compass
of the words of the mind, were inforced to confesse,
that man scarcely was able to know himself. And if
he would duly ponder the nature of himself, he would
find it so strange, that it might seem vnto him a very
miracle: And thereof sprang that saying; *Maximum*
miraculum est homo, maximum miraculum sapiens
homo. For undoubtedly, as man is one of the greatest
miracles that ever God wrought, so a wise man is
plainly the greatest.

And therefore was it that some did account the head
of a man the greatest miracle in the world, because not
only of the strange workmanship that is in it, but much
more of the efficacy of reason, wit, memory, imagina-
tion, and such other powers, and works of the mind,
which can more easily conceive any thing in a manner
then understand it self. Amongst all the creatures of
God, it findeth none more difficult to be perceiued
then these same powers of it self; whereby it doeth
conceive and iudge: as it may be well conjectured by
the diversity of opinions, that the wisest Philosophers
did utter touching the spirit of man, and the substance
of it: whereof I now intend to make no rehearsal,
but who so listeth to read thereof, may find it largely

set forth, not onely in *Aristotle* his books *de Anima*, but also in *Galen* his book called *Historia Philosophica*: and again in *Plutarch* his work, *De Philosophorum placitis*, whose words are also repeated of *Eusebius* in the xv. book. Τὸ δὲ ἄλλο ἐπεὶ ἀναγκαῖον, unto whom I remit them that have desired to understand intricate difficulty of knowing our own selves, as touching our best part, and that part whereby we deserve to bear the name of men.

This matter seemed so obscure and difficult in knowledge; that *Galen*, who for his excellent wisdom and judgement in naturall works, is called of many men a Miracle in Nature, yet in searching the nature and substance of the spirit of man, he not onely confessed himself ignorant, but counteth it plain temerity to attempt to find it. So far above the hope of mans knowledge is that part, whereby man doth know and judge of things. And although the ignorant sort (which hate all things that they know not) do little esteeme the profoundnes of mans spirit and reason, the chief power and faculty of it: yet as there is a kind of fear and obedience of unreasonable beasts unto man, by the working power of God, so is there in those small reasoned persons a certain kind of reverence toward wisdom and reason, which they do shew oftentimes, and by power of perswasion, are enforced to obey reason, will they nill they. And hereby came it to passe, that the rudenesse of the first age of man was brought unto some more civil trade, as it is well declared by *Cicero*, in the beginning of his first book, *De Inventione Rhetorica*, where he saith thus: *Nam fuit quoddam tempus quum in agris homines passim bestiarum more vagabantur; & sibi victu ferunt vitam propagabant; nec ratione animi quicquam, sed plerique viribus corporis administrabant: Nondum divina religio, non humani ratio colebatur. Nemo legumum viderat nuptias, non certos quisquam in pueris liberos; non iam aquabile quid utilitatis haberet, acceperat;*

vat: ita propter errorem atque incertam caeca ac temeraria
dominatrix amicitia, ad se explendam viribus corporis
monetatur perniciosissimis satellitibus. Quo tempore quidam,
magis videlicet vir & sapiens, cognovit quae materia esset,
& quam ad maximam opportunitatem in unum inesse homi-
num, si quis eam possit elicere, & praecipiendo meliorem red-
dere. Quia dispersos homines in agris, & in telluris Sylvestri-
bus abditos, ratione quadam compulsi in unum locum, & con-
gregavit: & eos in utramquamque rem indacens utilem atque
honestam, primo propter insolentiam reclamantes, deinde pro-
pter rationem atque orationem studiosius audientes, ex feris &
immanibus, mites reddidit, & mansuetos.

This long repetition of *Tullyes* words will seem re-
digious to them that love but little, and care much lesse
for the knowledge of reason, but unto your Majesty (I
dare say) it is a delectable remembrance, and unto me
it seemed so pleasant, that I could scarce stay my pen
from writing all that mine eyes did so greedily read.

This sentence of *Cicero* am I loath to translate into
English, partly for that unto your Majesty it needeth
no translation, but especially knowing how far the
grace of *Tullyes* eloquence doth excell any English-
mans tongue, and much more exceedeth the baseness
of my barbarous stile: yet for the fruit of my sentence,
I had rather unto my meer English Country men ut-
ter the rudeness of my translation, then to defraud
them the benefit of so good a lesson, trusting they will
so learn to love reason, that they will also gladly and
greedily embrace all good Sciences, that may help to
the just furniture of the same, when they consider
that informed reason was the only instrument, or at
least the chiefest meanes to bring men into civill regi-
ment, from barbarous manners, & beastly conditions.

For the time was (such *Tully*) that men wandred
abroad in the fields up and down like beasts, and
used no better order in feeding then they: so that
by reasons rule they wrought nothing, but most of
their doings did they achieve by force of strength.

The Preface unto

"At this time there was no just regard of religion to-
wards God, nor of duty toward man. No man had
seen right use of marriage, neither did any man
know their own children from others; nor no man
had felt the commodity of just laws, so that through
error and ignorance, wilfull lust, like a blind and
heady ruler, abused bodily strength as a most mor-
tall minister for the satisfying of his desire. At that
time was there one which not onely in power,
but also in wisdom was great, and he considered
how that in the minds of men was both apt instru-
ments, and great occasion to the due accomplish-
ment of most weighty affairs, if a man could apply
them to use, and by reaching of rules frame them to
better trade. This man with perswasion of reason
gathered into one place the people that were wan-
dring about the fields and lay lurking in wild cotta-
ges, and woods, and bringing them into one com-
mon society, did trade them to all such things, as
either were profitable or honest, although not with-
out repining at the first, by reason that they had not
been so accustomed before. Yet at length through
reason and perswasion of words they obeyed him
more diligently, and so of a wild and cruell people,
he made them courteous and gentle.

Thus hath *Tully* set forth the efficacy of reason and
perswasion, how it was able to convert wild people to
a mildness, and to change their furious cruellness into
gentle courtesie: were it not now a great reproach in
this our time (when knowledge reigneth so large) that
men should shew themselves lesse obsequious to rea-
son? Vntesse it may be thought, that now every man
having sufficient knowledge of himself, needeth not
to hearken to the perswasion of others.

Indeed he that thinketh himself wise, will not esteem
the reason of any other, be he never so wise; so that
of such a one it may well be said: He that thinketh
himself wiser then he is, may justly be counted a dou-
ble

ble fool. Wherefore such men are not to be permitted in open audience to talk, but must be put to silence, and be made to give ear to reason; which reason consisteth not in a multitude of words heaped rashly together, and applied for one purpose, but reason is the expressing of a just matter with witty perswasions, furnished with learned knowledge: such knowledge had *Moses*, being expert in all learning of the Egyptians, as the Scriptures declare, and therefore was able to perswade the stubborn people of the Jews, although not without pain. Such knowledge, and such reasons did *Drusus* shew, which was the first Law-maker of all the West part of Europe. Like reason and wisdom did *Xamolxis* amongst the Goths, *Lycurgus* unto the Lacedemonians, *Zaleucus* to the Locrians, *Solon* to the Athenienses, and *Dunwallo Molmutius* two thousand years past amongst the old Britains of this Realm. And hereby came it to passe, that their Laws continued long, till more perfect reason altered many of them, and wisfull power oppressed most of them.

Drusus was son to king *Sarron*, and succeeded him in his kingdome;

At the beginning when these wise men perceived how hard it was to bring the rude people to understand reason, they judged the best means to attain this honest purpose, to depend of learning in every kind: for by learning (as *Ovid* saith) *Pectora mollescent asperitasque fugit* Stout stomachs do wax milde, and sharp fiercenesse is exile. Therefore as *Berosus* doth testifie, *Sarron* that was the third King over all this West part of Europe, for to bring the people from beastly rage to manly reason, did erect Schools of liberall Arts, which took so good successe, that his name continued in that sort famous above two thousand years after: for *Diondorus Siculus* which was in the time of *Julius Caesar*, maketh mention of the learned men or Gorthes of Celtes, and nameth them *Sarronders*, that is to say, *Sarron his Scholars and followers*.

Among these Arts that then were taught, some did

The Preface unto

inform the tongue, and make them able both to utter
 apply their mind, and also to perswade; as Grammar,
 Logick, and Rhetorick, although not so curiously as in
 this time; some other did appertain to the just order
 of partition of Lands, the true using of Weights, Mea-
 sures and reckonings in all sorts of bargains, and for
 order of building and sundry other uses; those were
 Arithmetick and Geometry. Again, to encourage men
 to the honour of God, they taught Astronomy, where-
 by the wonderfull works of God were so manifestly set
 forth, that no mans tongue, nor pen can in like sort ex-
 presse his infinite power, his unspeakable wisdoms,
 and his exceeding goodnesse toward man, whereby
 he doth bountifully provide for man all necessaries,
 not onely to live, but also to live pleasantly. And so
 was their confidence in Gods providence strongly
 stayed, knowing his goodnesse to be such, that hee
 would help man as hee could, and his power to be so
 great, that he would do nothing but that that was best.
 Beside these Sciences they taught also Musick, which
 most commonly they did apply partly to religious ser-
 vices, to draw men to delight therein, and partly to
 songs made of the manners of men, in praise of Vertue
 and discommendation of Vice, whereby it came to
 passe, that no man would displease them, nor do any
 thing evill that might come to their hearing: for their
 songs did make evill men more abhorred in that time
 then any excommunication doth in this time. The po-
 sterity of these Musicians continue yet both in Wales
 and Ireland, called *Bardes* unto this day, by the an-
 cient name of *Bardus*, their first founder.

And as these Sciences did encrease, so did vertue en-
 crease thereby. Again, as those Sciences did decay, so
 Vertue lost her estimation, and consequently was little
 in use: whereof to make a full declaration were a
 thing meet for a Prince to hear, but it would require a
 peculiar Treatise. Wherefore at this present I count

NEW FINE
 GUID OF THE
 KING OF THE
 CELTES
 AND HIS
 REIGN

This *Bar-
 dus Drui-
 dius* the 5.
 King of the
 Celtes.
 reigned 60
 years, and
 died 1832
 years be-
 fore Christ

it sufficient lightly to have touched this matter in general words, and to say no more of the particularity thereof, but onely touching one of those Sciences, that is, Arithmetick, by which not onely just partition of lands was made, but also touching buying and selling, all Assises, Weights, and Measures were devised, and all reckonings and accounts driven; yea by proportion of it were the true orders of Iustice limited, as *Aristotle* in his *Ethicks* doth declare, and the degrees of estates in the Common-wealth established; although that proportion be called Geometrickall and not Arithmetickall, yet doth that proportion appertain to the art of Arithmetick, and in Arithmetick is taught the progression of such proportions, and all things thereto belonging. Wherefore I may well say, that (seeing Arithmetick is so many wayes needfull unto the first planting of a Common-wealth, it must needs be as much required to the preservation of it also: for by the same meanes is any Common-wealth continued, by which it was erected and established. And if I shall in small matters in appearance, but indeed very weighty, put one example or two, What shall we say for the Statutes of this Realm, which be the onely stay of good order in manner now? As touching the measuring of ground by length and breadth, there is a good and an ancient Statute made by art of Arithmetick; and now it shall be to little use, if by the same Art it be not Practised and tried. For the assise of Bread and Drink, the two most common and most necessary things for sustentation of man, there was a goodly ordinance in the Law made, which by ignorance hath so grown out of knowledge, and use, that few men do understand it, and therefore the Statute books wonderfully corrupted, and the Commons cruelly oppressed: notwithstanding some men have written that it is too doubtfull a matter to execute those assises by those Statutes, by reason they depend of the standard of the coyne, which

which is much changed from the state of that time, when those Statutes were made. Thus shall every man read (that listeth) in the Abridgement of the Statutes, in the title of Weights and Measures, in the seventh number of the English Book, where he should have translated a good ordinance which is set forth in the French Book: but no marvell if the Abridgement doth omit it, seeing the great Book of Statutes doth omit the same Statute, as it hath done divers other very good Lawes. And this is the fruit of ignorance, to reject and condemn all that it understandeth not, although they use some cloaks for it: but such cloaks as being allowed, might serve to repell all good Laws, which God forbid.

Againe, there is an ancient order for affise of fire, Wood and Coals, which was renewed not many years past; and now how avarice and ignorance doth canvaase that Statute, it is too pitifull to talk of, and more miserable to feel.

Parthermore, for the Statute of Coynage, and the standard thereof, if the people understood rightly the Statute, they should not, nor would not (as they often-do) gather an excuse for their folly thereby: but as I said, these Statutes by wisdom and good knowledge of Arithmetick were made, and by the same must they be continued. And let ignorance no more meddle with the use of them, then it did with the making of them. Oh in how miserable case is that Realm, where the ministers and interpreters of the Law are destitute of all good Sciences, which be the Keys of the Laws! How can they either make good Laws, or maintain them that lack that true knowledge whereby to judge them? And happy may that Realm be accounted, where the Prince himself is studious of learning, and desireth to understand equity in all Laws. Therefore most happy are we the loving subjects of your Majesty, which may see in your Highnesse not only

onely such towardnesse, but also such knowledge of
divers Arts, as seldom hath been seen in any Prince
of such years, whereby we are enforced to conceive
this hope certainly, that he which in those years seek-
eth knowledge, when knowledge is least esteemed, and
of such an age can discern them to bee enemies both
to his Royall Person and to his Realme, which labour
to withdraw him from knowledge to excessive pas-
time, and from reasonable study to idle or noysome
pleasures, he must needs when he cometh to more ma-
ture years, be a most prudent Prince; a most just Go-
vernour, and a right Iudge, not onely of his Subjects
commonly, but also of the ministers of his Laws, yea,
and of the Laws themselves: and to bee able to con-
ceive the true equity and exact understanding of all his
Laws and Statutes, to the comfort of his good Sub-
jects, and the confusion and reproach of them which
labour to obscure or pervert the equity of the same
Laws and Statutes. How some of these Statutes may
be applied to use, as well in this our time, as in any o-
ther time, I have peculiarly declared in this Book. and
some other I have omitted for just considerations, till
I may offer them first unto Your Majesty to weigh
them as to your Highnesse shall seem good: for many
things in them are not to be published without your
Highnesse knowledge and approbation; namely, be-
cause in them is declared all the rates of alloyes for
all standards from one ounce upward, with other my-
steries of Mint matters, and also most part of the varie-
ties of coynes that have been currant in this your Ma-
jesties Realm by the space almost of six hundred years
last past, and many of them that were currant in the
time that the Romanes ruled here.

All which, with the ancient description of England
and Ireland, and my simple censure of the same, I have
almost compleated to be exhibited to your Highnesse:
In the mean season most humbly beseeching your Ma-
jesty

The Preface unto the Kings, &c.

jesty to accept this simple Treatise, nor worthy to be presented to so high a Prince, but that my lowly request to your Majesty is, that this amongst other of my Books may passe under the protection of your Highness, whom I beseech God most earnestly and daily, according to my duty, to advance in all honour, and Princely Regalcy, and to increase in all knowledge, justice, and godly policy. Amen.

Your Majesties most

obedient subject

and servant,

ROBERT ROOD

TO

All which, with the ancient description of England and Ireland, and my simple canonic of the same I have already completed to be exhibited to your Highness in the mean season will humbly beseech your Majesty

TO THE LOVING READER,

The Preface of M. Robert Record.

SOME of times have I lamented with my selfe the unfortunate condition of England, seeing so many great Clerks to arise in sundry other parts of the world, and so few to appear in this our Nation: whereas for pregnancy of naturall wit (I think) few Nations do excell Englishmen: But I cannot impure the cause to any other thing, then to the contempt, or misregard of learning. For as Englishmen are inferior to no men in mother wit, so they passe all men in vain pleasures, to which they may attain with great pain and labour: and are slack to any never so great commoditie, if there hang of it any painfull study or travel, or any labour.

Howbeit, yet all men are not of that sort, though the most part be, the more pity is it: but of them that are so glad, not onely with painfull study, and studious pain to attain learning, but also with as great study and pain to communicate their learning to other, and make all England (if it might be) partakers of the same: the most parts are such, that whateash they can support their own necessary charges, so that they are not able to beare any charges, in doing of that good that else they desire to doe.

But a greater cause of lamentation is this, that when learned men have taken pains to do things for the good of the commonwealth, yet they shall be allowed for their good doing but derided and scorned, and so utterly discouraged to take in hand any like enterprise again: so that if any be found (as there are some) that do favour learning,

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learning, & learned wits, & can be content to further knowledge, yet onely with their word: Such persons though they be rare, yet shall they encourage learned men to enterprife something at the least that England may rejoyce of. And I have good hope that England will (after she hath taken some sure taste of learning) not onely bring forth more favourers of it, but also such learned men, that she shall be able to compare with any Realm in the world. But in the mean season, where so few regards of learning are, how greatly they are to be esteemed that do favour & further it, my pen will not suffice at full to declare.

Therefore gentle Reader, whereas I do upon most just occasion judge, yea and know assuredly, that there be some men in this Realm, which both love and also much desire to further good learning, and yet are not well able to write their condign praise for the same, I think it better with silence to overpass it, than either say too little of it, or to provoke against them the malice of such other, which do nothing themselves that is praise-worthy, and therefore cannot abide to hear the praise of any other mans good deed.

And considering their great favour unto learning, though I my self be not worthy to be reckoned in the number of great learned men, yet am I bold to put myself in Presse with such ability as God hath lent me, though not with so great cunning as many men, yet with as great affection as any man to help my Country men, and wil not cease dayly, (as much as my small ability will suffer me) to endee some such thing, that shall be to the instruction, though not of learned men, yet at the least of the vulgar sort, whose argument al

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wayes shall be such as it shall delight all learned mites though they do not learn any great thing out of it.

But to speake of this present book of Arithmetick, I dare not, nor will not set it forth with any words, but remit it to the judgements of all gentle Readers, and namely, such as love good learning, beseeching them so to esteeme it, as it doth seem worthy. And so either to accept the thing for it self, either at the least to allow my good endeavour. But I perceive I need not use any perswasions unto thō, whose gentle nature and favourable mind is ready to receive thankfully, & interpret to the best al such enterprises attempted for so good an end, though the thing do not always satisfie mens expectation. This considered, did bolden me to publish abroad this little Book of the Art of numbring, which if you shall receive favourably you shall encourage me to gratifie you hereafter with some greater thing.

And as I judge some men of so loving a minde to their native Countrey, that they would much rejoyce to see it prosper in good learning, & mitty Arts: so I hope well of all the rest of Englishmen, that they will not be unmindfull of his due praise, by whose meanes they are helped and furthered in any thing. Neither ought they to esteeme this thing of so little value, as many men of little discretion oftentimes do. For who so setteth small price by the mitty service and knowledge of numbring, he little considereth it to be the chief point, (in manner) whereby men differ from all bruce beastes: for as in all other things (almost) beastes are partakers with us, so in numbring we differ cleane from them, and in man-
ner

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very peculiarly, *with that in many things they excell us again.*

The Fox in crafty wit exceedeth most men;
A Dog in smelling hath no man his peer;
To foresight of weather if you look then,
Many beasts excell men; this is cleer,
The wittinesse of Elephants doth letters attain;
But what cunning doth there in the Bee remain?
The Emmer foreseeing the hardnesse of winter,
Provideth victuals in the time of summer;
The Nightingale, the Linet, the Thrush, the Lark,
In Muscicall harmony passe many a Clark,
The Hedghog of Altronomy seemeth to know,
Thd stoppeth his cave where the wind will blow;
An Spider in weaving such Art doth shew,
The man can him mend, nor follow I crow.
No en a house will fall, the Mice right quick
Whence before; can man do the like?

Many things esse of the wittinesse of Beasts and Birds might I hear say, save that another time of them I intend to write, wherein they excell in manner all men, as it is daily seen: but in number will there never bea found so cunning, that could know or discern one thing from many, by daily experience you may well consider, when a Bitch hath many whelps, or a Hen many chickens: and likewise of other whatsoever they be, take from them all their young saving only one, and you shall perceive plainly, that they misse none, though they will resist you in taking them away, and will seek them againe if they may

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may know where they be, but else they wil never misse them truly; but take away that one that is left, and then will they cry and complain; and restore to them that one, then are they pleased again. So that of number, this may I justly say, is the onely thing almost that separateth man from beasts. He therefore that shall contemn number, declareth himself as brutish as a beast, and unworthy to be counted in the fellowship of men. But I trust there is no man so souleover-seen, though many right smally do it regard.

Therefore will I now stay to write against such, and return again to this my Book, which I have written in the forme of a Dialogue, because I judge that to be the easiest way of instruction, when the Scholar may ask every doubt orderly, and the Master may answer to his question plainly.

Why the
Author
wrote in
Dialogue
wise.

Howbeit I thinke not the contrary, but as it is easier to make another mans work thento make the like; so there will be some that will find faults, because I write in a Dialogue: but as I conjecture these shall be such as do not, cannot, or will not perceive the reason of right teaching, and therefore are unmeet to be answered unto, for such men with no reason will bee satisfied.

And if any man object, that other Books have been written of Arithmetick already so sufficiently, that I needed not now to put Pen to the Book, except I will condemn other mens writings: To them I answer: That as I condemn no mans diligence, so I know that no one man can satisfie every man: and therefore like as many do esteem greatly other Books, so I doubt not but some will like this my Book above any

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other English Arithmetick hitherto writtem, and
namely, such as shall teach instructors, for whose sake
I have so plainly set forth the Examples, as no Book
that I have seen hath done hitherto: which thing
shall be great ease to the rude Readers.

Therefore (gentle Reader) though this Book can
be but small aid to the learned sort, yet unto the sim-
ple ignorant (which needeth most help) it may be a
good furtherance and mean unto knowledge.

And though unto the King his Majesty privately
I doe it dedicate, yet I doubt not (such is his clemen-
cy) but that he can be content, yea, and much desi-
rous, that all his loving Subiects shall take the use of
it, and employ the same to their most profit. Which
thing if I perceive that they thank fully do, and re-
ceive with as good will as it was written, then will I
shortly with no lesse kindnesse set forth such introdu-
ctions into Geometry and Cosmography, as I have at
times promised, and as hitherto in English hath not
been enterprised, wherewith I dare say all honest
hearts will be pleased, and all studious wits greatly
delighted.

I will say no more, but let every man judge as he
shall see cause. And thus for this time I will stay
my Pen, committing you all to that true fountain of
perfect number, which wrought the whole world by
number and measure: he is Trinity in Vnity, and
always Amen.

Hen

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of ground, upon the breadth given, what
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this worthy Art of *Arithmerick* is unto Gen-
tlemen, Students of the Law, and such other
as are desirous of infallible truth.

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calculated by R. H. and the use thereof.

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10 per 100.

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at 8 per 100.

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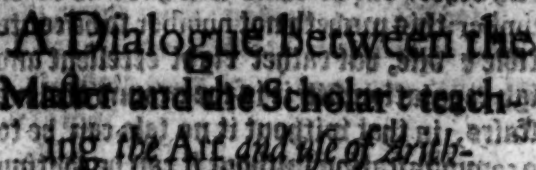
Before

Before the Introduction of
 Arithmetick, it were very good
 to have some understanding and
 knowledge of these Figures
 and Notes.

i	1	one	xx	20	twenty
ii	2	two	xl	40	fourty
iii	3	three	l	50	fifty
iiii	4	four	lx	60	sixty
v	5	five	lxx	70	seventy
vi	6	six	lxx	90	ninety
vii	7	seven	c	100	a hundred
viii	8	eight	cc	200	2 hundred
ix	9	nine	ccc	300	3 hundred
x	10	ten	ccc	600	6 hundred
xi	11	eleven	cccc	1000	a thousand
xii	12	twelve	cccc	1000	a thousand
&c.	&c.	&c.	&c.	&c.	&c.

Certain Tables of interest calculated by H. H.
 at 2 per 100.

Before



The Scholar Pen

[illegible]

all men are able to do it. And yet I have seen many
of them who are not able to do it. And yet I have
seen many of them who are not able to do it.
And yet I have seen many of them who are not
able to do it. And yet I have seen many of them
who are not able to do it. And yet I have seen
many of them who are not able to do it. And yet
I have seen many of them who are not able to do
it. And yet I have seen many of them who are
not able to do it. And yet I have seen many of
them who are not able to do it. And yet I have
seen many of them who are not able to do it.

Reb-
-

any thing alone, and much less talk or bargain
with other, but he shall still have to do with
number: this proveth not number to be contem-
ptible & vile, but rather right excellent and of
high reputation, & it is the ground of all mens
affaires, in that without it no tale can be told,
no communication without it can be continued,
no bargaining without it can truly be ended, or
no business that man hath justly completed.
These commodities if there were none other,
are sufficient to approve the worthinesse of
number. But there are other innumerable, far
passing all these, which declare number to
ceed all praise. Wherefore in all great houses
are Clerks so much desired: & in great Cities
Auditors so richly set: & in all learned Scholes
Arithmeticians so highly to be esteemed: all by reason
Arithmeticians so greatly valued: & all by reason
by number such things that might be said
would farre excell many more.

Scholar. Verily, Sir, if it be so, that these
men by numbering, their cunning do attain, to
whose great works most men do wonder, then
I see well I am much deceived, & numbering
is a more cunning thing then I took it to be.
Master. If number were so vile a thing as you
did esteem it, then would it not so be used in
such brave communication. Crave num-
ber, and answer to this question: How many
years oblige you do all so? & how many oblige
you do all so? & how many oblige you do all so?
Scholar,

Scholar. Mum.

Master. How many dayes in a weeke?
How many weeks in a year? What lands
hath your Father? How many men doth he
keep? How long is it since you came from
Spain to me?

Scholar. Mum.

Master. So that if number want, you an-
swer all by Mummies: how many miles to
London?

Scholar. A poak full of plums.

Master. Why, thus you may see, what rule
number beareth, and that if number be lacking
it maketh men dumb, so that to most questions
they must answer Mum.

Scholar. This is the cause, sir, that I judged
it so vile, because it is so common in talking e-
very where: For plenty is not dainty, as the
common saying is.

Master. For nor store is no store, perceive you
this? The more common that the thing is, be-
ing needfully required, the better is the thing,
and the more to be desired. But in numbring as
some of it is light and plain, so the most part
is difficult and not easie to attain. The easier
part serveth all men in common, and the other
requireth some learning. Wherefore as with-
out numbring a man can do almost nothing,
so with the help of it you may attain to all
things.

Scholar. O yes, sir, why then if I were best to
learn

learn the Art of numbring, first of all other learning, and then a man need learn no more: As all other come with it: as above you have said: Master, I say, not so; but if it be first learned, then shall a man be able (I mean) to learn, perceive, and attain to other Sciences; which without it he could never get.

Scholar, I perceive by your former words, that Astronomy and Geometry depend much on the help of numbring: but that other Sciences, as Musick, Physick, Law, Grammar, and such like, have any help of Arithmetick, I perceive not.

Master, I may perceive your great Exactness by the ordering of your Sciences: but I will let that passe now, because it toucheth not the matter that I intend; and I will shew you how Arithmetick doth profit in all these, somewhat grossly, according to your small understanding; omitting other reasons more substantiall.

Musick.

First (as you reckon them) Musick hath not onely great help of Arithmeticks, but is made, and hath his perfection, of it: for all Musick standeth by number and proportion:

Physick.

And in Physick, beside the calculation of critical daies, with other things, which I omit, how can any man judge the pulse rightly, that is ignorant of the proportion of numbers?

Law.

And as for the Law, it is plain, that the

man that is ignorant of Arithmetick, is not
fittest to be a Judge, neither an Advocate,
nor a Proctor. For how can hee well un-
derstand another mans cause, appertaining
to distribution of goods, or other debts, or of
summes of money, if he be ignorant of Arith-
metick? This oftentimes causeth right to be
hindered, when the Judge either delighteth
not to heare of a matter that hee perceiveth
not, or cannot judge for lack of understand-
ing: this cometh by ignorance of Arithme-
tick.

Now as for Grammer, we thinke you
should not doubt in what it needeth number.
For you have learned that Nouns of all sorts,
Pronouns, Verbs, and Participles are disting-
uished by numbers: besides the variety of
Nouns of Number, and Adverbs. And if
you take away number from Grammer, then
is all the quantity of Syllables lost. And wa-
y other wayes hath number help Grammer.
Whereby were all kindes of speeres found
and made: how if not by number?

Grammer.

But how needfull Arithmetick is to all
parts of Philosophy, they may soon see that
be read either Aristotle, Plato, or any other
Philosophers writings. For all their examples
almost, and their probations, depend of Arith-
metick. It is the saying of Aristotle, that hee
that is ignorant of Arithmetick, is meet for no
Science. And Plato his master wrote a little
sentence

Philoso-
phy.

sentence over his Schoollhouse doore, Let none
enter in hither (quoth he) that is ignorant of
Geometry. Seeing hee would have all his
Scholars expert in Geometry, much rather he
would the same in Arithmetick, without which
Geometry cannot stand.

Divinity.

Armes.

Armies.

And how needfull Arithmetick is to Divi-
nity, it appeareth, seeing so many Doctors ga-
ther so great mysteries out of number, and so
much do write of it. And if I should go about
to write all the commodities of Arithmetick
in civill uses, as in governance of Common-
weales in time of peace, and in due provision
of the Host, summing of their wages, provision
of victuals, victualing of Artillery, with o-
ther Armour; beside the cunningest point of
all, for casting of ground, for encamping of
men, with such other like: And how many
times also Arithmetick is conducing to, all
private Weales, of Lords and all Posses-
sors, of Merchants, and all other occupiers, and
generally for all estates of men, besides Audi-
tors, Treasurers, Receivers, Stewards, Bailiffs,
and such like, whose Offices without Arith-
metick are nothing: If I should (I say) parti-
cularly repeat all such commodities of the
Science of Arithmetick, it were enough to
make a very great book.

Scholar. No, no, sir, you shall not need: For
I doubt not, but this, that you have said, were
enough

enough to perswade any man to think this Art
to be right excellent and good; and so necessary
for man, that (as I thinke now) so much as a
man lacketh of it, so much he lacketh of his
sense and wit.

Master. What are you so farre changed
since, by hearing these few commodities in ge-
nerall, as if that you would be farre chan-
ged if you knew all the particular Commo-
dities.

Scholar. I beseech you, let referre those
Commodities that rest not behind unto their
place, more convenient: and if you shall be so
good as to utter at this time this excellent
treasure, so that I may be somewhat enriched
therein, (if ever I shall be able, I will requite
your paine.

Master. I am very glad of your request, and
will doe it, (if possible, with that so learn if you be
soready.

Scholar. And I to your authority, my selfe The duty
doe subscribe, whatsoever you say, I take it for of a Scho-
lar.

Master. That is too much, and meet for
no man, to be helpeless in all things, without
showing of reason. Though I might of my
scholar, some credence require, yet except I
them reason, I doe it not desire. But now
if you are, so earnestly set this Art to as-
taining heart, it is to omit no time, lest some
other passion coole this great heat, and then
you

you leaue off before you see the end.

Scholar. Whence many there be to conceiue of mistake that witer and turne to the other litle, wylde often tyme, and neuer come to the end; I am none of this sort, as I trust you partly know. For by my good will what I once begin, till I haue it fully ended, I would neuer leave.

Master. So haue I found you hitherto to deed; and I trust you will increas rather then goe back. For better it were never to pary than to be thus; and as in the end way: But I trust you will not bee so; therefore tell me by what I may call you the Science that you desire to geasse.

Scholar. I saye as you know.

Master. What nameth no matter; I would heare whether you know, and therefore I ask you. For great rebuke it were to haue studie in Science, and yet cannot tell how it is named.

Scholar. Some call it Arismetrick and some Anglime.

Master. And what doe these names betoken?

Scholar. What if it please you, of your word I learn.

Master. Both names are corrupted with ten. Arismetrick for Arithmetick, as the Greeks call it, and Anglime for Algorithm, as the Arabians found it, which both betoken.

Apr 14
1544

then the Science of Numbring: for Arithmos
in Greek is called Number: and of it com-
monly Arithmetick, the Art of Numbring:
So that Arithmetick is a Science of Art
teaching the manner and use of Numbring.
This Art may be wrought diversly, with Pen
or with Counters. But I will first shew you
the working with the Pen, and then the other
in order.

Scholar. This I will remember. But how
many things are to be learned to attain this
Art fully?

Master. There are reckoned commonly se-
ven parts or works of it.

Numeration, Addition, Subtraction, Mul-
tiplication, Division, Progression, and Ex-
traction of roots: to these some men add Dupli-
cation, Triplation, and Mediation. But as for
these three last they are contained under the
other seven. For Duplication and Triplation
are contained under Multiplication, as it shall
appear in their place: And Mediation is con-
tained under Division, as I will declare in his
place also.

Scholar. Yet then there remain the first se-
ven kinds of Numbring.

Master. So there doth: notwithstanding I
shall speake exactly of the parts of Numbring:
I must make but five of them: for Progressi-
on is a compound operation of Addition, Mul-
tiplication and Division. And so is the Ex-
traction

tractions of roots. But it is no harm to name them as kinds severall, seeing they appear to have some severall working. For it sojourneth not so much to contend for the number of them, as for the due knowledg and practising of them.

Scholar. Then you will that I shall name them as seven kinds distinct. But now I desire you to instruct me in the use of each of them.

Master. So I will, but it must be done in order: for you may not learn the last so soon as the first, but you must learn them in that order, as I did rehearse them, if you will learn them speedily and well.

Scholar. Even as you please. Then to begin: Numeration is the first in order. What shall I doe with it?

Master. First, you must know what the thing is, and then after learne the use of the same.

Numeration.



Numeration is that Arithmetical skill, whereby we may duely value, expresse, and read any number or summe propounded: or else so apt figures and places set downe any number known or named.

Scholar.

Scholar. Why then me thinketh you put a difference between the value and the figures.

Master. Yes so doe I. For the value is one thing, and the figures are another thing, and that cometh partly by the diversity of figures, but chiefly in the places wherein they be set.

Scholar. When must I know here three things, the value, the figure and the place.

Master. Even so. But yet adde Order to them, as the fourth. And first mark, that there are but ten figures that are used in Arithmetick; and of those ten, one doth signify nothing, which is made like an o, and is privately called a Cypher, though all the other sometime be likewise named. The other nine are called signifying figures, and be thus figured.

A Cypher.

Figures.

1. 2. 3. 4. 5. 6. 7. 8. 9.

And this is their value.

i. ii. iii. iiii. v. vi. vii. viii. ix.

But here you must mark, that every figure hath two values. One always certain, that it signifieth properly, which it hath of his form, and the other uncertain, which he taketh of his place.

A place is called the seat or room that a figure standeth in. And look how many

A place.

figures are written in one summe, so many places hath that whole number. And that must be called the first place, that is next to the right hand, and so reckoning by order towards the left hand, so that that place is last that is next to the left hand. As for example. If three stood before you six men in a row, side by side, and you should tel them as they stand in order, beginning with the man that was next to your right hand; though that were next him should be called the second, and so forth to the furthest from your right hand, which is the first and the last.

Scholar. Sir, I perceiue you well: so might I reckon Letters of any other thing. As if I should write eight Letters after this order, a, b, c, d, e, f, g, h. then must I say, to the first, g, the second, f, the third, e, the fourth, d, the fifth, c, the sixth, b, the seventh, a, the eighth.

Master. That is well done. And after the same sort use hereafter, that what I declare by one example, doe you expresse by another: and so shall I perceiue whether you understand it or no. And so passe over nothing, till you perceiue it well and be expert therein.

Scholar. I pray you how many of these places be there in all?

Master. There is no certain number of them, but they are sometimes more, and sometimes fewer, according to the sum that is expressed.

Numeration.

13

For to many as the figures are, so many are the places, and the last place is so called, not because it is last of all other, but it is the last of that present summe, and it may be the middle place in another summe.

Scholar. We haue thus perceiue this very well, as touching the order of reckoning of the places, but as for the number of them, you say there is no certainty. Shall I therefore be declared the value of the figures by the difference of places, which you called the value uncertain.

Value uncertain.

Master. But first let me hear whether you know perfectly the certain value.

Value certain.

Scholar. Yes sir, as you wrote them, so I marked them.

Master. Write in the first five.

Scholar. By this figure 5.

Master. And how six?

Scholar. Thus, 6.

Master. Write these three numbers, each by itself, as I speak them, vii, lxxx, lxxxvi.

Scholar. 7, 4, 3.

Master. How write you these four other, ii, i, ix, viii.

Scholar. Thus (I wrote) ii, i, 6, 8.

Master. Now there you misse: look on mine example again.

Scholar. Sir, true it is, I was to blame, I take 6 for 9, but I will beware hereafter.

Master. Now then take heed, those, cer-

taine

C 4

certain values every figure representeth when it is alone written without other figures joined to him. And also when it is in the first place, though many other be before it. For example, This figure 9 is 9, standing now alone.

Scholar. How is he alone and standeth in the number or so many letters?

Master. The letters are none of his letters. For if you were in France in the middle of a thousand Frenchmen, if there were no English man with you, you would reckon your self to be alone.

Scholar. So it is. When 9 without those figures of Arithmetick betokeneth 9. Whatsoever other letters be about it.

Master. Even so, and so doth it be in the first place joined with other, how many soever doe follow, as in this example, 3679. You see 9 in the first place, and doth betoken nine as it were alone.

yd Scholar. I perceiue that, and doth not 7 that standeth in the second place, betoken vii. and 6 in the third place, betoken vi. and so 3 in the fourth place betoken three.

Master. Their figures be as you have said, but their values are not so. For as in the first place every figure betokeneth his own value certain onely, so in the second place every figure betokeneth his own value certain, ten times as in the example, 7 in the second place

is seven times ten, and is lxx. And in the third place, every figure betokeneth his own value an hundred times, so the 6 in that place betokeneth 600. And in the fourth place every figure betokeneth his own value a thousand times, as in the afore said number 3 in the fourth place standeth 3000, and in the fifth place every figure standeth 10, his own value a hundred times, and in the sixth place a C, times, and in the seventh place a CCC times, and in the eighth place a CCC, so that every place exceedeth the former ten times.

Scholar. As thus: If I make this number A general Rule.
at all adventures. 01350684, here are eight places. In the first place is 4 and betokeneth four: in the second place is 8 and betokeneth ten times 8 that is 80. In the third place is 6 and betokeneth six hundred: in the fourth place 0 is nine thousand, and 5 in the fifth place is CCC times 5, that is CCC 500 3, in the sixth place is a CCC times 3, that is, CCC 3. Then 1 in the seventh place, one CCC, and 9 in the eighth place, ten thousand thousand times 9, that is CCC 9000. And now I cannot easily nor quickly read it in order.

Master. What shall you practise by this means? If it be put a prick over the fourth figure, and so over the seventh. And (if you have so many) over the tenth, thirteenth, sixteenth, and so forth, will leading two figures between every two prick. And those two

roomed

Ternaries.

rooms between the pricks are called Ternaries.

When thou art in the last prick, and the figures are set down, thou shalt not write any more figures, but thou shalt write the value of the figures as if they were written alone from the left, and at the end thou shalt write so many times thousands as there are pricks.

After that, come to the next three figures, and count them as if they were apart from the rest, and add to their value so many times thousands, as there are pricks before them, and the first place of your whole number. As in the next example, three figures following your first one. As in example 913509684, this your number.

Put a prick after 9 in the fourth place, and after 1 in the seventh place, and then no more (for your places come not to ten) as thus 913509684.

Do now go to the last prick after 1, and take it and the figure that followeth it, and write them alone.

Scholar. 91, that is, 91.

Master. So it is, then write for the number of your pricks, thus 91.

Schol. That is, 91 thousand thousand.

Master. So it is. When take the three other figures from one to the next prick, and write them.

Scholar.

Scholar. When I perceive in the example above I have picked insufficiently for that that Cypher that is picked signifies nothing yet must be have the pick, because he came in the thirteenth place. When will I perceive number that summe. First, there be 12, 9, 9, 9, 9, and then followeth 864, 9, 9, 9. And what shall I now doe? There is a Cypher in the third place, and no figure after him but they that I have reckoned. shewed.

Master. He did serve for them that you have already reckoned, to make them in a place further then they should be. If he were alone, and therefore now ye shall let him go. And so do always when he occupieth that place next before any pick, which is the last of the Ternary, and a Cypher in the last place signifies nothing.

Scholar. Then shall I say but 29, 9, 9.

Master. So, but go forth.

Schol. 105 thousand. Now are all my picks spent, and yet remain 240, so that I must value them, C C C xl, one.

Master. Now can you reckon after the sort: and remember that every such room parted, is called a Ternary, or Trinity, for you have numbered, or valued the summe most truly, and by the aid of the picks each denomination is distinct most plainly.

Scholar. What call you Denomination?

Master

Trinity

Denomination.

Master. It is the last value or name added to any summe. As when I say, an hundred and twenty pounds: Pounds is the Denomination. And likewise in saying, 25 men: Men is the Denomination, and so of order: But in this place (that I spake of before) the last number of every Ternary is the Denomination of it. As for the first Ternary, the Denomination is unites, and of the second Ternary, the Denomination is thousands, and of the third Ternary, thousand thousands or Millions; of the fourth, thousand thousand thousands, or thousand Millions: and so forth.

Scholar. And what shall I call the value of the three figures that may bee pronounced before the Denomination, as in saying, 203000000. that is, two hundred three millions. I perceive by your words, that Millions is the Denomination: but what shall I call CCIII. joyned before the millions?

Master. That is called the Numerator, or valuer, and the whole summe that resulteth of them both, is called the summe, value, or number.

Numerat-
or.
Summe or
value.

Scholar. Now is there any thing else to be learned in Numeration? or else have I learned it all?

Master. I might tell you here who were the first Inventors of this Art, and the reason of

of

of all these things that I have taught you, that I will reserve till ye have learned all the practice of this Art, lest I should trouble you with over many things at the first.

But yet this you must mark, that there are three kinds of Numbers, one called Digits, another Articles, and the third Mixt numbers.

Three
kinds of
numbers.
Digits.
Articles.

A Digit is any number under ten, as these

1. 2. 3. 4. 5. 6. 7. 8. 9.

And 10 with all other that maybe divided into ten parts just, and nothing remains, are called articles, such as are 10. 20. 30. 40. 50. &c. 100. 200. &c. 1000. &c.

Mixt.

And that number is called mixt, that containeth articles, or at the least one article and a digit, as 12. 16. 19. 21. 38. 107. 1005. and so forth: and for the more ease of understanding and remembrance, mark this. The digit number is never written with more then one figure, but the article and the mixt number are ever written with more then one figure. And thus they differ, that the article hath evermore this cypher, 0 in the first place: and the mixt number hath ever there some digit.

Scholar. By these last words I perceive it much better then I did before, and now I think I will never misse to know those things again.

Master. If you remember now all that I have said, you have learned sufficiently the first kind of Arithmetick, called Numeration.

Remember I will expect you now to remember
 the name of a summe pronounced, and
 to write it down in the places of
 its value, and practice it is that maketh ma-
 teriall and prompt in all things. Ifc ma-
 keth ma-
 teriall.

And as you have learned to gather and ex-
 press the name of a summe pronounced, and
 let down before you, to write it down in
 its value, and to write down the figures
 and in the places, any number onely named,
 or recited to you, or if your self imagined; as
 for a proof. Now note you, or write down this
 summe, five thousand two hundred fifty and
 eleven?

Scholar. This troubleth me now, whether
 I should begin at the first; or at the last. For
 reason (me thinketh) should cause me to begin
 at the first, and yet if I write it as you speake
 it, I must begin at the last.

Master. When you know your places per-
 fectly, you may begin where you list; but the
 more ease for your hand is to begin with the
 last, that is to say, as I did speak them, yet for
 the more surety, a while you may begin with
 the first, repeating my words backward thus:
 Seven, fifty, two hundred, five thousand: or else
 sounding them all by their digit, or value, as
 thus: seven, five, two, five; so that way is
 easiest: But then must you look well whether
 there be any cypher in your summe, that bee
 may

now he is in his place; and if he has a
good lumme (as you know it) in about 9,
is there a cypher in the first place, then it
is not lumme, it is about 9; then is there
a cypher, and in the first place, and another in
second, and so forth.

But because this thing is such that can be let forth without using words; I think hereunto at the end of Numeration, to my Table unto and ready for the first use of it.

The following is a list of the names of the persons who have been appointed to the various positions in the various departments of the Government of the State of New York, for the year 1900:

and legal. **Lo this is the Table.** The table is

and the other to the other side of the river.

~~Not yet to be used~~

After 1914 you know your place.

THE UNIVERSITY OF CHICAGO

1941

NOTE: INTEREST IN THIS CASE MAY BE HIGHER THAN IN OTHERS

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...and the ...

17

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371

100

100

100



The Table

23

The right side or hand.

The names of Digits, values certain, or values.

The denominations of the place or value uncertain.

One	Two	Three	Four	Five	Six	Seven	Eight	Nine	The denominations of the place or value uncertain.
1	2	3	4	5	6	7	8	9	
10	20	30	40	50	60	70	80	90	Ten
100	200	300	400	500	600	700	800	900	Hundred
1000	2000	3000	4000	5000	6000	7000	8000	9000	Thousand
10000	20000	30000	40000	50000	60000	70000	80000	90000	Ten thousand
100000	200000	300000	400000	500000	600000	700000	800000	900000	Hundred thousand
1000000	2000000	3000000	4000000	5000000	6000000	7000000	8000000	9000000	Million
10000000	20000000	30000000	40000000	50000000	60000000	70000000	80000000	90000000	Ten million
100000000	200000000	300000000	400000000	500000000	600000000	700000000	800000000	900000000	Hundred million
1000000000	2000000000	3000000000	4000000000	5000000000	6000000000	7000000000	8000000000	9000000000	Billion

This Table (as you may see) hath eleven Places, and in each of them are set all the Digits, whose certain value is written on the right hand of the Table; and the value uncertain on the left hand; so that by this Table you may learne both how to expresse any number that you will, if that it exceed not eleven

eleven places) that is to say, M^{C} . thousand millions, and so may you by help of it, value all sums proposed under the said number.

For example, take the summe that I proposed before, which was five thousand, two hundred fifty and seven. And if you will expresse it, take the first number (as I speak it) which is five D . whose valuer or certaine value is 5, and his uncertain value, or denomination is D . first you shall seek at the right hand of the valuer 5. Then seek along under the title of denomination toward the left hand till you finde thousands, and under it, right at the foot of the Table is the number of the place that is in the fourth, wherein you must write your digit or valuer 5.

Afterward come to the second part of the number, two hundred, whose valuer is 2, and his denomination C . Seek two at the right hand of the Table, and go along under the denomination toward the left hand, till you come under C . then look to the foot of the Table, and there you shall see the number of the place, that is to say, the third, wherein you must set your digit 2.

Then doe so by your other two numbers that remain, and you shall find 5 in the second place for your fifty, and 7 in the first place for your seven. And thus you may do with other numbers.

Scholar. Gaffer, I thank you heartily. I perceiue you seek to instruct me most plainly

and

and briefly, and not to hide your knowledge
with words too, as many do. For this rule
into plain, that I can believe it no plain.
And though it seem somewhat long, yet I
perceive it to be a fine way.

Master. So it is, and though it be long, yet it
is neither too long, neither too plain for young
learners that lack practice: for this Table is
in need of a Teacher to them that lack one.
And now I trust I have said enough of Nu-
meration, which after you have well practised,
then may you learn forth.

Schol. Yet I pray you in one thing to tell
me your judgment. Why do men reckon the
order of the places backward, from the right
hand to the left?

Why num-
bers are
written
backward.

Master. In that thing all men be agree, that
the Chaldees which first invented this Art, do
set these figures as they set all their Letters,
for they write backward, as you learn it, and
so do they read. And that may appear in all
Hebrew, Chaldee and Arabick Books: for they
be not onely written from the right hand to
the left and so must be read, but also the right
end of the book is the beginning of it, whereas
the Greeks, Latins, and all Nations of Eu-
rope, do write and read from the left hand
toward the right: and all their Books begin
at the left side.

Schol. What reason hath satisfied me.

Master. It neither satisfieth me, neither
liketh me well, because I see that the Chaldees

and Hebrews do not so use their own Numbers, as at another time I will declare. But this plain reason may best satisfy you presently, that seeing in pronouncing of Numbers we keep the order of our own reading, from the left hand to the right: and again, we do ever name the greater numbers before the smaller: it was reason that the lesser places containing the lesser numbers, should be in on the right hand, and the greater places containing the greater numbers, to proceed toward the left hand.

Scholar. This reason is to me so plain, that it seemeth now against reason to make doubt of that order. So that now for Numeration I am satisfied; hoping that practise shall make me fully ready and expert in it. And in the mean season I desire to learn the other kinds of Arithmetick.

Master. That is well said: but what should you next learn? can you tell?

Scholar. I remember you said that Addition was next.

Master. When so, and what that is, must you first know.

And of the book is the beginning of the Greek, Latin, and all Nations of Europe, be taught and read from the left hand toward the right: and all their Books begin

Addition

And of the book is the beginning of the Greek, Latin, and all Nations of Europe, be taught and read from the left hand toward the right: and all their Books begin

Addition.



Addition is the gathering together and bringing of two numbers, or more into one summe. As if I

have 160 Books in the Latine tongue, and 136 in the Greek tongue, and I would know how many they bee in all, I must write these two numbers one over another, writing the greatest number highest, so that the first figure of the one being under the first figure of the other and the second under the second, and so forth in order.

When you have so done, draw under them a right line, then will they stand thus.

Now begin at the first places toward the right hand alinaped, and put so.

ther the two first figures of these two numbers, and looke what cometh of them write under them, right under the line.

As in saying 6 and 0 is 6, write 6 under 6, as thus:

And then go to the second figures, and do likewise: as saying 3 and 6 is 9, write 9 under 6 and 3, as here you

see. And likewise do you with the figures that be in the third place, saying, 1 and 1 be 2, write 2 under them, and then will your whole summe appear thus:

$$\begin{array}{r} 160 \\ 136 \\ \hline 296 \end{array}$$

$$\begin{array}{r} 160 \\ 136 \\ \hline 96 \end{array}$$

$$\begin{array}{r} 160 \\ 136 \\ \hline 296 \end{array}$$

$$\begin{array}{r} 296 \\ \hline 296 \end{array}$$

So that now you see that 160, and 136, do make in all 296.

Scholar. What? this is very easie to do, me thinketh I can do it even since.

There came through Cheapside this day of carrell: in the first was 848 sheep, and in the second was 186 other beasts.

Nowe two summes I must write as you taught me thus, then I put the two first figures together, saying, 6 and 8, they make 14. Nowe must I write under 6 and 8, 14.

Master. Not so: and here you are twise deceived. First, in going about to adde together two summes of sundry things, which you ought not to doe, except you keepe onely the number of them, and care not for the things: For the sum that should result of that addition, should be a sum neither of sheep, nor of other beasts, but a confused sum of both. Nowe heft sometimes yee shall have sumes of diverse denominations to be added, of which I will tell you anon: but first I will shew you where you were deceived in another point, and that was in writing 14, which came of 6 and 8, under 6, 8, which is impossible; for how can two figures of two places be written under one figure and one place?

Scholar. Truth it is, but yet I did not understand you.

Master.

Master. I said indeed, that you should
 write that under them that did result of them
 both together, which saying is alwayes true
 if that summe doe not exceed a digit: but if it
 be a more number, then must you write the dig-
 it of it under your figures as you have said
 before, and if it be an article, then write it be-
 der them, and in both sorts you shall keep the
 article in your minde, and therefore when you
 have added your second figures, which oc-
 cupy the place of tens, you shall put that one
 thereto, which you kept in your minde, for
 though it were ten indeed, yet in that place it
 is but as one, because that every one of that
 place is tenn, for that it is the place of tens.
 And in like manner, if you have in the second
 place any great a number that it amounteth a-
 bove, then write the digit, and reserve the
 article in your minde, ever adding it to the
 next place following, and so of all other places,
 how many soever you have. And if you
 have any more number when you have added
 your last figures, then write the digit un-
 der the last figures, and the article in the
 next place beyond them: so shall your num-
 ber resulting of Addition have one place
 more then the numbers which you shall add
 together.

Scholar. Now doe I perceiue you, and the
 reason of this is, (as I understand) because
 that no one place can contain more 9, which
 is the greatest figure that is, and then all tens

of articles must be put to the next place following: so, every place (as I may see) exceeding the other place next before him by 10 and not 100.

Now, if it please you, I will return to my example of Castell. But I remember you said, I might not adde summes of sundry things together, and that I may see by reason. Matter. Truth it is, if you seek the summe of any thing, but if you onely seek a bare summe, and have no respect to the thing, then were it better to name the summe onely without any thing, as in saying 848, without naming sheep or any thing else. And likewise 186, naming nothing.

Now let me see how you can adde those two summes.

Scholar. I must first set them so that the two first figures stand one over another, and the other each one over his fellows of the same place: then shall I draw a line under them both. And so likewise of other figures, setting

alwayes the greatest number highest; thus shall followeth.

When must I adde 8 to 8, which shall make 14, that is a mixt number, therfore 848: soe must I take the digit which is 4, and write it under 8 and 8: keeping the article 1 in my minde, thus:

Next that I come to the second figures, adding them together, saying 8 and 4 make 12; to the which I put the one reserved in my minde, and that maketh 13; of which

Addition.

3

which number I write the eight
under 8 and 4 and keep the article
in my minde, thus :

When come I to the third figures,
saying, 1 and 8 make 9, and 1 in
my minde maketh 10. Sir, shall I write the
Cypher under 1 and 8.

Master. Yes.
Scholar. Then of 10 I write the Cypher
under 1 and 8, and keep the Article in my
minde.

Master. What needeth that, seeing there
follows no more figures.

Scholar. Sir, I had forgotten, but I will
remember better hereafter. When seeing I am
come to the last figures, I must
write the Cypher under them, and
the Article in a further place after
the Cypher thus :

Master. So now you see, that of 848, and
186 added together, there amounteth 1034.

Scholar. Now I think I am perfected in
Addition.

Master. That will I prove by this example.
There are two armies of Soldiers: in the
one are 106800, and in the other 9400. How
many are there in both armies say you.

Scholar. I will set them one over another,
beginning with the first num-
bers on the right hand, thus :

But whether number will not
match the other number.

Master

Master. What forsooth not.

Scholar. When do I adde 9, to 9, and there amounteth 18, that must I write under the first place thus:

106800
2400

Master. Well said.

Scholar. Then likewise in the second place I adde 0 to 9, and there ariseth 9, which I write under the second place thus:

106800
9400

Then I come to the third place, saying, 4 and 8 make 12, of which I write the digir 2 and keep the article 1 in my mind thus:

106800
9400
200

Then I adde 9 to 6, which make 15, to that I adde the article 1 that was in my mind, and it is 16, I write 6 under 6 and 9, and keep one in my mind thus:

106800
9400
6200

Master. Why doe you not write both figures seeing you are come to the last couple of numbers?

Scholar. Nay, reason thewith me, that I must adde that article that is in my mind unto the next figure of the upper summe, though there be no more in the lower summe.

Master. What is well considered: thus do so.

Scholar. When say I, 0 in the ober summe and 1 in my minde maketh 1, that write I under

understand. When thou hast there yet one more
in the over summe, which hath none to be ad-
ded to it, for there is none in the nether sum,
nor yet in my mind; therefore I think I must
write that when as thou

Master. *Pea.*

Scholar. When both my whole summe ap-
pear thus:

Master. If you mark this

you have learned perfectly

the common Addition of

all summes which are of one denomination:

so that you observe this also, that in Addition

you must have three numbers at the least:

the first how can you say that you have none?

ever let the greatest number be in the high-
est, for that is the best way, though it be not

necessary, but it is the best way, though it be not

needful, but it is the best way, though it be not

needful, but it is the best way, though it be not

needful, but it is the best way, though it be not

needful, but it is the best way, though it be not

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needful, but it is the best way, though it be not

needful, but it is the best way, though it be not



pen to come. For your better understanding
take this example for all. I would adde these thirteene summes. 11 02 889
into one, which I set after this manner 194 999
ner: then do I beginne and gaad 999
ther the summe of the first row of 1013699
Figures, which cometh 607, (for 1002399
I take 9 there tenne times, and 14099
that is 90) then 9 and 8 is 17, that is 1699
is in all 107, of which summe I adde 99
write the 7 under the first row of 1001299
Figures, and then for that 100 is 1000099
ten times, I keep tenne in minde 99 10099
which ten I make adde unto the next sum 892
row of 9 figures, which are in the second 379
row place 100 100 100 100 100 100 100 100 100
which second row of 9 figures (when they are
added together with that ten that I have in
my minde) make in all 12, of which summe
write the digit 2 under the second row, and
then (for that 100 containeth twelue tenths)
I keep twelue in minde to be added to the
third place of row of 9 figures, which being
added together, make in all 60, the cypher 0
I set down under the row of 9 figures in the
third place of row of 9 figures 100 100 100 100 100 100 100 100 100
And the Figure 6 I keep in minde to be ad-
ded to the row of 9 figures in the fourth place,
which (when they are added together) make
20. The Figure 0 I write 9, I set down under
the fourth place. And because it is my last
work, I set down the 2 also that I have in
my

my minde to the 9 in the first place; as in 4889
 so those summes do make in all 4889
 29057. But (for your more easie worke) when you have an addition
 of so many summes to be added together, you were best part that
 summe into two or three parts, and then worke them severall, and so put
 their additions together, and this were the best thing you could do
 when other many summes fall to be added.

Scholar. This seemeth somewhat hard, by the reason of so many numbers together.

Master. I think if I doe often practise, even with the same example, either by working of it alone, or else by parting it as you said even now, that I shall be able to do so shortly with any other sum.

Master. So shall you. For it is often practise that maketh a man quick and ripe in all things, but because, as well in great summes as in small, there may chance to be some error, I will teach you how you shall prove whether you have done well or no.

Scholar. That were a great help and ease.

Master. Begin first with the highest number, and then to all the other orderly, and adde them together, not having regard to those places, but as though they were all united.

The proof
 of Addition.

and still as you makest increments above 9
 cast away 9. When you have over casting a
 way 9 as often as it amounteth thereto; and
 so do till you have gone over all the numbers
 that you intended first to add; and together
 they remaineth after such addition and casting
 away of 9, write it in some roth place by the
 end of a line, for the better remembrance; and
 thus is the first part of your work proved.
 Then secondly, put together the figures that
 result of the addition under the line, still ca-
 sting away 9 also. And then that that remain-
 eth write at the other end of the line; and if
 those two figures be like, then have you well
 done, but if they be unlike, then have you mis-
 sed. As for example, in this present summe.
 The first figure of the other line is 9, let him
 go, then 8 and 8 is 16, take away 9 there re-
 steth 7, and add that 7 to 4 that followeth,
 and it maketh 11, from which if you take 9,
 there resteth 2. When come to the next roth
 whose first and second numbers are 9, there-
 fore overpasse them both, and take the 5 to the
 2 which did remaine in the first row, that ma-
 keth 7, put thereto the 4 following, and that
 maketh 11; thence take 9, and there remaineth
 2. Next unto that, go to the third line, whose
 two first numbers put away let passe because
 they are alike; then take the two figures of 2,
 which (with the other two that remained, in
 the second row) make 6. When go to the
 fourth row, whose two first numbers let go,

and

Addition.

first 10, from that I take 9, and there remaineth
one the next figure is 9, and therefore I let
him alone, so that I am remaining: which I
let at the end of a line thus: ~~the sum is 10~~

Then I come to the Total sum, and there
I finde that all the Summes put together make
10, from which I take 9, and there remaineth
also, which I put at the other end of the line,
thus: ~~all is 10~~

And because they be like, I know that I
have well added.

Master. So you know now both how to
make five summes, or more together, and also
how to prove whether you have done welth,
no, and now I will teach you how to add
summes of divers denominations together:
which thing can never be but when the one
Denomination is such that it containeth the
other certain times. And yet you shall add
them to the other, not after this sort (as you
did them that were of one denomination) but
after such a sort as I will now shew you, that
is to say:

If you have a summe of divers denomina-
tions, then look that you set every denomina-
tion by himselfe with some note or figure
of his denomination, as they are wont to
be written. When write your other Summes
in under that first, that every such set un-
der the other of the same denomination.
As for example, if your denomination be
pounds

Addition
of num-
bers of di-
vers deno-
minations.

pounds, shillings, and pence, write pounds under pounds, shillings under shillings, and pence under pence: and not shillings under pence, nor pence under pounds.

Scholar. Now that you have spoken it, methinketh it needeth not to warne me of it, for it were against reason so to confound summes: but yet if you had not spoken of it, peradventure I should have been deceived in it.

Master. If you do say it is plain, I will speak no more of it, but with an example make the matter to appear evidently.

First, one man oweth me 22 l. 6 s. 8 d. and ther oweth me 5 l. 16 s. 6 d. and another oweth me 4 l. 3 s. I would know what this is all together: Therefore must I

li.	s.	d.
22	6	8
5	16	6
4	3	0
<hr/>		

first set down my great summe, and then the other, every one under his denomination agreeing to the greatest sum, as here you see with a line under them.

Then must I begin at the smallest numbers (which must alwaies be set next to the right) and adde them together: and if the sum will make 1, 2, 3 of the next denomination) then must I keep it in my minde till I come to that place, and under that first place must I note the residue (if there remain any of the same denomination:) but if there remain none, then need I to write under it nothing. And this is all that you must mark in this Addition: for all other things are like to the manner

manner of Addition before mentioned: Therefore the chiefest point of this Addition is, to know the values of common Coines, and rated summes. As how many shillings be in a pound, how many pence in a shilling, of which (and of other like things) I will instruct you hereafter in teaching of Reduction: But now I may not disturbe your wit from the thing that we are about.

Wherefore let us returne to that former example which I proposed of the Debtors: which summes when I had set orderly, they stood thus with a line under them.

When to adde them into one summe I must begin at the right hand where the smallest denomination is, and adde them together, first saying, 6 and 8 make 14. Now, seeing these 14 are pence, which contain one shilling and 2 pence: the 2 pence I set down li. s. d. under the line of pence: and the 22—6—8 one shilling I keep in my minde 5—16—6 to carry to the next row being the 4—3—0 place of shillings.

When do I adde the shillings together, saying, 1 in my minde and 3 make 4, and 6 make 10, and 6 make 16, and 1 in the second place which standeth for 10, make 26, which is 1 pound 6 s. The 6 s. I set li. s. d. down under the place of shillings, as appeareth in the example. And the 1 pound I keep to 4—3—0 carry to the pounds.

Then

Then come I to the pounds, adding them
all together, saying, 1 that I keep and 4 make
5, and 5 make 10, and 2 make 12. The figure
of digit 2 I set down right under that place
or row of pounds where I gather them, and
the article 1 I keep to carry to the
next place, saying, 1 in minde li. s. d.
and 2 is 3, which 3 I set down 22—6—8
directly under the 2. And then 5—16—6
appeareth my whole summe 4—3—0
thus: 32—6—2

And thus must you do with any such like
summes whatsoever, whether they be money,
weight, or measure, which (if you practise
divers summes) you shall be well acquainted
with the feat of Addition.

But now can you tell how to prove this
Addition, or such other like of divers denomi-
nations, and to try whether you have well
done or no?

Scholar. I would I could.

Master. That shall you do by this means:
you must make a Croce which shall have
as many lines as you have sundry Denomi-
nations in your Addition: As if

you have but two Denominations, then you may make it thus: that
the other part and neither part may
serve for one Denomination. And
if you have three Denominations (as pounds,
shillings, and pence) then must you make
three

Proof of
Addition
of fivers
denomi-
nations.

thre lines, thus: The upright line may serue for pounds, and the highest thwart line for shillings, and the low-
est for pence: as for example, the sum which we last wrought:

li.	s.	d.	
21	6	8	6
3	16	6	6
4	13	0	2
32	6	2	5

For the proof of which, because it containeth thre Denominations, I must make a crosse of thre lines as in the example before. When I reckon first at the right hand the pence, 6 and 8 make 14, from which I take 12 for the next Denomination, that is to say, a Shilling, and there resteth 2, which I must write at one end of the nether thwart line.

After that I gather the sum of the Shillings 3, 16, 6, which maketh 25, to whom I put 1 that I took of the pence, and that maketh 26, from those I take 20, the quantity of the next greater Denomination, that is to say, a pound, and there resteth 6, which I write at the end of the highest thwart line.

Wherby, I adde together the pounds, 4, 5, and 2, which make 11. to them, I adde the one that came of Shillings, and they make 12, from whence I cast 9, and thereresteth 3, that 3 I joine to the 2 in the next place, and they make 5, which 5 I set at the Crosse
also

also. And thus is my first part of my work
proved: and now I shall go on to the second.

What done I come to the tenth solmine un-
der the line, and examine it, beginning at the
pence, where I finde but 2, and cannot take
from him: therefore I set him at the other
end of the nether thwart line: then I come to
the shillings, where I find onely 6, which
(because it is less then nine) I set it at the
other end of the line of shillings: that is, the
obermoſt thwart line.

Last of all, of the 3 or 4. I take three times
 9, which is 27, and there remaineth 5, which
 I write under the upright line: either else I
 may reckon them simply without any respect
 of their valuation or place: saying, 2 and 3
 make 5, which because it is lesse then nine,
 I set under the upright line as before. Then
 I consider every number, comparing it to the
 number that is against it: and because I find
 them to be every one like his match, I know
 that I have well done.

Scholar. This Crosse I perceiue doth serue
for these 3 Denominations, pounds, shillings,
pence : but what if I had s. d. ob. and qd. 121

Master. These lines as I have said, do
serue for three Denominations, such as they be,
as here three do serue for pounds, shillings,
and pence : but if you have no pounds in your
sum, then may they serue for shillings, pence,
and halfe pences : yea, for 8. ob. and q. or in
weight for ℥. q. and l. or in measure for Elles,
Quarters,

Quarters, and Nails, if you have no greater Denomination : so that you remember that the upright line serveth for the greatest Denomination, and the highest thwart line for the next, and the lowest for the least.

And so if you have four Denominations,
you must make your crosse with so many lines.
And if your summe be of more Denominations, make so many
lines in your crosse. And thus
till I make an end of Addition
on, saying what here (for the better understand-
ing of sh^e in sh^e) I have set you down certain
examples both of money, weight, and measure,
with their workes and proofs.

Examples of Addition

23	10	4	130	17	10
45	6	2	28	6	18
37	2	9	13	13	14
25	15	6	120	0	0
<hr/>			<hr/>		
131	13	5	19	13	10
<hr/>			<hr/>		
4	4	4	The proofs 8		
<hr/>			<hr/>		
25	15	6	120 0 0		
<hr/>			<hr/>		
131	13	5	19 13 10		

Addition.

45

C.	q.	li.	yards.	q.	nayles.
34	1	3	17	3	3
12	2	2	35	2	1
7	3	4	26	1	3
13	0	13	54	2	0
57	2	22	134	1	3

2	2	1	1
4	4	3	3
3		8	



Subtraction

E 4

Subtraction.

Scholar.



Hen have I learned the two first kinde of Arithmetick : now (as I remember) doth follow Subtraction, whose name (me thinketh) doth sound contrary to Addition.

Subtraction.

Master. So it is indeed : for, as Addition increaseth one grosse summe, by bringing many into one : so contrariwise, Subtraction diminisheth a grosse summe by withdrawing of other from it. So that Subtraction or Rebating is nothing else but an Art to withdraw and abate one summe from another, that the remainder may appear.

Scholar. What doe you call the Remainder?

Master. What you may perceive by the name.

Scholar. So me thinketh : but yet it is good to aske the truth of all such things, lest in trusting to mine own conjecture, I be deceived.

Master. So it is the surest way. And, as I see cause, I will still declare things unto you so plainly, that you shall not need to doubt. Howbeit, if I do overpasse it sometimes, (as the manner of men is to forget the small knowledge of them to whom they speak) then do you put me in remembrance your selfe,

self, and that way to surest.

And as for this word that you last asked me, take you this description: The Remainer is a summe left after one Subtraction made, Remainder. which declareth the excess or difference of the two other numbers, as if I would abate or subtract 14 out of 18, there should remain 4, which is called the Remainer, and is the difference betwixen those two numbers 14 and 18.

Scholar. I perceiue then what Subtraction is: now resteth to know the order how to work it.



Master. What shall you do by this means.

First, you must consider, that if you should go about to rebate, you must have two sundry summes proposed: The first, which is your grosse summe, (or summe totall) and it must be set highest: and then the rebatement, (or sum to be withdrawn) which must be set under the first, (together it be in one parcell, or in many) and that in such sort, that the first figures be one just over another, and so the second, and third, and all other following, as you did in Addition: then shall you draw under them a line, and so are your summes duly set to begin your working.

Then begin you at the right hand (as you did in Addition) and withdraw the lesser number out of the bigger, and if there remain any thing, write that right under them beneath the line: and if there remain nothing

(by

(by reason that the two Figures were equal)
then write under them a cypher of nought:
And so do you with all the other Figures,
evermore abating the lower out of the higher,
and write under them the Remainder still, till
you come to the end: And so will there appear
under the line what remaineth of your grosse
summe after you have deducted the other sum
from it, as in this example.

I received of your Father 48 s. of which I
have laid out for you 36 s. now would I
know what doth remain. And therefore I
set my number thus in order. First, I write
the greatest summe, and under
him the lesser, so that the Fi-
gures at the right side be even
one under another, and so the
other thus.

When I do rebate 6 out of 8,
and there resteth 2, which I
write under them right be-
neath the line thus.

When I go to the second Fi-
gures, and do rebate 3 out of 4,
where there remaineth 1, which
I write under them right, and
then the whole summe and op-
eration appeareth thus.

Wherby it appereth, that if I rebate
36 out of 48, there remaineth 12.

Scholar,

Scholar: Now will I proue in a greater summe, and I will subtract 2367924 out of 3468946 , thus: 3468946
 2367924
 I thus set in order thus: 3468946
 2367924

Then do I begin at the right side, and deduct 4 out of 6, and there resteth 2, which I write under them. Then go I to the second figures, & withdraw 2 out of 4, and there remaineth 2, which I set under them also, then I take 9 out of 9 and there resteth 0, which I write under them (for you say, that if the figures be equal, so that nothing doth remain, I must write the cypher 0 under them.)

Master, It was well remembered: now go forth.

Scholar: When I come to the fourth place, and draw 7 out of 8, and there remaineth 1, which I write under them also. When in the fifth place, I take 6 out of 6, and there resteth 0, (for if I write under them the cypher 0.) When in the sixt place, 3 rebated from 4 there remaineth 1, which I write under them, and likewise in the seventh and the last place, 2 taken from 3 there is left 1, which I write under them: 3468946
 2367924
 so have I done my whole working, and my summe do appeare thus: 1101022

See, that (if I do rebate 2367924 out of 3468946) there remaineth 1101022 .

Master: This is well done. And that you may be sure to perceiue fully the Art of Subtraction,

raction, let me see how you can subtract
 52984732 out of 8150003456 .

Scholar. First, I set down the greatest
 summe, and after that, I write under it the
 lesser number, begin-
 ning at the right side,
 and then my Figures
 will stand thus:

8150003456
 52984732

Note.

When take I 2 from 6, and the rest is 4,
 which I write under them. When do I with-
 draw 3 from 5, and there remains 2, which
 I write under them. When take I seven out
 of 4, but that I cannot, what shall I now do?

Master. Marke well what I shall tell you
 now, how you shall do in this case, and in all
 other the like: If any figure of the nether
 sum be greater then the figure of the summe
 that is over him (so that it cannot be taken out
 of the figure over him) then must you put 10
 to the over figure, and then consider how
 much it is, and out of that whole summe, with-
 draw the nether figure, and write the rest un-
 der them. Can you remember this?

Scholar. Yes, that I trust I shall. Now
 then in mine example where I should have
 taken 7 out of 4, and could not, I put 10 to
 that 4, which maketh 14, from it I take away
 7, and there resteth 7 also, which I write un-
 der them.

Master. So have you done well. But now
 must you mark another thing also: that
 (when

(whensoever you do so put ten to any Figure
of the over number) you must adde one till 10
the Figure or place that followeth next in the
nether line: as in this example there follow-
eth 4, to which you must put 10, 8750003456
put 1, and make him 5, 52984732
and then go on as I have
taught you. 018732

Scholar. When shall I say, 4 and 1 (which
I must put to him for the 10 that I added to 4
before) make 5, which I should take out of 3,
but that cannot be; therefore I must put to it
also 10, and then it will be 13, from which I
take 5, and there resteth 8 to be written under
them: and because of that 10 added to the 3,
I must adde one to 8 that followeth in the ne-
ther line, and that maketh 9, which I should
take out of 0 and cannot; therefore I put there
to 10, & that maketh 10, from 10 I take 9, and
there remains 1, which I write under them.

Thus do I adde 1 likewise to the next fi-
gure beneath, which is 9, and that maketh 10;
that 10 should I take out of the figure above;
but I cannot, for it is 0; therefore I put 10 to
it, and so take I 10 out of 10, and there resteth
0 to be written under them.

Then come I to the next figure, which is
2, and to him I do adde 1, which maketh 3,
that 3 I cannot take out of nought, there-
fore of that nought I make 10, and thence
doe take 3, so there remaineth 7 to be writ-
ten under them: likewise doe I put 1 to 5,
that

that 5, and make it 15, from which I rebate 6
 and there remaineth 9, which I write under
 them. Now have I 825003456
 spent all the neither
 Figures, and what
 shall I do more? 8197018724

Master. You should have added one to the
 next figure following (if there had been any)
 because you added 10 to the last figure before
 of the over line: but being there is no figure
 following, you must adde that one to the place
 following, and then deduct that one from the
 number above.

Scholar. When shall I say, because I bor-
 rowed 10 to the over 5, I must put 1 in the
 next place beneath, that is under 2, then must
 I subtract that 1 from 2, and there resteth 1
 to be written under that in the ninth place.
 Now I have no more to subtract, for there
 is not any figure remaining beneath, neither
 yet any unite to be added, because I borrow-
 ed not 10 to the figure last before: and yet is
 there 8 remaining in the over line, which I
 think (by reason) should be set at the end of
 the figures in the lowest row, which is under
 the line, for because there was nothing taken
 from it.

Master. That is well considered, and rea-
 son teacheth so indeed.

Scholar. But Sir, I beseech you, shall I
 allowes when any number so remaineth a-
 lone, as thus 8 do, write him under the line
 straight

straight against his own place.

Master. Now, what else? whether they be one or many: and this well remembred, you have sufficiently learned Subtraction; Now, be it, because of certain things that might deceive you, if you did not take good heed to your working, I will propose to you another example of many numbers to be subtracted, as thus: I receiv'd of a friend of mine to keep 2869 Crowns, of which at one time I deliver'd him again 500. at another time 368, at another time 440, at another time 80, and another time 64, now would I know how many do rest behind. Therefore first I set down my grosse sum, 2869 Crowns receiv'd. and underneath it I set

all the parcels thus, and

500	} delivered.
368	
440	
80	
64	

under them a double line.

Then first I begin at the first place, and gather together the summe of all those lines (save the obermost) in their first Figures: and so I doe with all the figures of the second place, and so forth, as I did in Addition, save that I leave out the highest row of numbers (as the line warneth me) and that summe so gathered between the double line, is the summe deliver'd in all: which summe I do afterwards subtract out of the highest row of numbers, and the remainder do I set under the nethermost line:

Note.

as for example.

I set the summes as 2869 Crowns received.
 before: then do I gather 500
 ther the first figures 368
 of al the places deliue- 440 Delivered,
 red together: where I 80
 finde but 4 and 8, that 64

maketh 12, (for three
 Cyphers increase no 1452 Delivered in all.
 summe in Addition, as 1417 Rest behinde.

you learned before:) of the 12 therefore
 do I write the digit 2 between the double
 line and keep the article in my minde, till I
 come to the second place, where I finde 6, 8,
 4, 6, that maketh 24, to them I put the arti-
 cle in my mind, and it is 25, of which I
 write 5 under the second place, and keep the
 digit 2 in my mind for the third place, where
 I finde 4, 3, 5, that makes 12, to the which
 I adde the 2 in my mind, and it maketh 14,
 thereof I write the 4 under the third place,
 and because there remains no more figures to
 be added, I write the digit in the fourth place,
 as you see in the example, and so it appeareth.
 I have deliuered in all a thousand four hun-
 dred fifty two Crowns.

Then come I to the subtracting of this
 summe between the lines, for by Addition
 it is equall to the five parcels ober it. Where-
 fore I proceed to subtract it from the ober-
 most summe, saying, 2 from 9 remains 7 to
 be written under them beneath the lowest
 line.

line: When in the second place I take 5 from 6 and there resteth 1 to be written under them. When in the third place, 4 from 8 resteth 4. Last of all, in the fourth place, 1 from 2 remaineth 1. And thus I see that after those five summes are subtracted from 2869, the Remainder is 1417.

To Schollar: This I perceive: but is there no shorter way and more speedy?

Master: Yea, when you are a while exercised therewith: for you may (as fast as you can gather the numbers together) withdraw them out of the highest summe: But if in quantifying those numbers added together, exceed the highest summe or upper number, then shall you as before hath been taught you, imagine to borrow 10, or 20, or 30 more, as need shall require, and put them to the upper number, to help to further the abatement, reserving or restoring the articles that you borrowed to the next place again: and so still go forward till you have ended your work: as for example. In the last summe proposed: I gather first, in the first place 4 and 8 that maketh 12; which I should deduct or take out of 9 in the upper number above the line, but I cannot: that therefore I add unto 9 an article of 10, and maketh the upper number 19, from whence I take 12, then there resteth 7, then for the article 10 I add to the next place of money delivered, saying, 1 that I bring, and 6 make 7, and 8 make 15, and 4 make 19, and 6 make 25

¶

which

An abridgment of the former manner of Subtraction.

which 25 I would take out of 6 in the upper number, but I cannot. Wherefore I adde 1 tens or 20 unto 6 in the upper number, and that maketh 26, then 25 out of 26, resteth 1, the tens which I borrowed, or have in my minde I adde to the next row, or summe delibered; saying, 2 that I bring, and 4 make 6, and 3 make 9, and 5 make 14, then 14 out of 8 I cannot take, but 14 out of 18 resteth 4. Also because there are no more places to be added, the one that I borrowed, or have in my minde, I rebate from two in the upper line, and there remaineth 1, which I set down in the remainder line: and so my summe appeareth (as before) to be 1417 Crowns.

So thus have you now a shorter way.

Scholar. I like both waies well, and I perceive both well: yet, as in the working it seemeth somewhat long, so in the other it leaveth very much (me seemeth) to remembrance, and therefore may cause error quickly: except a man have a quick and an exercised remembrance. But yet for the sharpening of my wit, be your patience (if you will give me leave) I will try what I can do in a like summe, to work it the shortest way: whereupon I would subtract out of 49391264, these three parcels;

7 hundred thou. or seven hundred thousand
15 thou. and 100
and hence to subtract the rest of the
I understand this. 49391264
7 hundred thousand 15 thousand 100
hundred

Therefore I set
 them first in due or-
 der: then I gather
 the parcels of the
 first place, which
 are 8. 2. 1. that is a

$$\begin{array}{r}
 40301964 \text{ Charge.} \\
 20003428 \\
 10002432 \text{ Disch.} \\
 10101461 \\
 \hline
 43
 \end{array}$$

11, which I should take or deduct out of 4,
 which is over him, but I cannot: therefore I
 adde an article, or one ten to 4, which maketh
 14, then 11 out of 14, there resteth 3 to be
 written under the first place between the two
 lines.

Then come I to the second place, saying, 1
 that I borrowed to have in my mind, and 6
 make 7, and 3 make 10, and 2 make 12, which
 I cannot take from 6, therefore I adde 10 to
 6, which maketh 16, and then 12 from 16,
 resteth 4, which I write under the second place
 between the two lines.

Then come I to the third place, saying, 1
 that I borrowed, or have in mind, and 4
 make 5, and 4 is 9, and 4 make 13, which I
 should take out of 9 that is over them, but I
 cannot: therefore I adde 10 to 9, which ma-
 keth 19, then 13 out of 19, rest 6.

Then come I to the fourth place, saying, 1
 in my minde, and 1 is 2 and 2 is 4, and 3 make
 7, which, because it cannot be taken from 1, I
 take it from 11, and there resteth 4.

After that, I come to the fifth place, where
 are only these cyphers, which make nothing,

unto which I adde 1 in my minde, then should I take that (that is to say) 1 from the figure over them, which is also a cypher, therefore I say thus, I cannot take 1 from 0, but 1 from 10 remaineth 9: so must I write 9 under them. When in the first place I finde but 1, and 1 in minde make 2, which I take out of 3 over him, and the remainer is 1: that must be written between the two lines in the sixth place. So I go to the seventh place, where I finde onely cyphers, and in the grosse sum over them a cypher also: therefore must I write the remainer (which is nothing) with a cypher also. When in the eight and last place, I gather 1, 1, 2, that maketh 4, which if I take out of that 4 that is over them, there will nothing remain: and that must be noted with a cypher between the two lines, as I have often said, and so have I ended my work, and the figures stand as followeth.

But Sir, I remember you taught me that cyphers should not come in the last place, for because they serve onely to increase the value of other figures which follow them and serve not those figures that go before them: and now in my example I have set two cyphers in the two last places.

Master. I commend you for your remembrance. And truly it is, you should not have set them here, but onely because that I would make you plainly to perceive the Art of Subtraction. Wherefore seeing that you do now perceive

percebe it, whensoever you would write down a cypher, look whether any other figures be yet behinde; and if not, then let go the o also, for it needeth not to write them in the latter places, where no other figure doth follow, except it be (as I did now suffer you) to teach the use of Subtraction the plainer.

Therefore your figures must stand thus

40301964 Charge.

when the worke is ch-

done, shall be thus

20003428

Scholar. Sir, I do

10002432

thinke with that that

10101461

you taught me before,

and by these two sums

194643

that you taught me

ask also, that now

I could subtract any

summe

Master. So may you if you have marked

what I have taught you. But, because this

thing (as all other) must be learned surely by

often practise; I will propound here two ex-

amples to you; wherein if you often exercise

your selfe you shall be right and perfect to sub-

tract any other summe lightly; for in them is

contained all the observances of whole num-

bers. And because you shall percebe some-

what both how to doe it, and also whether it

be well done when you have proved to do it:

therefore have I written under them both, the

Remainers.

30606	Lent.	308964	Debr.
10354	} Paid.	103143	} Paid.
10249		102397	
163		10102	
20766	Paid in all.		02198
9840	Rest to pay.		

Scholar. Sir, I thank you: but I think I might the better do it, if you did shew me the working of it.

Master. Wen, but you must prove your self to do some things without my aid, or else you shall not be able to do any more then you are taught: And that were rather to learne by rote (as they call it) then by reason. And againe, there is nothing in these examples, or any other of whole numbers, but I have taught you the rules of them already. I teach

Scholar. When I trust, by practise, to attain the use of it. And is this all that I shall learne of Subtraction?

Master. Wen, saying that (as you have seen in Addition) there are numbers of others Denominations, in which the working is not much unlike: yet (without some instructions bee given of it) it might seem to a learner more difficult then indeed it is. Wherefore I will be lesse shew you the use of it onely, by an example or two.

A certain

A certain man owed to me 14 l, 12 s, 8 d.
 of which he paid me at one time 4 l, 6 s, 8 d.
 at another time 3 l, at another 2 l, 3 s, 4 d.
 and last of all 6 s, 8 d.

Now would I know what re: 14 — 12 — 8
 moneys unpaid yet, therefore
 I set my summes thus, every one 4 — 6 — 8
 in their due place: As pounds 3 — 0 — 0
 under pounds, shillings under 2 — 3 — 4
 shillings, pence under pence. 14 — 6 — 8

Scholar. Sir, I pray you why do you write
 14 for the common speech used rather to say,
 40 s.

Master. We must here use the Denomina-
 tion that is greatest in any summe, so that
 wee may not write according as wee use to
 speake, saying, 16 d, 18 d, or likewise 7
 groats, 8 groats, 24 s, 40 s, 48 s, and
 such other: but wee must write every De-
 nomination that is in any summe by it
 selfe.

Note how
 the Pen
 differeth
 from the
 common
 order of
 Counter.

shillings and pounds. So must
 we write for the like summe now named, 1 s,
 4 s, 6 s, 6 d, 2 d, 4 d, 2 s, 8 d; 1 l, 4 s,
 2 l, 8 s: and so forth of other like.

Scholar. So that we may not write in A-
 richmetick, pence, when the summe amount-
 eth to shillings, nor shillings, when the summe
 amounteth to pounds. Now, if it please you, end
 your example.

the 14 l, 12 s, 8 d. **Therefore** to performe the worke. I say, 8 d, out of 8 d, remaineth 0; resteth nothing, therefore in the place of the rest 0; remains, right under the denomination, I set down 0. When comming to the shillings, where I finde 16; which should be taken out of 12, but I cannot; therefore I imagine to borrow 1 of the next denomination, that is, of the 14 l, and put that one pound so borrowed unto 12 s, that maketh 32 s.

Now 16 s, out of 32 s, resteth 16 s, which 16 s, I set downe directly under the place of the rest.

Lastly, comming to the pounds, saying, one pound in minde that I borrowed, and 9 make 10, then 10 out of 14, there resteth 4.

So doth my whole rest 0; remains, appear to be 4 l, 16 s, 0 d.

This I account the easiest way for a young beginner to practise, though it be something long.

Is there any shorter way for this worke also?

Yes, as in this last example, I will also shew you, for you may adde together the particular numbers

in each sort of denomination, and then subtract the lesser from the greater

they

will be the same

they are set in order, begin
 with the pence, say 14 — 12 = 2
 ing 8, 14, 8; make 20 d, which
 which 20 d, you should
 take out of the 8 d, above
 the line, but you cannot,
 therefore shall you borrow
 1 of the next denomination
 on, that is to say, 1 of the
 shillings, and put it to the 8 d, that maketh
 20 d, now 20, out of 20 resteth 0, which cy-
 pher I set down directly under them.

Then one shilling that I borrowed, I had
 in minde, and 6 make 7, and 3 make 10, and 6
 make 16, the 16 out of 12 I cannot take, there-
 fore of the next denomination I do borrow
 one l, and put it to 12 s, which maketh 13 s,
 then 16 s, out of 13 s, resteth 1 s.

Lastly, I came to the pounds, saying, 1
 in minde, that I borrowed, and 4 make 5,
 and 3 is 6, and 4 is 10, then 10 out of 11, there
 resteth 1.

So doth my remainder, or rest appear as be-
 fore, to be 4 l, 16 s, 0 d.

Scholar. When doe I perceiue this well,
 and if there bee no other thing to be learned
 in Subtraction, then may I come to Multi-
 plication, for that you reckoned to bee next in
 order.

Master. We have done indeed with the Art
 of Subtraction, as touching the working.

But yet before we goe to Multiplication, I
 will

Subtraction.

87

tell in that you be to examine your work, whether it be well done or not. For the performance whereof, if you mark what I said in Addition, you may easily perceive what is to be done for the proof of Subtraction, which is best made by the aid of Addition, thus:

Proof of
Subtraction.

Write under the lowest number (which is your Remainder) a line, and then add this remainder and all the other that you did subtract before, together, and write that that amounteth under the lower line: and if the summe that cometh thereof, be equall to the highest of the Subtraction, then is the Subtraction well wrought, or else not: As you may see for example in the sums set down before, and first in sum of one denomination, whereof one was this, and so on.

8250003456
52984732 is subtracted
from 8250003456, and the
Remainder is 8197018724

Now to prove whether it be truly wrought or not, I add the remainder and the number subtracted together, beginning at the right hand, and first I say, 4 and 2 is 6: which is set under the line.

Example
in a sum of
one denomination.

The number given. 8250003456

The number to subtract. 52984732

The Remainder. 8197018724

The Proofs. 8250003456

Then again in the second place, I say, 2 and 3 is 5, which I write under, next that in the third

thre place, 7 and 7 are 14, of which I write the Digit 4, and keep the article 1 in my minde. Then in the fourth place 8 and 4 is 12 and 1 in my minde maketh 13, whereof I write down the digit 3, and keep the article 1 in my minde. Again, in the fifth place, 1 and 8 is 9, and 1 in my minde is 10. Whereof I set down 0 and keep the 1 in my minde. And so going on to the rest (as it is taught in Addition) when I have made an end, I see that the lowest line of numbers and the highest be alike: wherefore I know that I have well done.

So likewise the proof is to be made in numbers of divers denominations: thus for example, in our summe of that kind which in the first forme of working, stood thus: (all the particular numbers to be subtracted, being brought into one.)

Example
in a sum
of divers
denomi-
nations,

Where in the title li. s. d.
of pence, I finde 8 and 12
the 8 I set downe
directly under in that
of pence: Then in the place
of shillings I find 16
and 16 which make
32 shillings, wherein
is contained 1 l. and
12 s. the 12 s. I set
down directly under
them in the due place

Proof.

14	12	8
of		

of shillings, and one pound I keepe.

Then coming to the pounds I say, 1 that I keepe, and 4 is 5, and 9 is 14, which 14 in one order I set down directly under them, as this figure sheweth directly. And the whole summe is 14 11 12 9, 8 8, agreeing with the upper number above. So I finde the work is good, and the Subtraction well wrought.

The same thing is to be done for the latter sort of Subtraction (where the particular summes are not gathered together into one whole.) For the Remainder and all the particular summes subtracted, being added together, is the summe that cometh thereof be equall to the highest number above, then is the Subtraction well wrought, or else not.

As for example also in the last summes which stood thus.

First, in the title of pence, I adde 8, 4, 8, that maketh 20 d, which containeth one shilling and 8 pence.

The 8 I set down under the lowest line in the row of title of pence, and that one shilling I keepe to carry to the next Denomination of place of shillings.

$$\begin{array}{r} 14-12-8 \\ \hline 4-6-8 \\ 3-0-0 \\ 2-3-4 \\ 0-6-8 \end{array}$$

Example
of a proof
in the latter
forme
of Subtra-
ction.

$$\begin{array}{r} 4-16-0 \\ \hline 14-12-8 \end{array}$$

Then returning to the shillings, saying:
one

one in minde; so that 3 keepe, and 16 make
 19, and 6 make 25, and 3 make 28, and 6
 make 32 shillings, which amounteth to one
 pound 12 s. the 12 s. I set down under the
 title of shillings, and 1 pound I keepe: and have
 in mind to carry to the next Denomination
 of place of pounds. Then come I to the
 pounds, saying, 1 that I bring and 4 make
 5, and 2 make 7, and 3 is 10, and 4 make 14.
 then do I write 14 under the pounds, and so
 have I ended the Addition: and I see that the
 lowest line is like unto the uppermost line in
 number, wherefore I know that I have well
 done.

And thus have I taught you the Art of Sub-
 traction, and the means to prove whether it be
 well wrought or not. Therefore now will I
 make an end thereof, and will instruct you in
 Multiplication.

Example
 1000
 100
 10
 1
 1000
 100
 10
 1

1000
 100
 10
 1
 1000
 100
 10
 1

1000
 100
 10
 1
 1000
 100
 10
 1

1000
 100
 10
 1
 1000
 100
 10
 1

1000
 100
 10
 1
 1000
 100
 10
 1

Multiplication

Multiplication.



Multiplication is an operation whereby two sums produce the third: which third sum so many times shall contain the first, as there are Vnites in the second. And it serueth in stead of many Additions:

Multiplication
what it is.

As for example: When I would know how many are 30 times 48, if I should add 48 thirtie times, it would be a long work: Therefore was this work of Multiplication devised, which shall do that at once, that Addition should do at many times.

Scholar. I perceiue the commodity of it partly, but I shall not see the full profit of it, till I know the whole use of it. Therefore Sir, I beseech you, teach me the working of it.

Master. So I iudge it best, but because that great numbers cannot be multiplied, but by the multiplication of digits, therefore I thinke it best to shew you the way of multiplying them. And when I say, 9 times 8, or 8 times 9, &c. And as for the small digits under 5, it were but folly to teach any rule, seeing they are so easie, that every child can do it: but for the multiplication of the greater digits, that shall you do.

Multiplication of
Digits.

First, set your digits one right over the other

Digit
at 10 and 10

The dif-
ference.

other, then from the uppermost downwards,
and from the nethermost upwards, draw
straight lines so that they make a crosse, com-
monly called Saint Andrews crosse, as you see
here. When look how many each of them
lacketh of 10, and write that against each of
them at the end of the lines,
and that is called the diffe-
rence: as if I would know
how many are 7 times 8,
I must write those Digits
thus.

Digit difference

When doe I looke how
much 8 doth differ from 10,
and I finde it to be 2, that 2
doe I write at the right
hand of 8, at the end of the
line, thus.

8

2

Digit difference

7

2

Digit difference

8

2

After that I take a diffe-
rence of 7 likewise from
10, that is 3, and I write
that at the right side of 7,
as you see in this example,

7

3

Digit difference

8

2

Then doe I draw a line
under them, as in Addition,
thus.

7

3

Last of all, I multiply the two differences,
saying, 2 times 3 make 6, that must I ever
set under the differences, beneath the line;
then must I take one of the differences, which
I will, for all is like, from the other digit (not
from his owne) as the lines of the Crosse

warn

harmes me, and that that is left, must I write under the Digit difference. As in this example, if I take 2 from 7, there remaineth 5, that 5 must I write under the digit, and then there appeareth the multiplication of 7 times 8 to be 56. And so likewise of any other digits, if they be above 5, for if they be under 5, then will their difference be greater then themselves, so that they cannot be taken out of them. And againe, such little summes every childe can multiply, as to say, 2 times 3, or 4 times 5: and such likes, and so forth.

Scholar. Truth be it, and seeing now I knoweth that I understand the multiplying of the greater digits, I will prove by an example how I can do it. I would know how many are 9 times 6.

Master. It is all one in value to say 9 times 6, or 6 times 9: but yet the order is best to put the lesse summe first, saying, 6 times 9, and so of all other summes.

Scholar. When would I know how many are 6 times 9: therefore I set the digits thus, and make the crosse, thus.

Then do I set their differences from 10 at the right side, the difference of 9, which is 1, against 10, and the difference of 6 which is 4, against 10 also, as in this example.

And under them draw a line. Then do I multiply the differences together, saying, 4 times 1 maketh 4, that 4 doe I write under them thus:

Then take I one of the differences from the other, as 1 from 6, or 4 from 9, and each wayes there resteth 5, which I do write under the digit thus. And so appeareth the multiplication of 6 times 9 to be 54. Thus I see the feat of this manner of multiplication of digits.

Master. Now might you go straight to the multiplication of great numbers, save that both for your ease and surety in working, I will draw you here a Table, whereby shall appeare the multiplication of all the digits, and this is it that followeth.

1	1	2	3	4	5	6	7	8	9
2	2	4	6	8	10	12	14	16	18
3	3	9	12	15	18	21	24	27	
4	4	16	20	24	28	32	36		
5	5	25	30	35	40	45			
6	6	36	42	48	54				
7	7	49	56	63					
8	8	64	72						
9	9	81							

In which Table when you would know the product in any multiplication of Digits, seeke your first or last Digit in the greater figures, and from it go right forth towards the right hand, till you come under the number of your second Digit which is in the highest row, and then the number that is in the meeting of the rows of little squares (which come directly from both your propounded Digits) is the Multiplication that amounteth of them. As if I would know by this Table the multiplication of 7 times 9. seek first 7 in the greater figures, and then go right forth toward the right hand, till you come under 9 of the highest row, in which place where you so come under the other digit (as here say example, you come under 9) is alwayes contained the off-
come

some, or product which you seek, and that place we terme to bee in the common angle, in respect of the two numbers so taken on the out-sides; as here in that common angle, where the rows of little squares, directly proceeding from 7 and 9 do meet, you have 63, which 63 is the summe of the multiplication of 9 by 7.

To multi-
ply greater
summes.

Scholar. This is very good and ready. And so may I find the multiplication of any digits: but now how shall I do in greater summes?

Multiplie.

Master. When you would multiply any summe by another, you shall marke that it is the meetest order to set the greatest number highest, which is the place of the number that must be multiplied; and likewise the lesser number under it, for that is the place of the Multiplier, or Multiplicator, that is to say, the number by which the Multiplication is made, and is in English alwayes put before this word, Times: in such speaking when I say, 20 times 70. And the number that followeth this word Times, is that which must be multiplied.

Times.

Therefore when I would multiply one number by another, I must write the greatest highest, and the lesser under it as this direction. And under them must I draw a line. As for example. If I would multiply 264 by 29 I must set them thus.

Or thus. Thus let those to be multiplied, who are joined a question, as these. There are 29 men in each man hath

264 Lambes. The question is, how many Lambes they have in all.

To the performance whereof, I must multiply every figure of the higher row, by every figure of the nether row, and that that amounteth I must set under the line, as thus :


First, I doe multiply 4 by 9, saying, 9 times 4 (or 4 times 9, which is all one) and that maketh 36, as the Table before of digits doth declare; of that 36 I must write the 6, that is the digit under the 9, and the article 3 I keep in minde to carry to the next place.

Then come I to the second figure of the higher row, which is 6, and say: 9 times 6 make 54, and with the 3 in my minde make 57, the 7 I set down under the 2, and 5 I keep in minde.

After that I come to the next figure, which is 2, and multiply it by 9, and that maketh 18, and with 5 that I have in minde maketh 23: wherefore because it is the last worke of the Multiplier, I set down in order as you see:

And so I have ended the first figure of the Multiplier. Wherefore I give it now a name with my Pen.

Then begin I with the next figure, 264
and multiply it into all the higher fi- 29
gures, as thus,

 First, 2 times 4 make 8, that 8 do 2376
I write under the second place; for evermore
the digit or first figure of the multiplication
that amounteth of the figure of the higher num-
ber, must be set under the multiplier of it, the
other in their order toward the left hand.

Scholar, I understand you thus, that the
digit of the summe amounting of the multi-
plication of the first figure of the higher row,
by the first figure of the lower row, or multi-
plier, must be set under the first place, and that
that amounteth of the same first figure by the
second multiplier, must be set under the se-
cond place, and so of the other, if there be more
multipliers.

Master. So meane I indeed: and if there
amount but a digit, then must it be set under
the multiplier.

And now to go forth: I multiply by the
same 2, the second figure of the higher row,
which is 6, saying, 2 times 6,
make 12, whereof I write the 264
digit 2 under the third place, & 29
the article 1 I keep in mind.

Then do I multiply the last 2376
figure of the higher summe by 28
that same 2, saying, two times two is 4, and
with the 1 that I have in minde maketh 5,
which 5 I write under the fourth place. And
so

so have I ended the whole Multiplication:
wherefore I also give the 2 a dash
with my Pen thus: and so I do
ether as soon as I have dispatched
any digit by which I multiply:
and the summes stand thus:

When must I draw a line un-
der all those summes that mount
of the multiplication, and must
adde all them into one summe, as
in the example you may see.

Where in the first place I finde
but 6, and therefore write I it un-
der the line. When in the second
place, 8 and 7 make 15, whereof
I write 5, and keep one in my mind, and so
forth as you learned in Addition. And so ap-
peareth the whole summe to bee 7656, which
amounteth of the multiplication of 264, by 29,
and that is the just number of the Lambs that
29 men had.

Scholar. If there be no more to be obser-
ved in it, then can I do it, I suppose, as by this
example I shall prove.

There is a piece of ground which conti-
neth 1365 yards in length, and 236 yards in
breadth: I would know how ma-
ny yards square there is in all this
piece of ground: Which numbers
I set down with the greater a-
bove, and the lesser under, as you
see.

Then doe I multiply 3 by 6, saying, 6 times 3 make 30, of which I write the Cypher in the first place, and the Article 3 I doe keepe in minde to carry to the next place.

Then doe I by the same 6 multiply the second figure of the higher summe, which is 6, saying, 6 times 6 make 36, and 3 in my mind make 39, of which I write the 9 under the second place, and the article 3 I keepe in mind.

Then doe I multiply the third figure, which is 3, by the same 6, and that maketh 18, and 3 in my mind make 21: the 1 I set down, and keep 2 in mind.

Then come I to the last figure of the higher summe, and multiply it by 6, saying, 6 times 1 make 6, and 2 in my mind make 8, the 8 do I write under the fourth place: And so have I ended the first multiplier, and dash him slightly with my Pen.

Then begin I with the second multiplier, and say, first, 3 times 5 that maketh 15, of which I set the 5 under the second place, because that the multiplier is there, and the article 1 I keepe in minde.

Then

Then come I to the second figure that is 6, and multiply it by 3, which maketh 18, & with one in mind maketh 19, the 9 I set down under the third place, and 1 I keepe in mind.

Then come I to the third figure, which is 3, and multiply it by 3, saying, 3 times 3 make 9, and with one in mind make 10, the cypher I set under the fourth place, and the article 1 I keep in mind.

And then comming to the last figure 1, I multiply it by 3, and it maketh 3, and with the one in mind it maketh 4, which 4 I set in the first place, and then I have ended two of the multipliers, and the summes stand as you may see in the latter end of the page, going before, and then I give 3 his dash.

Then come I to the third multiplier, and multiply it into every figure of the higher sum, and first I say, 1 times 1 make 10, of which I set the cypher under the multiplier in the third place, and the article 1 I keepe in mind.

And so multiplying the seconde figure 6 by that

1365
236
8190
4095
6

1365
236
8190
4095
1365
236
8190
4095

that same 2, there amounteth 12, and 1 in my minde maketh 13, whereof I write the digit 3 under the fourth place, and the article 1 I keep in minde.

Then do I multiply the said 2 by the third figure of the higher summe, which is 3, and that maketh 6, and the one in minde make 7, which 7 I set down under the first place, as appeareth by the example.

Then come I to the last place, and multiply that 1 by 2, and there amounteth 2, which I set in the sixth place, and then doth the summe stand thus.

And so have I ended the whole multiplication.

But now (as you taught me) to know what this whole sum is, I must adde all those parcels together, and then under the line will appear, as you may see, the grosse or totall sum, which is 322140. Whereby I know there is so many yards square in that piece of ground.

Master. This is well done.

Scholar. When me thinketh I could call it well done, when I know, whether I have well done or no.

Master

Master. It is to be proved by 9, as Addition was, but the surest proof is by Division, and therefore I will reserve that proof by Division, till you have learned the Art of division: And anon I will shew you how it is commonly proved.

¶ But first, for your further instruction in this exercise of Multiplication, I will with an example more try your cunning, and so make an end: And the question is this, I would know how many daies it is since the Nativitie of our Lord and Saviour Iesus Christ, unto this year 1645. Which to performe, you must multiply this present year 1645, by the daies in the whole year, which are 365.

Scholar. Now for that you have given me so much light into the question, you shall see I will handsomely finish the work, & coming for according to your former instruction, I set them down with a line under them thus.

¶ When I say 5, 5 times 5 is 25, I set down the digit 5, and keep the article 2 in my mind to be added to the next place; then I say, 5 times 4 is 20, and 2 in mind is 22, I write the digit 2 in the second place, and keep the article 2, to be added to the third place: then I say, 5 times 6 is 30, and 2 in mind, is 32, I write the digit 2 in the third place and keep the article 3: then coming to the last figure, I say, 5 times 1 is 5, and 3 in mind is 8, which I set down in the fourth place: thus

3

I have ended my first multiplier, which I cancell.

Then I come to my second multiplier, which is 6, and multiply it into the upper number, saying 6 times 5 is 30, I write the 0 under the second place, and reserve the article 3 to be added to the next place; then I say, 6 times 4 is 24, and 3 in minde is 27, I write 7 in the third place, and reserve the article 2 for the next place; then I say, 6 times 6 is 36, and 2 in minde is 38, the digit 8 I set downe in the fourth place, and keepe 3 in minde: Againe, I say 6 times 1 is 6, and 3 kept is 9, which I set downe, and so have I finished two multipliers, wherefore I cancell 6 with my Pen.

Finally, I begin with the third and last multiplier, saying, 3 times 5 is 15, I write 5 in the third place, and reserve the article 1; then 3 times 4 is 12, and 1 kept, is 13, I write 3 and keepe 1 to be added to the next place; then 3 times 6 is 18, and 1 in minde, is 19, I write 9 and keep 1, the article; againe

1645
368

8225
9870
4935

600425 days

Multiplication.

83

I say, 3 times 11 direct 33
 3, and 1 in
 side to 4, which
 I set downe, and
 so have I fin-
 ished the Multipli-
 cation, and the fi-
 gures stand as a-
 bove, which added
 together, the totall
 is 600425 dayes.
 For your further
 practise, exercise, and
 incouragement, be-
 hold these operati-
 ons, which I have
 brought to prime
 minutes.

1645

309

334

8334

98700

4935

100425

1401700

1200850

14410100

60

100425

100425

100425

100425

100425

100425

100425

100425

100425

Master. I commend you for your diligence,
 the worke is very perfectly done, which par-
 cels if you now adde together into one summe
 it will be 600425, which is the grosse or totall
 summe of that multiplication, and declineth
 the number of dayes since our Lord and Savi-
 our his Incarnation, unto the end of 1645
 years, besides 407 dayes, and twelve houres
 of leape years.

Scholar. This is marvellous, mee thinke,
 that such great matters may so easily be at-
 chieved by this Art, which heretofore I ever
 thought had been impossible, as I thinke soth
 of people are of that minde.

Master,

Master. Truth it is, that knowledge hath no greater enemy then ignorance: so this is one of the least of ten thousand things that may be done by this Art, as hereafter you shall be able to justifie.

Scholar. The manner of Multiplication I perceiue, if there be no more in it.

Master. Yes, there are other formes and holts for ease, and shorter labour of the work of Multiplication, but I will remitt them till you haue a little tasted Division, where also the like helpe into Division may be used: and so therefore under one example for both, will I shew you both, as in Multiplication, and also in Division.

But sith the other formes and workings doe nothing differ from these works in effect, but onely in setting of the numbers, I will over-passe them till a more meet place and time. And now will I instruct you in Division, so that you thinke your selfe sufficiently to perceiue what I haue taught you.

Scholar. Yes Sir, I thanke you, but I doe not perceiue how to examine my worke, to trauel whether I haue well done, or no: therefore as you promised me ere-while, I pray you shew me how I shall probe it.

Master. That is commonly used by the people of 9, as you learned before in Addition, saying that it differeth from that forme in diuers respects. As for example, First, you must make a crosse after this manner.

Then

Prooffe of
Multipli-
cation.

Then must you examine your summe that
should be multiplied and look what remaineth
after casting away 9 ; that let you at the one
side of the crosse, then examine the multiplier;
and whatsoever remaineth in it after casting
away 9 so often as you can, write that at the
other side of the crosse: then must you multi-
ply those two numbers together, and looke
what amounteth thereof, if it be under 9 , write
at the higher part of the crosse: but if it be a-
bove 9 , then take thence 9 as often as you can,
and write the rest at the head of the crosse. As
for example; wee will prove the example you
past of the price of ground, that contained
 1365 yards in length; and 236 yards in
breadth.

Therefore first I cast away all the nines
from the summe to be multiplied, saying, 5
and 6 make 11 , cast away 9 , rest
 2 : then 3 and 2 make 5 , and 1
is 6 , that 6 I write at one side of
the crosse, thus.

Then doe I examine the Mul-
tiplicier, which is 236 , wherein
when the 9 is cast out, there re-
maineth 2 : that 2 therefore I set
at the other side of the crosse.

Then doe I multiply 6 by 2 , and it maketh
 12 , from which 12 I withdraw 9 , then resteth
 3 , which 3 doe I set at the head of the crosse.
Then doe I examine the grosse summe, amount-
ing of the multiplication: which is 322140 ,
where

where I finde 9 once, and 3 remaining: that
 I set at the foot of the crosse, and then I see
 if both agree with the other 3 at the top of the
 crosse, and so knowe I that I have done well: for if
 they two did differ, then there wold be some
 error in my worke in yaine, and the multiplication false.
 This is the common proof, but the most certaine proof is by di-
 vision, of which I will anon instruct you.

A sure
 prooffe of
 Multipli-
 cation,

Schollr. Sir, what is the chiefe use of Multi-
 plication.
 Master. The use of it is greater then you
 can yet understand: howbeit, these plaine com-
 modities it hath, that if you would resolve any
 great and whole value into many small and
 lesse portions, as if you would change pounds
 into shillings and pence, or any other greater
 or smaller parcels, by multiplication you shall
 doe it speedily and easily. Also if you should
 need to adde one summe to it selfe, or to any
 other often times, you shall doe it by multiplica-
 tion much more speedily, readily, easily, and
 surely, then by often and sundry Additions.
 Take you these commodities growne thence
 for an answer at this time, and hereafter I
 will more abundantly move you to perceive
 the use of it.

Division.

Division.

Scholar.



EN Sir, then in Division I pray you to instruct me. But me thinketh by the name of it, That it should bee all one with Multiplication: for I call that Division, when anything is parted into diuers and many parts.

Master. You take it as it is taken commonly: howbeit if you mark well, you shall perceiue that it is quite contrary to Multiplication, and doth not part one thing or few things into many, but contrarywise, it bringeth many parcels into few, but yet so, that these few taken together, are equall in value to the other many: for by diuision, pence are turned into shillings, and shillings into pounds: As for example, of 120 shillings, it maketh 6 pounds, so are 120 turned into 6, which is a smaller number; but then if you consider the Denominators, you shall see that they are such, that one of the latter is equall to 20 of the first, and so in value the summe are one, though in number they differ, and the latter summe is the lesser, and so it is alwayes in diuision, howbeit, yet in the working

Division
is it

A general
Rule for
placing the
figure.

working, the summe is parted by another, and thereof doth it take the name.

Scholar. I thinke I shall better understand the reason of the name when I know the use of the work, therefore now would I gladly learn that.

Division
what it is.

Master. Division is a distributing of a greater summe by the unitie of a lesser. Or, division is an Arithmetical producing of a third number in respect of two propounded numbers, which third number shall so often contain the unitie as the greater of the two propounded numbers contain the lesser. So that as Multiplication may seem to serue in stead of many Additions, so Division may seem to be in place of many Subtractions. Because that which number hath expressed how many times the lesser of your two propounded numbers may be subtracted from the greater: as by example will more largely appeare. Wherefore (as you may perceiue) into Division are required three numbers: The first which should be diuided, and that must generally be the greater: and the second, by which the other must be diuided, and that is (generally) the lesser, and is called the Diuision: And the third, which answereth to the question (How many times) and therefore is called the quotient.

A general
Rule for
placing the
figure.

The first must be first written, and the second set under it, that the last figure of the lower number be right under the last of

without

the

Division.

the higher, contrary to the manner of other
kinds of Arithmetick: for in them the
first figures were set over, under, or
other: but in division, the last figures must be
set next, except it chance so that the last figure
of the divisor be greater than the last of the
divident number, for then you shall set the last of
the Divisor under the last of the Divident
number, as for example.

An excep-
tion.

If you should divide 365 (which are the
summe of the days of a year) by
28, which are the days of a com-
mon Moneth, then should you
set them thus.

answering
divident

But if you should divide those
365 days by 52, which is the
number of weeks in one year,
then should you set them thus.

Likewise, if you should divide
the same 365 by 4, which is the
summe of the quarters of years,
then must I set them thus.
But, this doe I understand, but
now how should I do to divide the one by
the other?

Master. You must begin with the last fig-
ure next the left hand, and see how many
times the last figure of the Divisor may be
taken out of the last figure of the Divident
number, and that shall you note with a
crooked line toward your right hand, as
for example, I would divide 365 by 28,
then

Division.

then set I those two summes 365 (

And I look how many times

I may find 2 (which is the last figure of the divisor) in 3, (which is the last of the num-

ber to be divided) and considering that I can

take 2 out of 3 but once, I make a crooked

line at the right hand of the numbers, and

within it I set 1, and that is called the Quoti-

ent number, as I told you. Then because that

when 2 is taken out of 3 there

remaineth 1, I must write that 1

over 3, and deface or cancell the

3, and the 2, then will the figures

stand thus.

Then come I to the next figure of the di-

visor, and take it likewise so many times out

of the figures that be over it, and look what

doth remain, that I must write over them,

and cancell them, as in this example.

Wherefore now do I take once 8 out of 16,

and there remaineth 8, which I must set over

Quotient
number.

remaineth

remaineth before, and are written towards the left hand.

Master. So must you do: For you must so take the Divisor out of the over number, that there remaine not over it so great a somme as it selfe is, for then were your worke in vaine.

But yet againe here must you mark, that when you seeke how many times the last figure of the Divisor may be found in the number over him, that you looke also whether you may as often finde all the figures following in those that are above them (considering all the remainers, if there be any) If not, take the Quotient less by one, and then prove againe, and so still till you finde a meet Quotient: and by that meet Quotient must you alwayes multiply your Divisor, and let the product under your Divisor, so that the first figure stand under the first figure of your Divisor, and the second under the second, and so forth: And then subtract that product from the number to be divided that standeth directly over it, as you have seen me do.

Mark how
the divisor
is kindred
to the
quotient

When you have thus brought ours, then must you begin againe, and write your Divisor for anew, nearer toward the right hand by the place, as in this example, you shall see 285 (10 two under 8, and 8 under 5, thus.

Then (as before) seeke how many times you may

3

take

For more information on the number pack line
now.

Q. Now, what time of day is it, that you may find a
 longer time in 8, than there is in 9, and that you
 can find the figure following 8 many times
 in the other that is over him. Can you find 8

What you need to know about the new law

bet over him, that you look all together

[Faint, illegible text at the bottom of the page]

from the total of 254, in which sum

and the other one is a copy of the same.

per your District (and) contact all relevant

[illegible][illegible]

Let $\mathbf{z}_1, \mathbf{z}_2, \dots, \mathbf{z}_n$ be the columns of \mathbf{Z} . Then $\mathbf{Z}^T \mathbf{Z} = \mathbf{I}_n$ if and only if $\mathbf{z}_1, \mathbf{z}_2, \dots, \mathbf{z}_n$ are orthonormal. If \mathbf{Z} is an $n \times n$ matrix, then $\mathbf{Z}^T \mathbf{Z} = \mathbf{I}_n$ if and only if \mathbf{Z} is an orthogonal matrix. If \mathbf{Z} is an $n \times m$ matrix, then $\mathbf{Z}^T \mathbf{Z} = \mathbf{I}_m$ if and only if \mathbf{Z} is a semi-orthogonal matrix.

Then on 3 take 8 as many times out of 3 as

saying, 3 times I make 14, and if I take
out of 25, there remains 11, so then 3 cancell

25 and 8, and on the 5th and 8th, 1900

1. 1941 (1941) 1941

07101 3 4

Mark how
to consider
this kinde
of Remai-
ner.

92B3

£ 65

[illegible]

Master. Can you take the sum of your divi-
for (which is 4) out of one, which is the total
of the other number + 1, which is 5, and you will

Scholar, I had forgotten, because the last
of the divisor cannot be taken into the part
of the other number; but so many as it doth
contain, therefore mark it, subtract it from
the dividend, one place under the first, and
bring down the next digit, and so on till
you have brought down the whole dividend,
and then divide again.

And then must I looke how often I haue
 been the benefitee of the Sacrament (that is 4.)
 in 15, which I may doe 3 times, therefore I
 say, 3 times 4 is 12, which I take out of
 13, and there remaineth 1, when I see I make
 at the right hand of my summation twelve 12
 and 12 is twice off my 12, therefore 37 and 3
 must be 40, and 4, which be 44, and 44 is 88
 the 3 I let be 1, therefore 89, and 89 is 178
 maineth, and then the 8, which be 80, 3
 times 80, and then 240, and 240 is 480, and 480

When I multiply the same Quotient in
to every figure of the Divisor and multiply
the same that amounteth with all the num-
bers over them, as first I say, 3 times 2
make 6, which I take from 8, and there
remaineth 2, I scruell there, which is ad vanced
fore 10 and 5, and multiplieth 3 times 5
over the 6 that is that cometh 15, which
maineth, 10.

When doe I say likewise, 3 times 2 make 6, which I take out of 12 and there resteth 6, there.

therefore I cancell the 12 I shal remaⁿ in
and the 2 over, and then I write the 6 that remaⁿ
neth thus.

Then should I set for^{ward} the divisor into the :
next place toward the right hand, thus.

Master. But you may see that over the
is no figure, therefore I must set the divisor
yet forwarde by another place.

And marke, whensoever it chanceth so,
that you should set forwarde the divisor, and
that it cannot stand there, because there is no
number over the last place, or if there be and
it is lesser then the last figure of the divisor,
then must you remove the divisor yet once
gain: and because that his first place over-
nothing served to do nothing to much as
any, therefore you shall write in the quotient
a cypher, and if you should by chance need to do
some thing, for every time write a cypher in
the quotient. The reason of this followeth
the next example.

Scholar. Then you shall see
set my summe thus, and no number over
it, because I have moved
the divisor, so that I have com-
skipped one place, I must
write a cypher in the quo-
tient: and then must I
leske a new quotient, as

in this example I muste knowe howe often
 say: How many times one 4 is there in 6? (and yett saye that it
 can be but once)

therefore doe I write it in the quotient: and then saye 4 a time
 taken out of 6, remaineth 2.

I cancell the 4 out of the 6, and the 2
 over them, thus: $\begin{array}{r} 1 \\ 4 \overline{) 6} \\ \underline{4} \\ 2 \end{array}$

Then saye I how often one 2 is in 2? once
 out of 2, remaineth nothing.

I write the 1 in the quotient: and thus
 stand as follows: $\begin{array}{r} 11 \\ 4 \overline{) 6} \\ \underline{4} \\ 2 \\ \underline{2} \\ 0 \end{array}$

ling the 8 and the 2, thus: $\begin{array}{r} 11 \\ 4 \overline{) 6} \\ \underline{4} \\ 2 \\ \underline{2} \\ 0 \end{array}$

denote thus: $\begin{array}{r} 11 \\ 4 \overline{) 6} \\ \underline{4} \\ 2 \\ \underline{2} \\ 0 \end{array}$

in Master. How might we have said, once
 out of 8, and it remaineth 3: but this is
 not the way.

Scholar. Where once out of 8, remaineth 3
 what shall I write downe? The answer is
 Master. Borrow of the next number which

is behinde (for there is no more) and doe as you
 learned in Subtraction in a like case.

Scholar. Then must I borrow of the
 3 coming behinde next, and make that 13

then I saye one 4 is in 13
 three times, and I write
 the 3 in the quotient: and
 thus: $\begin{array}{r} 113 \\ 4 \overline{) 6} \\ \underline{4} \\ 2 \\ \underline{2} \\ 0 \end{array}$

Division
of
Forest
Service

I shall examine and try my work, whether
I have done well or no, that though no man
be by me to tell me, yet I may perceive it my
selfe.

Prooffe of
Division.

Master. Some men (yea and commonly
most) doe try it by the rule of 9, as in all the
other kindes, save that their order is; First
they cast away 9 as often as they can out of
the divisor, and that remaineth they set at
one side of a crosse, as in our first example
the divisor was 28, from which
you may take 9 three times, and
1 remaineth: which they set by
a Crosse, thus

When they likewise examine the Quotient,
(which in our example is 17) and from thence
they cast away 9 as often as they can, and
the remainder they set at the other side of
the Crosse, and then they multiply together
those two remainers, and so if that amount-
eth they adde the remainder of the Division,
if there were any, from that whole summe
they will take 9 as often as they can, and
the rest they set at the head of the Crosse
as in our example the quotient was 17, from
which take 9, and there remaineth
8, and therefore
must you set 8 at the head
of the Crosse, thus
When thou multiply 17 by 9, and it be 153, and
thereto adde the remainder of the Division
(which was 1) and it will be 154, which summe
doth

both not amount to 9, and therefore must be set wholly at the head of the Crosse, as you see here.

And this number on the head of the Crosse is the first proof, to which if you find another like in the number that was divided, then you have done well.

Therefore now shall you likewise examine the whole summe that was divided, and take away 9 as often as you can, and that that remaineth, set at the foot of the Crosse: and if it be equal to that in the head of the Crosse then have you done well, else not.

As in our example the whole summe was 365, which maketh 14 from that take 9, and there resteth 5, which set at the foot of the Crosse thus.

And you shall see that they agree: therefore have you well done.

Now will I likewise examine our second example, where the divisor was 457, which maketh 11, from thence I take 9, and the 2 that remaineth I set at the right side of the Crosse thus.

Then examine I the quotient, which was 301, where I finde but onely 4, that I set at the other side of the crosse thus.

When I multiply 4 by 2, and

21 and it maketh 5 to that 1 make the
maier of the division (which was 21) and
maketh 1 and they two make
20, wherein I find twice 9, and
I remaining 2 that I must
set at the head of the Cyph-
res.

Then I examine the whole
number to be divided, which
was 14028, where I find
twice 9 remaining 2, which
I set at the foot of the Cyph-
res.

And because it doth agree with the square of
the head of the Cyphres, I know that the divi-
on was well wrought.

The proof
of Divi-
on more
certain by
Multipli-
cation.

Matter. This is the common proof, how-
beit, the more certain working is by the con-
trary kinde: as to prove division by multipli-
cation, thus:

Multiply the quotient by the divisor, and
if the summe that amounteth, be equall to the
summe that should be divided, then have you
well divided: else not.

Now let this man you mark, that if there
remained any thing after the division,
that must you adde to the summe that
amounteth of the multiplication. As in our
first example our quotient was 15, and the
divisor was 28: Now multiply the one by the
other, and the sum will be 420, to that you
adde the 1 that remained after the division,
then

Scholar. By your patience I will prove that; and first set down the grosse summe and the multiplier, not after the rule of Multiplication, but after the rule of division, for now that number is become the Divisor, that was before the Multiplier. I should set them therefore thus

When shall I seek how many times 2 in 7, that may be thre times and one remaineth; but then may not 9 be found so often in 28; therefore must I take a lesser quotient, that is to say 2: then say I, twice 2 maketh 4, which I take out of 7, and there remaineth 3; then do I cancell 7 and 2, and over 7 I set 3, and in the quotient I set 2: so the figures stand thus.

Then say I further, 2 times 9 make 18, which I abate out of 39, and there resteth 18: then cancell I 3; and over him set 1, and likewise I cancell 6 and 9, and over them I set 8: so that thus stand the figures.

When I set forward the Divisor by one place, and seek a new quotient, that is to say, how many times 2 are in 18, which I finde to be 9 times: but then can I not finde 9 so many times in 5, therefore I take a lesser quotient, as to say 8: but yet that is too great: so if I take 8 times 2 out of 18 there remaineth



remaineth but 2, and I cannot finde 8 times 9
in 2: therefore yet I take a lesser quotient,
that is 7, which is alittle too great, for if I take
7 times 2 out of 18, there resteth 4, but now
I cannot take 7 times 9 out of 45, therefore
yet I seek a lesser quotient, as
to say 6, then say I, 6 times 2
make 12, that I take out of 18,
18, and there remaineth 6, so
I cancell 18, and the 2, and
write 6 over 8, thus
When I say I forth, 6 times 9
maketh 54, that take I out of
65, and there remaineth 11,
and the figures stand thus:
When now I set forth the
divisor again, and seek a new
quotient, which will be 4:
though I may finde 4 in 11, yet it is not
times, & 1 remain, yet I can-
not finde so often in 6, therefore
yet I set the figures thus:

And the 4 in the quotient
I multiply into the figures of the Divisor,
saying, four times 2 makes
8, which I take out of 11, and
there rests 3, therefore I can-
cell the 11, and the 2, & set 3
over the first place of 11, thus:

And then do I say forth
4 times 9 maketh 36, which
I take from 36, and there remaineth nothing,

And
the
first
place

so that the quotient of this Division will
(where 7656 is divided by 29) be 264:
which both declare, that if 264 be multipli-
ed by 29, the summe will be 7656. And thus
I perceive how both Multiplication is
proved by Division, and Division also by Mul-
tiplication.

Master. Now have I ended the five com-
mon kinds of Arithmetick: For (as touch-
ing Mediation, Duplation, Triplation, and
such other) they are no severall kinds of A-
rithmetick, but are contained under the o-
ther. For Mediation is contained under Di-
vision, and is nothing else but dividing by 2:
and so are Duplation and Triplation contain-
ed under Multiplication: for Duplation is no-
thing else but multiplying by 2, and Triplati-
on is multiplying by 3, of which I will onely
propose an example, for the rules you have
heard already.

An exam-
ple of Me-
diation.

If you would mediate, or divide into 2, the
summe 4531010, you shall set 2 for the divi-
sor, and work as you learned
before, as thus:

When I finde 2 in 4 five times, therefore
my quotient must be 2: So I cancell 4 and 2,
and remove the divisor toward them, as the
work requireth and
as before in Division
on hath beene decla-
red.

Which mediation or division by 2 hath
finished,

finished, you shall have 10; your quotient
225504, which is the half of 451008; and
you may trie by duplication; 10; double that
quotient, or multiply it by 2, and the same
number shall amount.

Duplication.

I will no longer tarry about these, seeing
they are but numbers of the other kindes. But
herewith (according to my promise) I will
teach you certaine easie wayes both of multi-
plication and of division. And first of multi-
plication.

If you would therefore multiply any summe
by 10, you shall need to do no more but add a
cypher before his first place; as for example,
36 multiplied by 10, make 360.

Easie
formes of
Multipli-
cation.

And likewise if you would multiply any summe
by 100, put two cyphers at his beginning. And
if you would multiply any summe by 1000,
add three cyphers to the beginning of it.
Scholar. Which do I will perceiue, and also
the reason of it.

Master. I will omit all reasons till our next
meeting, when I shall tell you the reason of all
other parts of Arithmetick also; and as to our
matter now, looke, as I have told you, that you
both remember it, and also often practise it.

And now you have learned how to multi-
ply easily by 10, 100, 1000; and of like manner
may you do with any other of like sort.

But now if you will multiply by 20, 30, 40,
and so forth, or by 100, 300, and such like,
where there is one cypher in the first place,

as many orderly in the first places, you shall take away those cyphers, and multiply the summe onely by the other figure, or figures, (if they bee many) and then at the beginning of the summe that amounteth, you shall set so many cyphers as you tooke away.

Example of 1873, which I would multiply by 300. First, I omit the 2 cyphers from the multiplier, and I multiply the summe by three onely that is left, and it amounteth to 8619: before which I put the two cyphers that I before omitted, or tooke away, and then is it 861900. And that is the summe that amounteth when 1873 is multiplied by 300.

Scholar. And if there were two or more figures beside the cyphers, I must onely take away the cyphers, and multiply by the other figures, as I learned before. As if I would multiply 93648 by 25000, I should take away the three cyphers, and multiply the same by 25, and then at the beginning of that totall summe should I add the 3 cyphers againe.

Master. Even so: but if it chance the number that should be multiplied, or both the summes, as well the number that should be multiplied, as the multiplier, to have cyphers in their first places, evermore omit the cyphers and work by the rest. But remember to restore as many cyphers to the amounting summe as you have before, as in this example: 30000 shall be multiplied by 206, I shall onely take away two cyphers from the mul-

seem number, and then multiply 302 by 206,
and afterward adde the two cyphers againe.
But if I should multiply the same 30000,
by 2060, I shall not onely take away the
two cyphers from the number that should
bee multiplied, but also I may take away the
one cypher from the multiplier, and then
must I adde three cyphers to the summe that
amounteth: but take heed that you take away
no cypher that cometh after any signifying
figure, as in the last example, you may not
take away that in the fourth place of the
higher number, neither that in the third place
of the multiplier: howbeit, yet thus you may
do: If one cypher or more come in the middle
of your sums, you may multiply by the other fi-
gures, and overshipe them: but so, that you give every figure his due
place: as thus, I will multiply 2999
3026 by 2004, therefore I set downe
them thus.

And thus I doe multiply them. First 4
times 6 make 24, I set the 4 under the 6th
place and keep the 2 still in my minde: then
say I againe 4 times 6 make 24, and the 2
that is in my minde maketh 10, I set downe
the cypher 0, and keepe the article 1 in my
minde: then 4 times 0 is 0, and the 1 in my
minde maketh 1, I set downe the figure 1;
and say againe 4 times 3 is 12, I set downe
2, and keeping the 1 still in my mind, having
no more places of the upper number to multi-
ply

I put it down next in the
 fifth place. But when I come to the next place
 (being a cypher) I let it go, because it mul-
 tiplieth nothing, & likewise the second cypher.
 But then when I come to the 2, and mul-
 tiplieth into the 5 of the other number, you
 must take heed (according as I taught you
 in multiplication) that the first number is
 the first of the multiplication. And so
 the 2 is set right under the 1 of the
 other, and the other orderly, as
 shall be left hand, according as
 you may see in this example, which
 being finished, with the
 addition thereof gathered together,
 will stand as this example sheweth.

Which is indeed wrought so
 much the sooner and shorter by
 other shipping of the two cy-
 phers: which otherwile (if the
 same example were wrought as
 length) it would have had
 workings more, as by the same
 example here also set down both
 appear. I thank you for the
 ease in this way of multiplication
 (and for the short division) you shall
 greatly further me in the
 place of the number of the

Matter. Now, I will teach you some easie
wayes in division also, and first this. If you
would divide any summe by 10, you shall one.
If with your Pen make a square line between
the first figure of your summe and the second,
and then have you done: for the whole number
that followeth the line, standeth for the quo-
tient, and the figure that is before the line, is
the Remainder. As for example,

3648 divided by 10. $\overline{364}8$
364 is the quotient, and beto-
keneth that so many times are 10, in 3648,
and the 8 after the line is the remainder, which
cannot be divided into 10, but by breaking it
into fractions, wherewith I will not meddle
yet.

And so likewise if you would divide any
summe by 100, with your pen you shall cut
away the two first figures, and if you would
divide by 1000, you must cut away the three
first figures, and so of any other divisor, whose
last figure is 1 and the other cyphers, look how
many cyphers the divisor hath, and so many
figures at the beginning shall you cut away
with the square line, and they stand alwaies
for the remainder, because they are lesse then the
divisor, and cannot be divided by it, and the o-
ther figures that are behind the line stand for
the quotient.

But now if your divisor have any other
figure in his last place than 1, and in all his
other places have cyphers, look how many
cyphers

amobad
nonib 30

cyphers they be, cut away so many of the first figures of the number that should be divided, and divide the rest that followeth the line by that figure that is in the last place, as if it were the whole divisor.

Example of 64:84, which I would divide by 300; here must I cut away the three first figures, (for so many cyphers my divisor hath) and must divide the rest by 3, which is the figure in the last place of the divisor. First therefore I part away the two first figures and the summe standeth thus: $64:84$

Then doe I divide 64 by 3, and the quotient is 21; for in 6 I finde twice 3, and once, and 1 remaining, which 1 with the 2 next before, doth make 12, wherein I finde 3 four times: And this is a ready way to turn shillings into pounds: for sith one pound doth contain 20 shillings, I must divide the whole number of shillings by 20. Therefore easily do it. I see that my divisor hath one cypher, and therefore I cut away one figure from the beginning of the whole summe of shillings, and then I doe mediate or divide by 2, the other figures or summe that followeth.

Scholar. I will put an example.

As you would divide 64:87 shillings, by 20: that is to say, if I would turn so many shillings into pounds, I must cut away the first figure, that is 7, and divide the rest, that is 64:8 by 2, so shall the quotient be 3:14

whereby

whereby I know that 6428 shillings make
3214 pounds, and 7 shillings remaining.

Master. Now probe by multiplication whe-
ther you have well done or no.

Scholar. The quotient is 3214. Now I
doe multiply by the divisor 2, and it doth ex-
mouut to 6428.

Master. Hereby you may perceive not on-
ly that you have well done, but also: how by
division you may turn shillings easily into
pounds: and contrarywise by multiplication
you may turne pounds into shillings.

But here shall you see amongst divers men
divers forms of such division: but if you
marke what I have told you you shall per-
ceive easily all the waies. For when they do
not cut away so many of the first figures of
the summe that they would divide as there
are cyphers in the first places of the divisors
but they set all their cyphers orderly under the
first places of the number that they would di-
vide: and then with the other figures they divide
(if there be many) they divide the rest of the
summe.

Another
manner
of the A-
bridge-
ment.

Example. If they would divide 121723
by 3409, they doe thus: they set their
summes thus:

And then do they divide orderly: till they
come to the cyphers: for there they stay and
end their work, as in this example.

They seeke how often 3 may be found in
7, which is two times, and 1 remaining:
there.

line, must be set to the 31 (that was cut away with the line) in higher places, as you see here: where that 17 with the 31, do make 1731.

Scholar. Sir, is there no other forme of division in practise but this?

Master. Yes verily, there are other formes in practise, but because I love brevity I will declare only one, which I first learned of, and is practised by that worthy Mathematician, my ancient and respectfull loving friend, Master Henry Bridges, wherein not any one figure is defaced or cancelled. As if I should divide 72 by 6, first place them thus $6 \overline{)72}$ if you please you may write the dividend, because though this is a loose paper that it may necessarily without cancelling or defacing of the work be applied to, and removed from the dividend as pleasure; then apply your divisor 6 to 7, the first figure of the dividend, and inquire how oft it may be had in 7, and seeing 6 is but once in 7, set 1 in the quotient line thus $6 \overline{)72}$ 1

Then multiply the divisor 6, by the quotient 1, and set the product 6 under 7 thus $6 \overline{)72}$ 1 6

Then draw a line under 6, and subtract 6 out of 7, thus $6 \overline{)72}$ 1 6

Then draw a line under 6, and subtract 6 out of 7, thus $6 \overline{)72}$ 1 6

Write the Divisor in a loose paper to remove at pleasure.

6 out of 7, setting the remainder 1 under 6, thus :

When bring down the next figure of the dividend, and set it with the Remainer 1 under the line, thus :

And bring the movable divisor 6 under the 2, and as before enquire how oft 6 is in 12, and finding it to bee twice in 12, set 2 in the quotient, thus :

And multiply 6 by that new quotient 2, setting the product 12 under the other 12, and subtracting it out of the upper number, there resteth nothing. And since the unittes of this product do stand under the unittes of the dividend, the division is ended : otherwise you should proceed as before, bringing downe the next figure; removing the divisor, dividing, multiplying, subtracting, &c.

Scholar. This is very easie, but if there be greater numbers propounded, is the operation the same : If the numbers bee lesser so great, the worke is the same without any difference, as shall appear by this example.

Divide

Divide 7890 by 33.

First let them thus, then bring the divisor under 78, and see how oft it is there found, which is twice, and therefore set 2 in the quotient, by which multiply the divisor 33, and set the product 66 under 78, and subtract it out of it thus.

Then bring the next figure 9 down, and set it with the Remainder 12, it maketh 129, and removing the divisor 33 thereto, enquire how often 33 is contained in 129, and I finde it but thrice, (though at the first it made a shew of more) therefore set 3 in the quotient, and multiplying 33 by 3, set the product under 129, subtracting that product out of the number above, and proceed as before.

Then shall you finde the divisor 9 times in the Remainder, therefore setting 9 in the quotient, multiply, and subtract as before, and at the last you shall finde only 3 remaining, which must be set above a line after the quotient, and the divisor under, as above appears.

Scholar. Is there no more difficulty in

the

the whole Rule: may y^e reader knowe
Master, not my, although your num-
ber bee never so great, as before I have
said.

And here will I make an end of Divi-
sion, (saying that I doe request you to exercise
your selfe well herein by many summes, till
you have attained some expertnesse therein.)

For the reasons and conclusions thereof be so
many, and so available for all sorts of men what-
soever; that if I should speak of the infinite uses
thereof, I should rather lack words then matter.
And therefore recommending it to your judge-
ment hereafter, upon your further travell in-
to the Art, I will here end this Treatise, re-
presenting unto you one example, or simple
question of Division and Multiplication, in
stead of many, which is this.

There are foure brasse Peeeces: The first of
them at a shot spendeth 3 pounds of powder,
the second spendeth 5 pounds, the third 4
pounds, and the fourth 2 pounds: If they are
all appointed against the battery of a Hold,
and there is allowed by the garrison Gunner
700 pounds of powder to be spent by these foure
Peeeces in this assault: The question is, what
The first shew many, that each Peece shall
justly make about with this 700 pounds of
powder? And lastly, how many pounds of
powder ought justly to be allowed to each
Peece for his true proportion of the whole?

A question
of shooting
in Ord-
nance.

Scholar. Why Sir, you make the stile, to
beare mee in hand, that these two demands
may bee simply resolved by Multiplication and
Division.

Master. Truly that they may, and that you
may by and by worke your selfe with a little
labour: first adde together their quantities of
powder, that is, 9 pounds, 5 pounds, 4 pounds
and 2 pounds, all which make 20: Divide the
700 pounds of powder by that 20, and your
quotient giveth 35, as here
appeareth, which sheweth
for more certainty that they
shall make just 35 shotes
about.

Scholar. Sir, all this have
I done, and I see it is so, but whether it bee
true or not, I cannot tell.

Master. To try the truth of the same, mul-
tiply the first peece that spends 9 pounds by 35,
and you shall see his allowance, which is 315
pounds of powder. Multiply also the second
peece that spends 5 pounds by 35, and you shall
find 175 pounds his allowance: then 4 by 35,
and you shall finde 140 pounds his allowance.
Lastly, multiply 2 by 35 and you shall find 70
pounds his allowance. All which
four particular summes you shall
adde together by Addition, as here
appeareth, and it maketh just 700
pounds, and so is the question tri-
ly absolved.

Scholar.

Scholar. Truly Sir, these excellent conclusions do wonderfully more and more make me in love with the Art.

Master. It is an Art, that the further you travell, the more you thirst to go on to ward. Such a fountain, that the more you draw, the more it springs: and to speak absolutely in a word, (excepting the study of Divinity, which is the salvation of our soules) there is no study in the world comparable to this, for delight in wonderful and godly exercises; for the skill hereof is well knowne immediately to have flowed from the wisdom of God, into the heart of man, whom he hath created the chiefe image and instrument of his grace and glory.

Scholar. The desire of knowledge doth greatly incourage me to be studious herein: and therefore I pray you cease not to instruct me further in the use hereof.

Master. Verily a good will. And now therefore, for the further use of these two latter, that is, Multiplication and Division, I will briefly shew you the seat of Reduction:

Reduction

Reduction.

Reduction
what it is.

Reduction is, by which all summes of grosse denomination may be turned into summes of more subtile denomination. And contrariwise, all summes of subtile denomination may be brought to summes of grosser denomination.

Grosse denomination.

Scholar. What call you grosse denomination, and subtile denomination?

Subtile denomination.

Master. What I call a grosse denomination, which both containeth in it many other subtile: as a pound, (in respect to shillings) is a grosse denomination: for it is greater then shillings, and containeth many of them. And shillings (in comparison to pounds) are a subtile denomination, for because they are lesser then pounds, and many of them are contained in one of the other: and so likewise of other things: whatsoever thing is compared to other, if it be greater and containeth many of them, it is a grosse denomination, but if it be lesser (so that many of them are in the other) then are they called the subtile denominations: whereby you may perceiue that one denomination may be called a grosse denomination, and also a subtile (that is to say, a great and small) in diuers comparisons. For shillings compared to pounds, are a subtile or small denomination: but compared to pence, they

they are a grosse, or great denomination.

Scholar. Now I understand the matter, I pray you teach me the use.

Master. The use is easily learned, if you remember what you have learned before.

If you will reduce any Summe of a grosse denomination into a Summe of a smaller or sub-

tiller denomination, you must consider how many of that subtiller denomination doe make

one of the grosse denomination; and by that number of Numerator do you multiply the Sum.

As if you would reduce 30 pounds into shillings, you must consider that in a pound are contained 20 shillings, therefore multiply the one

30 by the other 20, and there will amount 600, whereby you may know that in 30 pounds are contained 600 shillings.

And thus if you would reduce 30 shillings into pence, considering that in a shilling are 12 pence, you must multiply 30 by 12, and it will be 360, whereby

you may find that in 30 shillings are contained 360 pence. And thus may you reduce any

grosse denomination into a more subtiller, by multiplication, if you know how many of the

lesser doe make the greater: of which thing I will now give you a briefe Table for the most

attentively Kindes of Money, Weights, Measures, and Time, and such like: whereby you

may know how often each subtiller denomination is contained in the grosse, when you shall

need it for the foresaid kinde of Reduction: And also the same that serve you, if you would

reduce

30

To reduce
grosse de-
nominari-
on to sub-
tile.

reduce any summe of a subtiler denomination into a summe of a greater denomination. For in such Reduction you must consider (as in the other forme) how many of the smaller do make the greater: and by that number you must divide the other summe and the quotient will declare how many of the greater denomination are comprehended in that summe: as for example. If you would know how many shillings are contained in 3240 d. consider that 12 pence doe make 1 s. you must divide that 3240 by 12 and your quotient will be 270 whereby you know that so many shillings are in 3240 d. But if you would know further how many pounds are in these 270 shillings seeing that every pound containeth 20 shillings divide that 270 by 20 and it will be 13 and 10 remaining whereby you may know that in 3240 d. (or 270 shillings) are 13 pounds and 10 shillings. For evermore the remainder must be named by the name of denomination of that summe that was divided, which in this place were shillings. And thus may you doe with any other kindes of Denominations.

¶ Therefore, to the intent you may have certaine light or knowledge in most common coynes, weights and measures, (which is the chiefe and principall thing in traffick to be known) I have in each Reduction, as they come in order, set downe certaine instructions incident thereunto. And first I have hereunto

added

Reduction.

1113

added this Table, wherein is comprehended, not onely our currant and common coynes, but also the most part of the usuall coynes of Christendome, with their just weights and value currant in this Realme of England, intending at the latter end of my Addition to this Booke, to write of the ordinary Money used in divers places, and their common values currant for traffick, with the manner of their exchanges from place to place, &c.

0	12	1	8	Great Tunc.
0	25	2	7	Double Tunc. K.H.
0	10	3	6	Double Tunc. of E.
3	8	4	5	Rozell.
8	14	5	4	Half Rozell.
4	7	6	3	Old Noble.
0	11	7	2	Half Noble.
0	2	8	1	Angell.
11	0	9	0	Half Angell.
11	0	10	0	Solinge.
7	4	11	0	2 parts of Solinge.
20	0	12	0	George Noble.
11	4	13	0	Half George Noble.
11	0	14	0	Five Crowns K.H.
0	2	15	0	Half Crown K.H.
8	11	16	0	Sovereign K.H. half.
0	11	17	0	Sovereign K.H.
0	11	18	0	Edward Tunc.
0	11	19	0	Richard Tunc.
0	11	20	0	Elizabeth Crowne.
0	11	21	0	Half Crown.
0	11	22	0	Nile.

Double

A Table of the names, and now valuation of
the most usual Gold-coins throughout Great
Brittaine, with their severall weight of
Pence and Grains; and what they
are worth of current English money this
present year, 1671.

The names & titles of the Gold.	The weight in Pence & Grains.		The value in Shill. & pence.	
Great Sovereign.	10	0	33	0
Double Sever. K.H.	8	1	12	0
Double Sov. of S.E.	7	7	12	0
Royall.	4	23	16	6
Half Royall.	2	1 d.	8	3
Old Noble.	4	6	14	8
Half Noble.	2	3	7	4
Angell.	3	8	11	0
Half Angell.	1	16	5	6
Salute.	2	5	6	11 ob.
2 parts of Salute.	1	11	4	7
George Noble.	3	0	9	9 ob.
Halfe George Noble.	1	12	4	11 q.
First Crown K.H.	2	9	6	11 ob.
Base Crown K.H.	2	0	5	6
Sover. K.H. best.	3	14	11	8 obq.
Sovereign K.H.	4	0	11	0
Edward Sever.	3	15 d.	11	0
Elizabeth Sever.	3	15 d.	11	0
Elizabeth Crown.	1	9	5	6
Half Crown.	0	19 d.	2	9
Vnite.	0	12	22	0

Double

Double Crown.	3	6	11	6
British Crown.	3	1	1	6
Frisch Crown.	1	7	4	4 obq.
Half Crown.	0	19 d.	2	9
Crosse Dagger.	3	6 d.	1	0
Half Crosse Dagger.	1	15	3	6
Rose Royall.	0	21	3	0
Spur Royall.	4	10 d.	10	0
The Angell.	1	23 d.	11	0
Half Angell.	1	11 d.	5	6

All the severall pieces of Gold heretofore mentioned, are set down according to their valuation by the Kings Majesty's proclamation for Gold, dated the 23 of November, 1611.

A Table of forain Gold-coyne, according to their ancient valuation and severall weights, in Pence and Graines.

The names & titles of the Gold.	The weight in Pence Grains		The value in Shill. Pence.	
Unicorn of Scot.	2	10	6	0
Scottish Crown.	2	5	6	0
French Noble.	4	16	13	4
All sorts of French Crowns.	2	5	6	0
Flanders Riders.	2	6	6	6
Gelders Riders.	2	2	3	6
Philips Royall.	2	10	10	0
Philips Crown.	2	5	5	0
Golden Gilden.	2	2	4	8
New And. Gild.	2	2	5	0

The names & titles of the Gold.	The weight in Pence, Grains	The value in Shill. Pence
Flanders Noble.	14 0 10	10 0 0
Half Flan. Noble.	7 2 6	5 0 0
Flan. Angell best.	3 1 6	2 10 0
Flan. Royall best.	3 0 10	1 10 0
Cavokus Gilden.	10 1 12	10 0 0
Flanders Royall.	2 1 6	5 0 0
Saxon Gilden.	3 2 2	4 0 0
Flanders Crowne.	2 5	6 0
Philip Gilden.	2 3	10 0 0
Half Pbn. Gild.	1 1	5 0 0
Golden Lion.	2 16	7 0 0
3 parts of golden Lion	10 10 0	10 0 0
2 parts of golden Lion	10 10 0	10 0 0
Dauids Gilden.	2 1 12	4 0
Horne Gilden.	3 12	4 11
Old undre Gilden.	10 10 0	10 0 0
Cruza long Crosse.	2 6	6 0 0
Cruza short Crosse.	2 6	6 0 0
Milreyes.	4 0	10 0 0
Half Milreyes.	2 10	5 0 0
Portague. 1 ounce.	2 16	68 0 0
Golden Castile.	2 23	10 0 0
Ducket of Aragon.	2 6	6 0 0
Hungary Ducket.	2 7	6 0 0
Double Pistole.	4 9	10 0 0
Single Pistole.	2 4 10	5 0 0
Ducket of Floren.	2 5	6 0 0
Double Ducket.	4 11	13 0 0
Single Ducket.	2 6	6 0 0
Double duc. of Rome	4 13	12 8



It is to bee understood (gentle Reader) that whereas in these Tables the weight is called by the name of a penny, it is not meant a penny of silver money, but a penny of Goldsmiths weight, which containeth 24 Barley-cornes. Concerning which see Troy weight in folio 193. or in the margin.

So if a man have not the weight wherewith to weigh any peece of gold, he may do it with barley-cornes, being dry, and as it is said in folio 193.

The prices of Gold which the bringers in of forain Gold shall receive at the Mint,

according to the Kings Majesties Pro-

clamations. Dated the 14. of March 1562.

For an ounce of French crowns, being 22 Karacts fine, 3 li, 6 s.

For every ounce of Spanish Pistols, being 21 Karacts, 3 graines and a halfe fine, 3 li, 6 s.

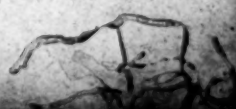
For Duckets of Spain, being 23 Karacts, 1 graine fine at least the ounce, 3 li, 6 s. 2 d.

For Milre's Crusado long crosse, Crusado short crosse, the ounce, 3 li, 6 s. 2 d.

For Hungary Duckets being 23 Karacts, 1 graine fine at least the ounce, 3 li, 6 s. 2 d.

For the Checkers of Venice, being 23 Karacts, 1 graine fine at least the ounce, 3 li, 6 s. 2 d.

For



For Barbary Gold, being 23 Karatts and 11 graine fine, at the least the ounce. — 3 li. 9 s. 4 d.

¶ And if the said Barbary Gold be of less fineness, abatement to be made according to the rate of the said 23 Karatts and 11 graine fine.

For Sultaince being 23 Karatts, 1 graine fine at least the ounce. — 3 li. 8 s. 8 d.

For all other Gold, being 22 Karatts fine the ounce. — 3 li. 6 s. 4 d.

¶ And being sold at a greater price according to that rate, and being sold for a less, so that the bringer in supply the less fine, with the more fine, in such sort, that in the totall it makes good at the same rate of 22 Karatts fine.

The price of Silver, which the bringers in of foraine Silver shall receive at the Mint, according to the

Kings Majesties aforesaid

Proclamation.

For the ounce of Spanish silver ever money of Civill. — 5 s. 4 d.

For the ounce of Mexico money. — 4 l. 10 d.

For

For Ingots of Silver, being an
 ounces, 7 4 weight fine, ac-
 cording to the Standard of
 England, the ounce.

And for other Silver of more fineness, a bet-
 ter price according to that rate, and for counter-
 less, so that the bringer in supply the like fine
 with the more fine, in such sort, therein the co-
 st is made good the said rate of 11 ounces,
 3 pence weight for according to the Standard
 of England.

Of Silver Coynes current in this

R E A L M E,
 The Silver pence of 12, of silver to pound
 The Silver half crown of 1. 2. 6.
 The Silver shillings, halfe shilling, and the
 three pence.
 Philip and Maries shilling, and halfe shilling.
 The Mary cross, and Mary two pence.
 Queen Elizabeths shilling, and 6 d. 4 p. 2 d.
 2 d. 4 p. three farthings, and halfe penny.

Here would I have expressed the values
 of the other Coynes of silver, but they are
 not current in this Realme, and therefore
 I have not put them in, but I have put in
 the rate

11 ounces,
 3 pence

Standes
 Coynes.

rate. And againe, they are so different in so many places, that it were matter enough to, a great booke to speake sufficiently of them all. Howbeit, because you shall not be altogether ignorant of them, I will shew you the values of some that are most in use, and first of France.

French
Coynes.

The most common coyns are Deniers, Soules, and Frankes: 12 deniers make 1 shilling, 20 soules make 1 Frank. So that as you see these 3 kindes are like in the rate to pence, shillings, and pounds with us; but that this is the difference, that their denier is but the ninth part of our penny, and so their Soule (commonly called Soules) goes 9 to our shilling, and 9 of their frankes to an English pound of money. So that three of their frankes make a noble. And by those three you may easily bring any French money into English money, according as I have set forth here following.

2160 Deniers make 180 shillings. And so of other in like sort. And for the use of these Coynes, I will shew you the manner, that you have some understanding in, by which numbers, you may know the value of the Coynes of Flanders, they be so called, because they were first used there from whence they came into our country, that

Flanders
Coynes.

that

that you have an example of their money to
 write you withall, you shall take those that
 be most common, as Sivers both single and
 double, Groats Flemish, Carolus and Gylden
 A Flemish Groat is a little above 2 farthings
 English. A single siver is 1 d. 6 s. 6 half far
 thing. The double siver Carolus is 1 d. 6 s.
 half farthing. Then there is also the Carolus
 Gylden which is worth 10 sivers. And the
 Flemish Noble is worth 3 Carolus Gyldens
 and 3 sivers. So that if you would convert Flemish mo
 ney and other kind of money whatsoever
 it be into sterling, you must reduce it
 first into the smallest part of English money
 that is in that Coyn. As for example, if I
 would reduce 268 double sivers into English
 money (considering that a double siver con
 taineth 2 d. farthing) you must first look how
 many farthings be in the double siver and you
 shall find them 12, therefore multiply the
 summe of the sivers by 12, and then have you
 their value in farthings, which is 4784. Now
 if you divide that by 4 then there will appeare
 the number of pence, but better it were to di
 vide it by 8 for so many farthings are in one
 shilling, and then will the quotient declare
 the summe of the shillings. And if you would reduce any summe
 of single sivers into English money, you must
 multiply the summe first by 12, and then have
 you reduced them into a certaine summe, that
 is

Not well

D
Money2
shillings

is to wit, half-farthings, which make 10 pence
800 by 8, shall tell amount the sum of pence
or if you divide it by 96, the sum of shillings
shall appear.

But mark this in all Division: when you
do reduce to bring one Denomination into a-
nother, if there be any Remainder after the
Division, that must be named by the denomi-
nation of the gross summe that was divi-
ded. As for example, I would bring 254 Far-
things into pence, therefore I divide that
254 by 4 (for so many farthings make a
penny) and the Quotient is 63, which is the
summe of the pence, and then remaineth yet
2, which are farthings still, as one may prove
by dividing. And this must be marked in all
Division, namely, when it is come to Redu-
ction.

Note wel.

Danks
Money.

¶ Touching Danks Money, they have
their Soulx, whereof 20 is a Liver: which is
2 shillings sterling. They have also their Grass
whereof 80 make a Gilden, which is 4 shil-
lings sterling. They have also Dollors, and
their common or old Dollor is 35 Grass. These
Dollors they have, which be others, some va-
lued at 24 Grass, some at 26, and some at 30.
And thus much I thought good to add to the
Author, touching Danks Money.

Spanish
Money.

Concerning Spanish Money; whereof the
most common are Cornadoes, Marveides,
Marveide, & Marveides make a Ryall, and
11 Ryall

as shall you see Duckets for the Ducker worth
 374 Marvedels, which is 374 shillings 10 pence sterling.
 The cost of 1000
 Duckets is 124 pounds 5 shillings sterling
 into Duckets, consider that pence is the
 least value or denomination named in this
 question: therefore divide 374 pounds 5 shil-
 lings into pence, and it maketh 29820 pence:
 which if you divide by pence that a Ducker is
 worth (which is 70) you shall have 426
 Quaters 416 Duckets; you have found your
 Quaters.

In Venice they have Bettes & Souldyes } Venice
 Licenses } Bettes make an English penny, 60 } money.
 Bettes a shilling, which is 2 Souldyes, and 20
 Souldyes a Lira of Venice which is a pound
 sterling.

Thus much have I said of Money: Now Weights
 will I shew you in like sort the distinction of
 weights.

After a Statute made anno 11 H. 7. there
 ought to be but one sort of weight: as 24 Barley weight, law
 corns dry, and taken out of the middlest of the A penny
 Ear, do make a penny weight, 20 of those penny weights
 make an ounce, and 12 ounces a pound of An ounce.
 Troy weight, by which is weighed Bead, Gold, A pound
 Silver, Pearl, Silke, and such like. But commonly there is used another weight called Haberdupoise
 Haberdupoise; in which 16 ounces make a poise
 pound: therefore when you would reduce weight
 ounces into pounds, you must consider toge-
 ther your weight be Troy weight or Haber-
 dupoise: and if it be Troy weight, you must
 divide

A very 35 Cloves, weight is a pound, that
is a pound and 10 pound, and much more
the way of Suffolk Cheese, and the like is
as should be the Barrell of Suffolk butter.

Barrell
Suffolk

The Way of Essex Cheese containeth six
score and sixteen pound and is much to alter
the Barrell of Essex butter.

Sope
meat

Moreover this weight is used by the Apotheca-
ries in their Physick composition, and mixture of
medicine, whereof the least is a graine.

10 Graines	}	A Drachm	}	3
3 Scruples		or Dragma		3
And		A ounce		3
8 Dragmes		A pound		3
16 Ounces				

The Apo-
thecaries
weights.

Now of weights are made other measure
both for grain and liquor: for a pound in Troy
weight, maketh a pint in measure, so that 8
pound or 8 pints do make a gallon: halfe a
gallon is named a pottle, and halfe a pottle is
called a quart, which containeth two pints.

Measures
for liquor
2 pints
A pint
Gallon
pottle
Quart.

Now above a Gallon the next measure is a
Firkin: then the Tertian, a Kilderkin, or halfe
Barrell, and a Barrell. And by these measures are
sold commonly Ale, Beer, Wine, and Oyle, but-
ter and Sope, Sugar, and other things.

Firkin.
Tertian.
Kilderkin.
Barrell.

There is also another measure for the mea-
sure of wine, which is named a Tun, and is
of threescore and six hogsheads.
The Firkin is the sixth part of a Tun.
The Barrell is the twelfth part of a Tun.

Wine
measures
Tun
Hogshead

The Barrell

Ale
measures
Tun
Hogshead

Beer measures.

**Some mea-
sures.**

Herrings.

Salmon & Halsey

**Wine mea-
sures.**

as being the Barrill of Suffolk barter.

- Soper's Mill, 500 Birch, Kilderkay, and
Birch Mount & Birch Mount measures 5100

Moreover the Stamer took time the weight of every of those three vessels being empty.

For Daniel has said that the

Half a Barrell weight 13 pounds
A Ferkin weight 11 pounds

Herrings also sold by the same measure that

Herrings are sold by the sale, 100 for the hundred, for shewen to the fish.

2 Salmon and Helen have a greater mean

Salmon - the Barrell - holds a 22 - Gal - 5 - gallon

Federal Reserve Bank of Chicago

Barrel and a Barrel. And by these means we

Now 26 for minor vessels they are as follows:

smaller than Hogheads, but it weighs 200
 lbs.: Every Hoghead is fine, but it is

there are many other wine vessels, but of them all for this Table, and make the most

30

Busshell.
A quarter.
A Wey.

A busshell
A quart
A Wey

Seven Pecks.
Eight Busshells.
Two quarters.

Strike.
Cornock.

These are the common names and measures, but in divers places there be divers sorts. The Busshell in many places is two Busshell, but then is that Busshell there called a Strike: and in some places butts a quarter is called a Cornocke. But those diversities are too many to tell you of, they are all: and again, they are against the law and statutes, I count them unmeet to be used.

Measure
to mete
length,
breadth, and
thickness.

But now remaineth yet another kind of measure, whereby men mete length, breadth, and thickness, and these are, an Inch, a Foot, and such other: whose names and quantities this Table sheweth.

An Inch.
Foot.

12 Inches of Breadth make a Foot, 12 Feet make a Yard.

Yard.
Ell.

3 Feet make a Yard, 4 Yards make an Ell.

Pearch.

1 Pearch in breadth, and 40 in length, is made a Pearch of ground, which is called a Pearch, and is a fourth part of an Acre.

Acre.

4 Pearches make an Acre of ground. 40 Pearches make a Furlong. 8 Furlongs make a Mile. The Statute, is in length 1760 pards, 5280 foot

Somewhat greater then the Italian mile of

It cannot be well done without the knowledg of Fractions, which as yet you have not learned, I will let them passe till another time, that I have taught you the knowledg of broken numbers.

Scholar. But yet sir of the parts of time
I pray you tell me somewhat. The parts of time.

Master. You know that a naturall day hath 24 houres, and every houre hath 60 minutes. A day,
It needeth not to tell you, that 7 dayes make An houre.
a week, and 4 weeks make a common month, Week,
and 12 months make a year, lacking one day, Moneth
and certain houres and minutes: but of that Yeare.
I shall instruct you hereafter.

Here will I make an end of Reduction for this time, which though it be counted no kind several of Arithmetick, you see it is no lesse needfull to be knowne; or easier to be done, then any of the other.

Scholar. Sparry sir it seemeth unto me much harder then any other sort, for it requirerh the knowledg of so many things: but now sir when you see time, I am ready to learn to you as much of Reduction as you have taught me, I remember; but and if I doe at any time forget, I shall have re-

couple to the Tables. **And you sit down**

[illegible]

that I have taught you the knowledge of pro-

1900

[Faint, illegible text at the bottom of the page]

[illegible]

...and the ...

1945

44 hours, and every hour that I miss.

It wouldn't tell you that 7 days later

3 weeks, and 4 weeks make a season month.

and 12 months makes a year. Jack had one day.

and certain routes and minutes : but of that

...not to be ...

1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 13. 14. 15. 16. 17. 18. 19. 20. 21. 22. 23. 24. 25. 26. 27. 28. 29. 30. 31. 32. 33. 34. 35. 36. 37. 38. 39. 40. 41. 42. 43. 44. 45. 46. 47. 48. 49. 50. 51. 52. 53. 54. 55. 56. 57. 58. 59. 60. 61. 62. 63. 64. 65. 66. 67. 68. 69. 70. 71. 72. 73. 74. 75. 76. 77. 78. 79. 80. 81. 82. 83. 84. 85. 86. 87. 88. 89. 90. 91. 92. 93. 94. 95. 96. 97. 98. 99. 100. 101. 102. 103. 104. 105. 106. 107. 108. 109. 110. 111. 112. 113. 114. 115. 116. 117. 118. 119. 120. 121. 122. 123. 124. 125. 126. 127. 128. 129. 130. 131. 132. 133. 134. 135. 136. 137. 138. 139. 140. 141. 142. 143. 144. 145. 146. 147. 148. 149. 150. 151. 152. 153. 154. 155. 156. 157. 158. 159. 160. 161. 162. 163. 164. 165. 166. 167. 168. 169. 170. 171. 172. 173. 174. 175. 176. 177. 178. 179. 180. 181. 182. 183. 184. 185. 186. 187. 188. 189. 190. 191. 192. 193. 194. 195. 196. 197. 198. 199. 200. 201. 202. 203. 204. 205. 206. 207. 208. 209. 210. 211. 212. 213. 214. 215. 216. 217. 218. 219. 220. 221. 222. 223. 224. 225. 226. 227. 228. 229. 230. 231. 232. 233. 234. 235. 236. 237. 238. 239. 240. 241. 242. 243. 244. 245. 246. 247. 248. 249. 250. 251. 252. 253. 254. 255. 256. 257. 258. 259. 260. 261. 262. 263. 264. 265. 266. 267. 268. 269. 270. 271. 272. 273. 274. 275. 276. 277. 278. 279. 280. 281. 282. 283. 284. 285. 286. 287. 288. 289. 290. 291. 292. 293. 294. 295. 296. 297. 298. 299. 300. 301. 302. 303. 304. 305. 306. 307. 308. 309. 310. 311. 312. 313. 314. 315. 316. 317. 318. 319. 320. 321. 322. 323. 324. 325. 326. 327. 328. 329. 330. 331. 332. 333. 334. 335. 336. 337. 338. 339. 340. 341. 342. 343. 344. 345. 346. 347. 348. 349. 350. 351. 352. 353. 354. 355. 356. 357. 358. 359. 360. 361. 362. 363. 364. 365. 366. 367. 368. 369. 370. 371. 372. 373. 374. 375. 376. 377. 378. 379. 380. 381. 382. 383. 384. 385. 386. 387. 388. 389. 390. 391. 392. 393. 394. 395. 396. 397. 398. 399. 400. 401. 402. 403. 404. 405. 406. 407. 408. 409. 410. 411. 412. 413. 414. 415. 416. 417. 418. 419. 420. 421. 422. 423. 424. 425. 426. 427. 428. 429. 430. 431. 432. 433. 434. 435. 436. 437. 438. 439. 440. 441. 442. 443. 444. 445. 446. 447. 448. 449. 450. 451. 452. 453. 454. 455. 456. 457. 458. 459. 460. 461. 462. 463. 464. 465. 466. 467. 468. 469. 470. 471. 472. 473. 474. 475. 476. 477. 478. 479. 480. 481. 482. 483. 484. 485. 486. 487. 488. 489. 490. 491. 492. 493. 494. 495. 496. 497. 498. 499. 500. 501. 502. 503. 504. 505. 506. 507. 508. 509. 510. 511. 512. 513. 514. 515. 516. 517. 518. 519. 520. 521. 522. 523. 524. 525. 526. 527. 528. 529. 530. 531. 532. 533. 534. 535. 536. 537. 538. 539. 540. 541. 542. 543. 544. 545. 546. 547. 548. 549. 550. 551. 552. 553. 554. 555. 556. 557. 558. 559. 560. 561. 562. 563. 564. 565. 566. 567. 568. 569. 570. 571. 572. 573. 574. 575. 576. 577. 578. 579. 580. 581. 582. 583. 584. 585. 586. 587. 588. 589. 590. 591. 592. 593. 594. 595. 596. 597. 598. 599. 600. 601. 602. 603. 604. 605. 606. 607. 608. 609. 610. 611. 612. 613. 614. 615. 616. 617. 618. 619. 620. 621. 622. 623. 624. 625. 626. 627. 628. 629. 630. 631. 632. 633. 634. 635. 636. 637. 638. 639. 640. 641. 642. 643. 644. 645. 646. 647. 648. 649. 650. 651. 652. 653. 654. 655. 656. 657. 658. 659. 660. 661. 662. 663. 664. 665. 666. 667. 668. 669. 670. 671. 672. 673. 674. 675. 676. 677. 678. 679. 680. 681. 682. 683. 684. 685. 686. 687. 688. 689. 690. 691. 692. 693. 694. 695. 696. 697. 698. 699. 700. 701. 702. 703. 704. 705. 706. 707. 708. 709. 710. 711. 712. 713. 714. 715. 716. 717. 718. 719. 720. 721. 722. 723. 724. 725. 726. 727. 728. 729. 730. 731. 732. 733. 734. 735. 736. 737. 738. 739. 740. 741. 742. 743. 744. 745. 746. 747. 748. 749. 750. 751. 752. 753. 754. 755. 756. 757. 758. 759. 760. 761. 762. 763. 764. 765. 766. 767. 768. 769. 770. 771. 772. 773. 774. 775. 776. 777. 778. 779. 780. 781. 782. 783. 784. 785. 786. 787. 788. 789. 790. 791. 792. 793. 794. 795. 796. 797. 798. 799. 800. 801. 802. 803. 804. 805. 806. 807. 808. 809. 810. 811. 812. 813. 814. 815. 816. 817. 818. 819. 820. 821. 822. 823. 824. 825. 826. 827. 828. 829. 830. 831. 832. 833. 834. 835. 836. 837. 838. 839. 840. 84

THE UNIVERSITY OF CHICAGO

There, which though it be counted as a great

Richmond, you see it is no less a matter to be

...to be made, then that of the e-

1991

2. The following is a list of the names of the persons who have been appointed to the various positions in the organization of the National Association of Manufacturers:

... ..

1990-1991

... ..

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U. S. DEPT. OF AGRICULTURE

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Position.

I have been thinking of you very much lately, and
 how much you have accomplished in the last
 year. I am sure you will be very successful
 in the future. I am sure you will be very
 successful in the future. I am sure you will be
 very successful in the future. I am sure you will
 be very successful in the future. I am sure you
 will be very successful in the future. I am sure
 you will be very successful in the future. I am
 sure you will be very successful in the future.

**What Pro-
gression is.**

The first of these is the *Arithmetical*, which is the science of numbers, and is divided into *Arithmetic* and *Algebra*. The second is the *Geometrical*, which is the science of the properties of figures, and is divided into *Geometry* and *Trigonometry*. The third is the *Mechanical*, which is the science of the properties of matter, and is divided into *Mechanics* and *Hydrostatics*. The fourth is the *Astronomical*, which is the science of the properties of the heavens, and is divided into *Astronomy* and *Chronology*. The fifth is the *Medical*, which is the science of the properties of the human body, and is divided into *Medicine* and *Surgery*. The sixth is the *Political*, which is the science of the properties of the human mind, and is divided into *Politics* and *Economics*. The seventh is the *Philosophical*, which is the science of the properties of the human soul, and is divided into *Philosophy* and *Theology*. The eighth is the *Divine*, which is the science of the properties of the human spirit, and is divided into *Divinity* and *Religion*. The ninth is the *Human*, which is the science of the properties of the human body, and is divided into *Humanities* and *Letters*. The tenth is the *Natural*, which is the science of the properties of the human mind, and is divided into *Natural Philosophy* and *Mathematics*. The eleventh is the *Artificial*, which is the science of the properties of the human soul, and is divided into *Artificial Philosophy* and *Mathematics*. The twelfth is the *Divine*, which is the science of the properties of the human spirit, and is divided into *Divinity* and *Religion*. The thirteenth is the *Human*, which is the science of the properties of the human body, and is divided into *Humanities* and *Letters*. The fourteenth is the *Natural*, which is the science of the properties of the human mind, and is divided into *Natural Philosophy* and *Mathematics*. The fifteenth is the *Artificial*, which is the science of the properties of the human soul, and is divided into *Artificial Philosophy* and *Mathematics*.

Arithmeti-
cal pro-
gression.

most numbers rehearsed or placed down in difference, diversity or excessse, be equal and like.

Tls center can't find Doug 30

Major. In them, it stays just about.

The Zerkow.

to matter, too, the way we can get the most out of it.

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|----|----|----|----|----|----|----|----|----|-----|
| 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 2 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 |
| 3 | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 | 30 |
| 4 | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 |
| 5 | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 |
| 6 | 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 | 60 |
| 7 | 7 | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63 | 70 |
| 8 | 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 | 80 |
| 9 | 9 | 18 | 27 | 36 | 45 | 54 | 63 | 72 | 81 | 90 |
| 10 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 |

YOUNG PEOPLE: If you begin at the

First number of any of them on the left hand,

and to 19020 Page, Washington, D.C. 20540
 Ed. Schmitt, 1000 S. 10th St., St. Paul, Minn. 55108

1941-1942

SECRET

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| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |
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(2) the common excess or difference to

It follows that the first, and the continuously so, must

as the first number in the collection, together with

11

1

10



intereste in progression: that is to say
 some part of the whole intereste: and so be
 intereste profit is simple arithmeticall
 metrical progression is: I have here
 and also: I shall here propose you six propo-
 sitions: of which four of them were propo-
 sed by a friend of mine some years before they
 published: and the two first were never before
 made knowne to any man of that be three Men.

Scholar. This doth greatly encourage
 me to be attentive unto your works: for I
 shall not only be instructed by your
 the common knowledges: Rules of this
 science: but besides that, to have a
 further perfection: in such as you have
 taught me: I shall be able to pass great
 studies: and shall be able to solve
 harder things: and longer: therefore I
 beseech you, let me be your
 Disciple.

But if you will take one Rule
 of this science: I shall be able to solve
 all the questions that are proposed.



I.

Meaning A
 rule.

2.

3.

4.

1. The first question of the first progression
 is: To find the summe of the first
 terms of the progression: when the
 first term, the last term, and the
 number of the terms are given.
 2. The second question of the first progression
 is: To find the summe of the first
 terms of the progression: when the
 first term, the last term, and the
 number of the terms are given.
 3. The third question of the first progression
 is: To find the summe of the first
 terms of the progression: when the
 first term, the last term, and the
 number of the terms are given.
 4. The fourth question of the first progression
 is: To find the summe of the first
 terms of the progression: when the
 first term, the last term, and the
 number of the terms are given.

The

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Many more considerations could I propound
you in these *Arithmetical Progressions*, but these
are sufficient, to give you occasion to think that
fields of knowledge and *Art* are infinitely
capable of enlargement.

Scholar. Happy meet! I told but well understand that which is already indicated in my letter. And yet in my humble opinion, some things are so self-evident (trifles) to be omitted in about Propositions. Therefore I have partly printed the Rules, and leaving to their Propositions.

Master. I will orderly for each of these six propositions give you Rules, and with every one an example, ⁹¹ unless the phenomena and easiness need no farther exemplifying, and aid.

For the Solution of the first, multiply the Exceſſe by a number leſſe by 1 then the number of the per-
ces, and the off ſome Add to the firſt number, if
you ſhall have the laſt number which is ſought for.

As for example: If there were seven places
in a progression Arithmetical, whose continu-
all increase of mutual places were 4
and the first number were 3, and I would
know what the 1st and seventh number were
I multiply 4 by 7 in one relation 74 the
number

number of the place) by 4. the first number
 24. which I write 5. that is with a 0. and
 that is the last number which I desire to
 know. And this you may straightway write
 in countrell proceeding from 7. till the
 seventh place. increasing every one by one
 thus 2024 I knowe that the number is 2024
 which is the last being also the seventh
 is 29.

Scholar. I perceive straightway that the
 party in this Rule which in all works is to
 be understood that is it will save one from great
 labour. In a progression from 20 to 29
 instead of the hundred places as was said
 also it is very easie to work. and well con-
 fary for the totall summe finding. In a very
 long progression. of which I will orderly
 write in the next. and therefore now let
 us see if we can answer the this question by
 this proposition.

A Merchant buyeth 30 pounds of Spices and
 agreeth to pay for the first pound 4 pence for
 the second 7 pence. for the third 10 pence for
 the fourth 13 pence &c.
 The question is how much he must pay
 for the last pound. and thus both much the 30
 pound cometh for
 Scholar. According to the proposition I
 will multiply 49 which is less by one than the
 number of the place by the question which is

...the first number ...
...the last number ...
...the number of the places, which is 25 the number ...
...the total sum ...
...the number of the places ...

Master. The third Proposition was ...
...the first or the last number given ...
...the first and the last ...
...the last ...
...the first ...
...the last ...
...the first ...
...the last ...
...the first ...
...the last ...
...the first ...
...the last ...

3 Proposition

Master. It is thus brought ...
Scholar. Then I entreat you to proceed to ...
...the number of the places, which you would ...
know. As in this Progression.

2 Proposition

...the number of the places ...
...the total sum ...
...the number of the places ...
...the total sum ...
...the number of the places ...
...the total sum ...
...the number of the places ...
...the total sum ...
...the number of the places ...
...the total sum ...
...the number of the places ...
...the total sum ...

encrease

Now w^hich is be^h known to be 7, and the
first number given, being 8, I would know
what number standeth under 4, that is to say,
in the fourth place. I multiply 7 by 3 (which
is less than the number of the place
propounded) that yeeldeth 21, to which I add
8, the first number, so cometh 29. which I
say to belong to the fourth place, as you see in
the example that is forth of. If in the third place
from the last, you would know what number
in the example should stand, the last number
being known to be 47, and the common
excess 7, then by 7 which is less by one than
the place propounded, I multiply 7 that ge-
teth 49, which appertaineth to the third place
if it help reckoned from the last, and so my
example geeth you.

In scholars oportet ut right good use of this
rule: If I had forgotten what the first num-
ber were, and remember still has the last the
common excess, and the number of the places,
then might I come by the knowledg of my
first number againe.

Report
non

And me thinketh, that it differeth not much
from the first proposition, saving that which
you make here a middle number, there was
made the last: and also in this point it differ-
eth, that in it the last was onely sought, and
no consideration had in numbing the places
from the last, as here I mark in your numbers
noted under your progression.

Master. And thinke you not, the middle
numbers

Numbers of progression standing of a hundred
to three hundred places, or more, may as much
number a man to come to the knowledge of
them by continuall increasing from the first
by the common excesse, as abating from the
last continually the common excesse, as the
very small numbers in a shorter progression
would do.

Scholar. Yes Sir, that I thinke right well,
therefore I am glad of this new framed pro-
position, and the manner of the working of it.

4 Proposi-
tion.

Master. The rule of the fourth Arabian, add
the first and the last together, and by the summe
divide the totall summe. Double the quotient, and
that will be the number of the places.

Scholar. Then if in a progression, whose
summe were 207, and the first number 12, and
the last 57, if I adde 57 and 12 together, that
maketh 69, and by it I divide 207, the quo-
tient will be 3, which I double, and so I have
6, and so many must be the number of the pla-
ces that this progression standeth on.

Master. Whether it be so, or no, how will
you try?

Scholar. Halfe 6, which is 3, being multi-
plied by 69, must make 207, the totall summe;
if 6 be the number of the places. For so the
whole work of your rule in summing any
Arithmetical progression did en-
forme me. I will then multiply
69 by 3, thus.

It cometh forth justly.

Master

Master. I want much herein to move your
 goodness both in memory and in will, im-
 plying your rule although in man (less hope
 to bid containe no such matter. Master
 Scholar. I pray you be aware from
 one example more. For I have heard that
 Master. I am well pleased, in that yet has
 lost; for you make me here longer here than
 willingly I should have been, but I cannot
 pay the help I could have omitted any thing
 to yet, without your great lack thereof. Scholar.
 I had received 89 pounds of
 certain men, but of how many I have forgot-
 ten, yet I remember that the first gave me 7
 pound; and the last 27 pound; and every pay-
 ment after which did rise by a like summe.
 And the man so whom I received this money
 conditioned with me, that he would pay me
 I should have received for my labour
 now, unless I could by Act find the truth of
 this case, I am like to lose the most part of my
 reward.

A question
 of money.

Master. I perceive you can hardly
 frame an example, which should concern your
 own gain: I pray you let me see how you
 would do justice in this point. Scholar. I have the first
 and the last together, that was 34
 which I divide by 4
 thus: 34 divided by 4 is 8
 and 2, which is the
 remainder of 2, in which 34 cannot be
 divided.

Propo-
 sition

Now to that note I am to the others for doubling of my quotient, and sheweth then both my justice, and my good will of my gains.

Master. Be careful the further from the matter, though it fall into a fraction: For you shall understand, that the fraction which of any sort will be proceeded to is the half of one such, as the units of the main number are. And that you may try if you doubt that which I sheweth, for there it will be equal to your divisor. For the double of 17 (the remnant) it maketh 34, and your Divisor also was 34, this maketh the remainder to be half of one.

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yenom to

Scholar. Now I am glad of this hard example: For with it I have a generall rule for the fraction that may hap in this work: for that the quotient being two and a half, I double that, it maketh 5, therefore should my gain be 5 shillings. And to be sure (by your leave) I will try it, for I will multiply half of 34 (which is the first shilling and last number joyned together) by 5, thus 17 by 5, thus 85.

It is most true (I see) that I should least nothing by the former working.

5 Propo-
sition.

Master. The first proposition hath this rule appertaining unto it: By the fourth rule find the number of the places that being done, from the last subtract the first, & the residue divide by a number lesse by 1, the number of the places, & the quotient will shew the excess which is sought for.

An

An example hereof shall be this: If ye had distributed 685 pounds to a certaine number of men, you neither can tell how many they were, nor how much the ones money exceeded his next before; but you are sure that the excess was equal between every two next; and also you remember that the first had 19 and the last 180 pounds, how would you finde the number of the name and the excess, continually observed in the succession of their payments?

Scholar. Your rule doth plainly bid first to finde the number of the places, which I will do according to the fourth rule: I adde 19, and 18 together, thus.

By this 197, I divide 685 thus.

Seeing there is no fraction but a whole number, being 3, I double that, and then must the number of the places be 10. Now from the last I subtract the first, as 18 from 19, thus: And so remaineth 99.

This 99 I divide by a number lesse by one then the number of the places, and seeing the places were 10, I divide 99 by 9, thus:

The quotient is 11, and so was the excess, if I have followed your rule right.

Master. You have brought every part of
this question both well in order, and truly in
the practise of your rules. Scholar. I will therefore it done also for
nably, so that the number of the places, the
excesse, and the totall summe may straight ap-
peare, as your first example stood,

The com-
mon ex-
cesse.
The pro-
gression.

11 11 11 11 11 11 11 11 11 11 11
19 30 41 52 63 74 85 96 107 118

That the places bee 10, and that from the
first to the last, the common excesse is 11; I
perceive most evidently: but whether the to-
tall summe bee 685, I have not yet proved,
which I will now doe: I adde 19 and 118
together, that maketh 137: I multiply this
by halfe the number of the places, thus.

All things agree most
exactly, so that I am per-
fect enough in these rules,
if I forget them not again.

Master. We make all things perfect.

6 Proposi-
tion.

Your sixth rule is this. By the number of the
places divide the totall summe, double the quoti-
ent, and that will bee the first and last joyned in
one summe. Then by a number lesse by 1, then
the number of the places, multiply the excesse,
that off come subtract from the first doubled
quotient, and the halfe of the residue is the first
number. The last number you may diversly find
out,

out, as by the first of our fixe rules, or by Sub-
tracting this first number from the summe which
hwe contained both the first and last jointly, (or
thirdly) by continuall adding the exesse.

Scholar. I pray you make this somewhat
more plaine with an example.

Master. If every moneth in the year (counting them now as 13) you gained clearly 40 shillings more then you did the moneth next going before, and at the years end you find the whole gaine 5720 shillings, but yee remember not how much either the gaine of the first moneth or the last was, by this rule it may be tried out.

**Example
of gain.**

Scholar. So that here ye seme to apply the
13 monechs to thirteene places, the 40 shil-
lings every one more then the other most before
it, to be the common excesse, and 5720 shillings
to the totall summe.

Master. It is true: by 13
then I divide 5720 in this
manner, and I am 100

I double this quotient
to have 3880 for the first
and the last summe joyned
together, by 12 which is
left by one then the num-

1710 (440)
1888

ber of the places. I multiply 40 (the common excess) so cometh 480. This 480 I subtract from 880, so remaineth 400: halfe whereof is the first number which wee desired to know: that is 200.

Example
of finding

And as for the last number, I can give you it three wayes. As by the first of my six rules I multiply the excess, by a number lesse by 1 then the number of the places, as 40 by 12 that giveth 480, which I adde to the first, being 200, so shall the last be 680.

The same summe cometh forth if we subtract 200 from 880.

And thirdly, If I begin at 200, and so proceed increasing by 40, I shall at the thirteenth place have 680, as thus:

| | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|
| 200 | 240 | 280 | 320 | 360 | 400 | 440 |
| 480 | 520 | 560 | 600 | 640 | 680 | |

Scholar. I thanke you most heartily for these six rules. Now if it bee your pleasure I would hear and learn somewhat of Progression Geometrical.

Master. There are yet very many rules and propositions which fall into this Arithmetical Progression.

And for the use and practise of them, I will propound unto you certaine pleasant and necessary Questions of Arithmetical Progression, and to the performance of their workings, such

such necessary rules and documents, as are requisite for the better understanding of them, or any such like; as in such (I suppose) question
A mercer sold 20 yards of Velvet to be paid in 12 weeks by Arithmetical proportion; the first week 6 shillings, the second week 2 shillings, the third week 18, and so forth increasing the number of weeks by 6 shillings, till the twelfth and last week were expired. The question is how many pounds he had for 20 yards of velvet.

A question of Velvet.

To the performance of this question, and such other the like, I set down the 12 payments in such sort, as for example, here appeareth.
Then touching the adding together of these summes, without the aid of Addition, according to the rule I taught you in Progression Arithmetical, I note the number of the places, which are 12, then adding the last number of the progression, which is 72, and the first number together, make 78; and multiplying 78 by halfe the number of the places, which is 6, amounteth to 468 shillings, and in pounds maketh 12 pounds 8 shillings. And so much hath the Mercer for his 20 yards of Velvet; which is nigh about 23 shillings 5 pence; a yard will
Scholar. I understand this worke very well; but is there any proof for the justifying hereof

noilbup A
noilb V 10

hereof, as you have of other workes (being so
perfectly wrought) that in your proceeding
and going forward from number to number
each number exceeding his fellow by an equal
or like quantity, is all that is demanded for
justifying of the same: yet notwithstanding,
because your request is reasonable, I will pro-
pose an example for the proove hereof.

The proof
of the last
question.

A certain man is bound to pay for 20 yards of
Velvet, the summe of 23 pound 8 shillings, and it
is to be paid weekly, in 12 weeks or termes by
Arithmetical progression. The question is
therefore to know with what number the said
Progression is to be begun and continued in
such equall proportion Arithmetically, that in
12 weeks the same may justly be accom-
plished.

For the resolution whereof, and of all such
other like, reduce 23 pound 8 shillings, all into
shillings, which maketh 468 shillings.

A generall
rule.

Then adde 1 unto 12, the number of the
termes, it maketh 13, which 13 you shall mul-
tiply by half the number of the termes, which is
6, it maketh 78; then divide 468 by 78, and
you shall finde 6 in the quotient, which is the
true number that shall begin and continue the
said Progression. What is to say, the first week
6 shillings, the second 12 shillings, and the
third weeke 18 shillings more, which is 18
shillings, and so every weeke as the first
shillings

A question
of a Farm.

Shillings more than the week before, as is
manifest in the question itself.

A Farme is to be sold to be paid by the weekes
in a year; the first week to pay 4 Shillings, the se-
cond week 8 Shillings, the third week 12 Shillings,
and so forth, increasing each number by 4, till the
number of 52 (which are the number of weeks in
a year is expired.) The question is, What the
price of the Farme cometh to?

Scholar. I doubt not but, by that you have
already taught me, to end this question very
well; wherefore I let forth the Progression
till his excessive 3 times. I would not draw
out this any farther, (to abridge your of great
labour that appears to fall out in this ques-
tion, and so may doe in any other the like) if a
question were proposed of 100 or 200 places
or more, and that this question; nor any other
the like can be ended, unless you know ab-
solutely what the last number of the Progressi-
on at the 52 place is, (or ought to be) I will
give you a generall rule how to know the last
number of any Progression Arithmetically, as
well as if you had ordinarily proceeded by con-
tinuall Addition, till you had come to the last
number wanted in this.

Multiply the excessive by a number lesse by
one than the number of the places, and thereo-
put the first number of the Progression, and
you shall have your desire.

A generall
rule.

Scholar.

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Scholar: This is well worth the
tiring: for if I understand you aright, I com-
ber that my excess is 4, which I multiply by
51, which is one lesse then the number of
the places, and it maketh 204, whereunto I
adde the first number of the Progression,
which is 4, and then it is 208, which you say
is my should be the last number of the Pro-
gression,

Master: This is a most approved truth. If
there were never so many places, you
Scholar: This is too late, that I were
much too blame, if I do not remember it. For
by the least betide, I have such an ease and
light into this excellent Art, that my heart
framed both seems to passe a great way more
furth study, and longer continuance.

Master: Many more considerations could I
propound you in these Arithmetical Progressi-
ons; but these are sufficient for a while, to give
you occasion to thinke that Reason of know-
ledge and Arts, are infinite capable of enlarge-
ment.

Scholar: Happy were I, if I did but well
understand that which is already written
and written. But these things, in my simple
fantasie, offer themselves to be greatly bene-
ficiall, unto the aid of Progressions. There-
fore now I will goe forward with your que-
stion. Now considering that the first and last
place is 208, I adde thereunto the first
number

number of the progressions, which is 4, it multi-
plieth 212, which 3 multiplieth by halfe the num-
ber of the places, which is 20, and it amount-
eth to 552 shillings. And to more is the 60
fall summe of Addition of this progression,
which maketh 275 pounds 12 shillings, as ap-
peareth here by my Tables.

Master, I like well your labour, and com-
mend you to your diligence: I will here
propound one example more, and therewithall
to this true with end, progression Arithme-
tical.

A certaine man bought 10 Ells of Holland, to be paid in 17 weekes, or termes, by Progression Arithmetticall: and the first week to pay 1 shilling 8 pence, the second week 3 shillings 4 pence, the third week 5 shillings, the fourth week 8 shillings 8 pence, and so forth, each week succeeding 20 pence more then the week before. The question is, what the summe of his 10 Ells cometh to.

A question of Holland

Scholar, Because here is mention made
both of shillings and pence, I feare there is
some harder matter contained herein, then in
the other before; therefore I pray you worke
it your selfe, and I will diligently mark your
labour.

A question of degree

Master: There is no more to be done in this, than in the other before: but because your request is so reasonable, be attentive unto me.

First, by the general rules, I seek to find out the last number of the 17 place, what this

this Progression ought to be. Therefore had
in my Tables multiplying the estate 20 by 16
which is one less then the number of the terms
for places, and it cometh to be 320; and
thereunto adding the first number of the pro-
gression, which is 20 pence, all is 340 pence
or 18 shillings 4 pence; for so much ought the
last number of the payments to be.

Then finally, to know what the whole 17
places amount unto, I add the first number
of the Progression and the last together, which
make 360. Now because 17 is an odd number,
whose halfe cannot be taken, I take the
halfe of 360, which is 180, and multiply for
180 by 17, cometh to 3060 pence, which
maketh as you see by Division 12 pound, 11
shillings. And so much is the buyer to pay for
his 20 Elles of Holland. Which 3060 pence
if you divide by 20, the number of Elles, that
man bought, you shall find 153 shillings 9 pence,
and so much payed he for an Elle one with
another.

The Proofs.

A certain man doth owe 12 pence 15 shil-
lings, to be paid in 27 weeks or terms by Arith-
metical progression. The question is to know what
what number he shall begin and continue the pro-
gression, in such equal proportions as the sum
may be truly paid and satisfied in 27 weeks.

A question
of debt.

of 12 pound 15 shillings, all into pence, which as you see here in many Tables, make 3060 pence, that I let stand by a while.

Then I add 1 to 17, the number of the place of terms, which maketh 18, which I should multiply by halfe the number of the weeks of terms which is 8; which 8 multiplied by 18 cannot well be done, unless you were acquainted with fractions or broken numbers, therefore you shall let that passe and multiply 17 by the halfe of 18, which is 9, (for that is all one with the multiplication of 8; and the multiplication of 9 into 17 maketh as you see 153, with which number you shall divide the 3060 pence before said, and the quotient bringeth forth 20 pence, which is the first number of payment to begin the progression withall; and so each weeke succeeding to rise 20 pence more then the weeke before, and thereby in 17 weeks shall 12 pound 15 shillings be payed: as before was sufficiently declared.

Thus much for progression Arithmetical.

Scholar. Certainly Sir, I know not how to render you condigne thanks for these benefits shewed me, which me thinketh are so easy, delightfull, and pleasant, that I count myself happy to be in your company.

Maker.

Progression
on
Arithmetic

Master. I am glad you delight so well here in, which is an Art of wonderfull dexterity to all sorts of men, of what degree or profession becom they be. And now will I proceed to progression Geometrically, wherein I will be more brief, both because I have been so long in this part of Arithmetical progression, and also so; that it would require the knowledge of Roots and square numbers, (whereof ye have learned nothing) if I should frame the like propositions in them as I have done in them. Therefore I will only teach you two practices about it, and so end the considerations and works of these progressions.

Progression Geometricall.

Progression Geometricall is when the number increase by a like proportion, that is, if the first number containe the first, 2, 3, or 4 times, so forth, then the third containeth the second many times also, and so of the fourth the third, 3, 6, 9, 12, 24, 48, and the first the fourth, 1, 3, 9, 27, 81, wherefore I set this for example. 1, 2, 10, 100, 50, 250.

Herein the first example you see, that every number containeth the other (that goeth next before him) two times: and in the second example three times, and in the third example five times. Now if you will know how to finde easily the summe of any such number, do thus: Consider by what numbers they be multiplied,

multiplied, whether by 2, 3, 4, 5, or any other, and by the same number multiply the last summe in the Progression.

To find the totall summe in any Geometrical Progression.

Scholar. I pray you worke it by this example: 2, 8, 32, 128, 512, 2048, which I have framed by proceeding from 2, and continually multiply by 4.

Master. Then must I multiply the last summe (which is 2048) by 4 also, and it will be 8192. Now must I abate from this sum the first number of the Progression, which here is 2, then resteth 8190: which summe I must divide by 1 lesse then was the number that I multiplied by. Seeing then I multiplied by 4, I must divide by 3, so dividing 8190 by 3, the Quotient will be 2730, which is the summe of all the Progression. And now to prove whether you can doe the same, I geve you these numbers to adde by this rule 3, 15, 75, 375, 1875, 9375, 46875.

Scholar. I cannot well tell by what number this Progression doth increase.

Master. In any such doubt doe thus: Divide the second number by the first, and the quotient will shew you the number that engendreth the Progression.

Scholar. Then is that number in this example 5, for so many times is 3 in 15.

Master. So is it. Now worke as I taught.

Scholar. The last number is 46875, which I multiply by 5, and it yeeldeth 234375, from which

which I abate the last number of the Progression that is 3, and there resteth 1 3 4 3 7 2, which I divide by 4, so that is one less then 5, and the quotient is 5 8 5 9 3, which is the whole summe of the progression.

Master. If you remember well this, you have learned the Art of progression both Arithmetically, and also Geometrically, which you may prove either by subtracting of each number alone from the summe, and so will there nothing remaine: or else by adding together of all the parcels, so that with the same summe amount.

A question
of Satten.

A Mercer hath 12 yards of Satten, which hee valuelh at 16 shillings the yard, and selleth the same 12 yards to another man to be paid as followeth: That is to wit, for the first yard to have one shilling, for the second yard two shillings, for the third yard foure shillings, for the fourth yard 8 shillings, &c. doubling each number following till the twelfth and last yard. The question is, who hath made the better bargaine of the buyer or the seller.

First you may set down 12, the number of the yards, as you see here in this example. And against each number the number of shillings due to be paid as the order of Duplication or Multiplication by two teacheth.

Then resorting to the adding up or summing of this progression, where I consider that the increase of this sum proceeded by the Multiplication of 2, & therefore after I have written

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16

Scholar. So Sir, by the grace of God this
yeare.

Master:

A question
of an horse

Master. Then what say you to this question? If
I sold unto you an horse having 4 shoes, and in e-
very shoe 6 nayles, With this condition; that you
shall pay for the first nayle one ob: for the second
nayle two ob: for the third nayle foure ob: and so
forth, doubling untill the end of all the nayles.
Now I aske you, how much would the price
of the horse come unto?

Scholar. First, to know the number of the
nayles, I must multiply 6 by 4. and it maketh
24. Then will I doe thus: I will write the
number of the nayles every one in order from
1 to 24, and against each number of the
nayles the summe of halfe pence duly, as the
order of Duplation or Multiplication by 2
teacheth, and as in the next figure following
appeareth.

When doe I resort to the Rule of summing
up the Progression, where I consider that the
increase of this summe proceedeth by the
Multiplication of 2, as the last example
did. And therefore multiplying the last
summe by 2 also, and it yeeldeth 16777216,
from which I abate the first number
which is 1, and then resteth 16777215,
which I should divide by one lesse then 2
or 1, which is 1, and the summe is 16777215.
Scholar. The price of the horse is 16777215 ob.

Progression.

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1 I did multiply, but seeing
2 that it is 1, I need not
3 divide it, for 1 (as you
4 have before said) doth make
5 ther multiply nor divide,
6 therefore I doe take the
7 number 16977205 for
8 the whole summe of the
9 halfe pence, which by Reduc-
10 tion I find to be 699050
11 shillings and 7 pence, halfe
12 penie: that is 340000
13 pounds, 10 shillings, 17
14 pence ob.
15 Master. That is well done,
16 but I think you will buy no
17 horse of the price.
18 Scholar. So sir, if I be wise.
19 Master. Well then, I can-
20 sweer mee to this questi-
21 on.
22 A Lord delivered to a
23 Bricklayer a certaine number
24 of loads of Bricks, whereof he

A question
of Bricks.

willed him to make twelve
walles, of such sort, that
the first wall should receive two thirdels of the
whole number, and the second two thirdels of that
which was left; and so every other, two thirdels
of that that remained: and so did the Bricklayer:
and when the 12 walls were made, there remain-
ed one load of Bricke.

Now I aske you, how many load went to each wall, and how many load was in the whole wall.

Scholar. Why Sir, it is impossible for mee to tell.

Master. Nay, it is very easie, if you mark it well. First well that I said, that every wall should receive two thirdels of the summe that was here. Then take away two thirdels from any summe, and you must needs grant that that whole remainder, is one thirdell of the summe left before. Example of 9, from which if you take two thirdels, there will remain three, which is one thirdell of 9. Likewise from three take two thirdels, and there will remain one.

Scholar. This is true, and now I perceive the least wall had but one load of brick.

Master. And by the same reason may you know how many load every wall had, according as the figures following both shew, and likewise what the whole summe of bricks was; for if you make 12 summes, and dividing by 3, still from the last remainder, as you may see here on the left line of the Table, there will appeare all the Remainders of the whole wall, and if you multiply the last of those 12 summes by 2 also, then will that be the summe of the loads which was delivered to the Brick layer.

The Remainder af- 3 1 1 6 Loads due to
ter every wall. 9 0 18 each wall.

27 9 54

81 8 162

243 7 486

729 6 1458

2187 5 4374

6561 4 13122

19683 3 39366

59049 2 118098

177147 1 354294

Summe of the loads 5 31448 delive-

Againe, if you double every Remainder, as you may see at the right side of this Table, those numbers will shew the summe of loads that went to each wall, howsoever you may perceive that each wall takes three times so great as the next less.

Scholar, now it appeares easie enough. Potentially I see that Arithmetick is a right excellent art.

Master, you will say so when you know more of the use of it: For this is nothing in comparison to other points that may be thought by it.

Scholar, When I beleeve you cease not to instruct mee farther in this wonderfull cunning

The Golden Rule, or Rule of Proportion direct, called the Rule of Three.

The Rule
of propor-
tion.



By order of the Science (as Men have taught it) there should follow next the extraction of Rootes of number, which because it is somewhat hard for you yet, I will let it passe for a while, and will teach you the feat of the Rule of Proportion, which for his excellency is called the Golden Rule. Whose use is by three numbers knowne, to find out any other unknowne; which you desire to know, as thus.

The Golden Rule.

Question
of board-
ing.

If you pay for your board for threemonths sixteen shillings, how much shall you pay for eight moneths?

To know this and all such like questions you shall consider which two of your numbers be of one denomination, and set them two the one over the other, so that the undermost be it that the question is of: as in this question, 3 and 8, be both of one denomination, for they both be moneths: and because 3 is the number that the question is asked of, I set the one over the other, and 8 undermost thus, with such a crooked draught of lines, When doe I set

the other number which is 16 against 2 at the right side of the line thus:

And now to know my question this must I do: I must multiply the lowermost on the left side by that on the right side, and the sum that amounteth I must divide by the highest on the left side: or in plainer words, thus I shall multiply the number of which the question is asked (which is called the third number) by the number of another denomination (which is called the second) and the sum that amounteth must I divide by the summe of like denomination (which is called the first)

Notes

Then for the knowledge of this question, I multiply 2 into 16 and there amounteth 32 which I divide by 3 & it needeth 10 shillings and 2 shillings remaineth which I turn into pence, and they be 24 pence, of which third part is 8 pence, so the third part of 128 shillings, is 42 shillings.

The third number.
The second number.

8 pence, which sum I write at the right hand of the figure 2 against 8 thus.

The first number.

Hereby I know that if three months boarding has come to 16 shillings, that 8 months boarding will come to 42 shillings & pence, & likewise of any other like question.

But here must you mark, that the first number and the third be of one denomination, and also the second and the fourth, for which you

Example A

to like denomination, and then of necessity must
the other number be in the second place.

Remember also that the place of the first num-
ber is highest on the left side, and the place of the
second right against it on the right side; the place
of the third number is under the first, as by a hole
examples you have seen.

Scholar. While I trust I can be

Master. But when the question be asked,

How long will 10s. 8 pence serve me? Here you see that 8
weeks will serve him, and saith 40 shillings.

But how long time 10s. 8 pence will serve
you know not, therefore you shall set 100 in

the third place, according as I told you even
now, and the first place must always be of

the same nature or Denomination, that the
third is of, which here is 40. Then must 8

needs be that other: Now multiply 10s. by
8, and it will be 840, which if you divide by

40, it will yield 21, which is the fourth num-
ber, and the whole time in weeks 21 weeks.

Thus will serve, if you spend 40 shillings in
8 weeks.

Now for the

question to this, as if you

should say 10s. 8 pence

serve for 8 weeks, 10s.

will serve for 21 weeks.

Other observations there be of working by

this rule, but I had rather that you should

learn this one well, then at the beginning

to

to trouble your minde with many tomes of
working, for this way can be as easie as all
the other, and hereafter you shall learn the o-
ther, more conveniently.

Note.

¶ And for your further aide and instruction
to make you better acquainted with this
Golden rule, I have here proponed six que-
stions, and their answers, which I think most
convenient and meet to prefer the desirous
to perfect understanding. The first foure are
all branches of one question sprang out of the
best tree (for a young learner to take of) that
groweth in this *Garden of Arts*: for that no
manner of question in the Rule of Three
whatsoever it be can be proponed, but it must
be comprehended under the reason or title of
one of these four.

The Questions.

If 15 Ells of cloth cost 7 pounds 10 shillings,
what comes 27 Ells to at that rate? Answer, 13
pounds 10 shillings.

If 27 Elles cost 13 pound 10 shillings, what
are 15 Ells worth? answer, 7 pound 10 shillings.

If 27 Elles cost 13 pound 10 shillings, how
many Ells shall I have for 7 pounds 10 shil-
lings? Answer, 15 Elles.

If I sell 15 Ells for 7 pound 10 shillings, how
many Elles are to be delivered for 13 pounds 10
shillings? Answer, 27 Ells.

If 8 pound of any thing cost 10 shillings 8
pence

The Golden Rule direct.

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pence: What money is to be received for 100 pounds Answer 95 pence, 4 fillings odd.

If 4 pound of any thing cost 7 pence: what money will 8765 pound of that commodity cost? Answer: 155 pound, 4 fillings, 3 pence, q.

Of all which questions, I omit the work of purpose, that you shall meet your task thereby at convenient leisure to situate each rule, and gather the fruit of them, and do unto me, before we make an end of this Rule, to give you some instructions of the Backer rule of Three, whose order is quite contrary to this that you have learned.

Scholar, I thank you heartily for the six Questions, which I will (God willing) practise at convenient times: I pray you proceed therefore to the Backer or Reverse Rule.

Example. If 100 pounds be worth 95 pence, what will 8765 pounds be worth? Answer: 155 pounds, 4 fillings, 3 pence, q.

~~If 100 pounds be worth 95 pence, what will 8765 pounds be worth? Answer: 155 pounds, 4 fillings, 3 pence, q.~~

~~The Backer Rule. If 100 pounds be worth 95 pence, what will 8765 pounds be worth? Answer: 155 pounds, 4 fillings, 3 pence, q.~~

The Golden Rule, or Rule

of Proportion Backward.

or Reverse.

Note this well.

Master. In the former Rule, evermore I took how much the third number is greater then the first, so much the fourth number is greater then the second. And contrariwise: look how much

The back-
er or re-
verse rule
of three.

the first summe is greater then the third (if it do chance so) so much is the second summe greater then the fourth.

But in this rule, there is a contrary order, as this: That the greater the third summe is above the first, the lesser the fourth summe is beneath the second: and this rule therefore you may call the Backer or Reverse Rule, as in example.

Question
of cloth.

If I have bought 30 yards of cloth of two yards breadth, and would have Canvas of three yards broad to line it withall, how many yards should I need?

Scholar. Why, there is none so broad.

Master. I doe not care for that, I doe put this example onely for your easie understanding: for if I should put the example in other measures, it would be harder to understand. But now to the matter: If you would knowe this question, set your numbers as you

The Golden Rule rentile. 283

do before: but you shall multiply the
first number by the second, and that ariseth
thereof, you shall divide by the third, which
thing if you doe here, I meane: if you multi-
ply 30 by 2, it will be 60: which number if
you divide by 3 there will appere 20: which
by I know, that it is 20 yards of cloth of two
yards broad: should be
lined with Canvas of
three yards broad: 20
yards of Canvas would
suffice, as this figure
sheweth.

And now because ye found fault with my
Example, how say you, perceibe you this?

Scholar, Yes Sir, I knowe.

Master, Then answer me to this question: how
many Ells of Canvas of 2 Ells broad would
serve to line 20 yards of say, of three quarters
broad?

Scholar, In good faith Sir I cannot tell: I
know not how to bring the summes to like
Denominations.

Master, Then will I tell you, first there is
mention here of quarters, and againe every one
of the measures both Ells and yards may be
parted into quarters, part them both in the
breadth and length, and then put forth the
question by quarters.

Scholar, Then shall I say thus: How many
quarters of Canvas of 2 quarters broad will
line 20 quarters of 3 quarters broad?

Master

301 Master. *Put me into the question.*
 302 Scholar. First, I will
 set them downe in their *Breadth. Length.*
 thus: $10\frac{1}{2}$ is $10\frac{1}{2}$.
 Then with the question,
 it is therefore the third
 number: then is 3 the number of the same deno-
 mination, I meane because they be both refer-
 red to breadth. Now I multiply 80 by 3, and
 it is 240, which I diuide by 3, and it peeldeth
 48. Then say I that 48 quarters of 3 quarters
 broad, will suffice to line 80 quarters of three
 quarters broad.

303 Master. Turn the quarters againe into Ells
 and yards.

Scholar. Then I say, that 9 Ells and three
 quarters of a yard of ell
 broad, will serue to line *Breadth. Length.*
 20 yards of three quar-
 ters broad, as this figure
 sheweth.

304 Master. Now what say you to this question.
 I lent my friend 400 pound for 7 moneths, how
 much money ought he to lend me againe for 12
 moneths to recompence my courtesie shewed him.
 Can you answer to this?

Scholar. Yes Sir, I *Moneths. Pound.*
 suppose, for 7 I will set
 downe my numbers
 thus: where I multi-
 ply 7 into 400, and it
 maketh 2800, which I diuide by 12, and it
 peeldeth

yeeldeth 237 pound, and there is 4 pound remaining of my division, what shall I do there with?

Master. Turne the same 4 pound into shillings, and then divide it by 12, as you did before.

Scholar. Well & it, it shall be done: so have I 6 shillings for my quotient, and yet remaineth 8 shillings upon my division.

Master. You must also reduce that 8 shillings into pence, which maketh 96, and divide that also by your divisor.

Scholar. So have I done, and I finde 8 pence for my quotient and nothing is left.

Master. Thus must you alwayes doe when any thing remaineth upon your Division, whether it be money, weight, measure, or any kind of thing whatsoever. This rule is so profitable for all estate of men, that by this rule onely (if there were no more but it) all men were bound highly to esteem Arithmetick.

By this Rule may a Captain in War, weigh many things, as Master Digger in his *Sestiocos* hath declared. Whelp now in this my simple addition, for a taste and encouragement, I will enlarge the Author with a question of still more, wishing you and every my Councrymen, or gentlemen whatsoever, that by nature be any thing given to Military Affairs, to be so familiar and acquainted with this Excellent Art, the which he shall finde not onely at the Sea, but also in the Campe and Field Service.

no. 100
100

no. 100
100

abun.

abundantly to the bar, either in Satisfaction
from a Captain of Souldiers wages, charges of
Ordnance, Powder, Shot, Munitions, and In-
struments whatsoever, as for example.

Question
of an Ar-
my.

If it should chance a Captaine which hath
40000 Souldiers to be inclosed with his enemy,
that he could have no fresh supplyance of victu-
als, which hee victuall which hee hath would
serve that Army but only three monthes, how
many should hee dismiss to make the victuall
suffice for the residue eight monethes? and so mil-
l Scholar.

As you may see the first
taught me, I set the Moneths downe
number thus; say 40000
say 3 these mo-
neths suffice 40000 ; 120000 said
to how many will
eight suffice? 120000 said
the first this; I multiply the first num-
ber into the second 40000 and it yeeldeth
 120000 , which summe I divide by 3 and
there will be in the quotient 40000 which I
I doe subtract from 40000 the re-
mainder will be 36000
that he must dismiss
 4000 , as this figure
saith.

Question
of a Fort.

Now Master, Now answer me to this question
If a Fort be inclosed by a Captain which
hath 40000 Souldiers to be inclosed with his enemy,
and such supplyance requireth that I should have
the

the same finished in 8 dayes than many workers
may say you are there to be appointed?

Scholar. As you taught mee, I set the
numbers 136, saying I had 136 Masons
in 28 dayes require
136 Masons, what
number of men by the
like proportion will 8
dayes require

To know this, I multiply the first number
28 into 136, and it yeeldeth me 3808. I divide
3808 by 8, and my quotient is 476. which
is the full number of Masons that may
ply this worke. And now all such
questions are very easie.

Master. Truly if you can calculate here-
in, you will find the way not only to the
wonderfull permut and permutation, but
therefore one question more I will propose;
and to leade on this Rule in whole numbers;
until we come to the use of broken num-
bers: for, but for the understanding of broken
numbers perfectly, not only in this Rule, but
in all other, the question that in the sight of
appearance seemeth to be 100 times more har-
der to absolue, may thereby be wrought as
soone, or sooner then this.

Scholar. Your words do greatly encourage
me to be studious to attaine whole numbers:
but might I once attain to be a practitioner
in broken numbers, I should think my selfe
happy.

Master. What say you then to this question? If 48 Joyners in two dayes make 200 light-horse-mens staves (estimating they worke but 12 houres a day) and such need requireth that 384 Joyners are set to the finishing of those 200 staves, in what time say you, will they make them up?

Scholar. I see here that I must turne my 2 dayes into houres. And so doing, I set my num- bers thus:

Saying, If 48 men are 24 hours, 384 men will make an end quickly. For it is grounded upon an old Proverb, many hands make quick speed.

I multiply 48 into 24 and it amounteth to 1152, which I divide by 384, and my quoti- ent is three houres, which is my desire.

Note.

I take this for a note worthy the marking, ei- ther in the Rule of Three forward, or backward, when the two numbers are multiplied together, the Product is of the same nature and denomina- tion that the second number is of.

The

The double Rule of Proportion direct.



Master. **W**hen you perceive now the use of this Rule, I will shew other which ensue of the same, and first the *Double Rule*, which is so called, because there is in it double working, by which things onely it differeth from this.

The double Rule.

Scholar. When by an example I shall understand it well enough.

Master. So shall you, and let this be the example: If the carriage of 100 weight (that is 112 pounds) 30 miles do cost 12 pence, how much will the carriage of 300 weight cost, being carried 100 miles?

Question of carriage

Scholar. I pray you shew me the working of it.

Master. You must make two workings of it: the first thus. If C weight cost 12 pence, how much will five hundred weight cost? Set your figures thus:

C weight. Pence.
1 12
5 2

And multiply 5 by 12, and thereof amounteth 60, which if you divide by one, the quotient will be still 60, that is the price of 300 weight for 30 miles.

Question

Then begin the second worke, saying: If

100 The Golden Rule double.

30 miles cost 60 pence,
 how much will 100
 miles cost? See your
 figure thus:

| | Miles. | Pence. |
|-----|--------|--------|
| 30 | 60 | |
| 100 | | 200 |

Then multiply 100 by 60, whereof amount-
 eth 6000, which being divided by 30, will yeeld
 200 pence. Then you may say, that 200
 pence will cost the carriage of 100 pounds
 weight 100 miles, after the rate of 12 pence
 for the 100 carried 30 miles.

Scholar. Now I perceiue it also.

Master. These and such other like questi-
 ons of the double Rule of Three, are to bee
 answered much sooner, at one onely working
 by the Rule of Proportion composed of five
 numbers, which anon I will shew you, and
 then when you haue the use thereof, you may
 use it which way you thinke good.

Scholar. Sir, I thanke you much for your
 courtesie: And I long now till this Rule be
 ended, that I may see how I may behaue my
 selfe with that new Rule of five numbers: for
 that I haue euer since you taught me hitherto
 in the Golden Rule, both forward and back-
 ward, wrought but with Three numbers
 onely.

Master. But yet a while we will go on for-
 ward with this Rule of Three, therefore an-
 swer to this question.

Question
 of sowing.

Thirty bushels of wheat sowed, yeelded
 in one year 360, how many will 80 bushels
 yeeld in 7 years? I meane, sowing every
 year

The Golden Rule Double.

year of those seven, till 80 bushels.

Scholar: I say, that if 30 bushels will yeeld 360 in one year, then 80 bushels will yeeld 960 in one year. When for the second yeeld, I say, if one year yeeld 960, then 7 years will yeeld 6720; as these two figures do shew, to shew the whole increase of the whole.

Seed. Increase. Year. Increase.

| | | | |
|----|-----|---|------|
| 30 | 960 | 1 | 960 |
| 80 | 960 | 7 | 6720 |

Question of Corne.

But now Sir, if I set forth 30 bushels of Corn to another man for 7 years, agreeing so that hee shall sow every yeare the whole increase of the Corn, and I at the end of these 7 years to have the halfe of the whole increase: I would know how many bushels will there amount to my part, supposing the increase to be after the rate of the last question, for 30 bushels in one year to yeeld 360?

Master: In such a question you must have so many severall workings as there be years, as for example: In the first year 30 bushels yeelds 360: then to know the yeelding of the second year, I must say, if 30 yeeld 360, how many yeeldeth 360? Worke by your Rule, and you shall finde 4320. Then say for the third year: if 30 yeeld 360, how many will 4320 yeeld? you shall have 51840, and so every year multiplying the whole increase by 360, and dividing

190 The Golden Rule double.

It be 30, the increase of the next year will amount as these 7 figures following doe orderly declare: where I have set 7 letters for the 7 years, of which the first is set without Art, because that is the increase which you do presuppose: and the last number of each other both shew the increase of that year that it standeth for, which the letters do declare, so that the increase of the seventh year, is 1074954240 bushells: how many quarters that is, and also how many wales you may by Reduction soon finde.

30 — 360 30 Z 360
 360 Z 4320
 30 Z 360 30 Z 360
 4320 Z 51840 51840 Z 622080
 30 Z 360 622080 Z 7464960
 30 Z 360 7464960 Z 89579520
 30 Z 360 89579520 Z 1074954240

Question
of mowing

Now with one question more I will prove you. If six Mowers doe mow 45 acres in five dayes, how many Mowers will mow 300 Acres in six dayes?

Scholar

The Golden Rule double. 191

Scholar. If 45 Acres require 6 Mowers, then 300 Acres require 40. Now againe, if 40 dayes require 40 mowers, then 6 dayes need but 33 mowers.

Master. Why doe you not make mention of this that remaineth in the last Division for the last part of the question is wrought by the Backer Rule, where the first number 3 is multiplied into the second, that is 40, whereof amounteth 120, which if you divide by the third number 6, the quotiene will bee 33, as you said: but then will there remaine: which cannot well be divided into 6 parts: howbeit you may understand by the 6 part of 3, the third part of one mans worke, which you must put to the 33; or else you must say that 33 Workemen will end all the 300 Acres in 6 dayes, save 2 mens worke for one day, or 2 dayes worke for one man. For such broken numbers called fractions, you shall hereafter more better perceiue, when I shall wholly instruct you of them.

Master. Yet one question more of field matter I will propound, and so I will make an end of this double Rule of Three.

Scholar. With all my heart, Sir I thanke you, and I will dispatch it as soone as I can, because I would faine see the order of the next Rule of 5 numbers.

Master. If a Captaine over a band of men did set 300 pioners a worke, which in eight houres did dig a trench of 200 Rods: I demaund how many labourers

Question
of entre-
ching.

Labourers will be able with a like trench in three
houres, to intrench a Camp of 3400 Rods.

Scholar. I thinke I am wile in the Back-
house ditch: for I know not well which way
to go about it. And besides that, truly I thinke
I shall never come to preferment that way my
profit is so small.

Master. You know not how God may raise
you hereafter by knowledge, and service into
the favour of your Prince, for the abasis of
your Country.

Example for Navigation: Sir Francis Drake,
a man greatly honoured for his knowledge,
was not the tallest man, and yet hath made
as great an adventure for the honour of his
Prince and Country, as ever Englishman
did.

Scholar. Sir, I thanke you for your good
encouragement, my minde, though I be little,
is as desirous of know-
ledge as any other: I
have pondered now a
little of it, and thus I
set forth the worke:

Saying, If 200 Rod require 300 men, what
shall 3400 rods require? I multiply 3400 by
200, and it yeeldeth 680000, which I divide
by 300, and my quotient is 2266 men.

Even must I say for the second worke; if
in 8 houres 500 men be able to discharge it,
how many shall performe the same in three
houres? Now if I would worke by the

Golden

The Golden Rule double. 193

Golden Rule of Proportion forward, I should find a lesse number of men: because three houres is lesse then 8 houres: but because reason teacheth mee, that the longer the time is, therein the trench must bee made, the more labourers I ought to have, therefore I use now the Backer Rule, as in example. And I have in my Quotient 13600. so many Pla-ners must I have to intrench the Campe in three houres.

Miller. You have answered the question
very artificially : And truly I commend you
for your diligence and apt understanding ;
and now according to my promise, I will (in
whole numbers) give you a little taste of the
Rule of proportion, compounded of five num-
bers.

The Rule of Proportion, composed of 5 Numbers.

The first
part of the
rule of
proporti-
on com-
pound,
direct.



The Rule of Proportion composed, is distinct for most needfull questions, into severall parts or workings. And there belongeth unto it alwayes five numbers, whereof in this Rule being the first part, the second number and the fifth, are alwayes of one nature and like denomination, which Rule is to be wrought thus: you must multiply the first number by the second, and that shall be your Divisor. Then again, multiply the other 3 numbers, the one by the other, and their Product shall be your Dividend.

And now according to my promise, we will first worke the question of weight and carriage, which I delivered you in the double rule of three, to bee absolved by this rule, which was this.

If the carriage of 1 C weight 30 miles cost 12 pence, what will the carriage of 5 C weight stand me in, being carried 100 miles?

C.weight. Miles. Pence. C.weight. Miles.

1 — 30 — 12 — 5 — 100

Now marke well how these five numbers stand: Then multiply the first number by the second, as 30 by 1, which maketh but

30,

The Golden Rule compound. 195

30. That number keep for your Divisor: When multiplied the other three numbers, the one into the other: that is to wit: 30 x 10 x 100, which maketh 30000: Lastly, 600000, which as you see here in our Tables, divideth by 30000, which 600000 you shall divide by the product of the two first numbers, which here is 3000, and you see there is found 200 pence, which is the duty that you ought to pay for the carriage of 500 weight 200 miles, after the rate of 4 pence a hundred, and agreeth with the conclusion of the double Rule of Three.

no less
should be

Note this.

Scholar: Sir I thank you, it is even so.

Master. Yet note this in a generality in this rule, look what unit or denomination your middle number is of (which here are pence) and of the like denomination or name is always your quotient.

Scholar: Well now and if it please you by your patience, I will see how I can end the question, next following of 30 Bushels of wheat sowed, which in one year yieldeth 300.

How many then will 80 Bushels in 7 years yield? 30 Bush. Year. 80 Bush. Year
yield in 7 years 1300 1. 360 180 7
following crop 80 1
year of these 7 80 1
will 80 Bushels, 288000
and according to your reasons I will set my numbers thus, 1300 1. 360 180 7
when

196 The Golden Rule compounded.

Master. I multiply 300 by 1 and the number 30
my Divisor: then multiplying the other three
numbers the one into the other, as before
saying Tables they make for 600, which
I divide by 300: and my Quotient is 2
halles, my Divisor for 600 is 300: and the
as the workings by the Rule of Three.

Master. But one question more I will pre-
sent unto you, and followe the Rule by the
piece. God herewith, that I may make you
work it in broken numbers.

Question
of Interest

What comes the interest of 258 pounds, for five
monethes, after the rate of 8 pound, taken in
the 100 pound for 12 monethes.

Scholar. Sir, this is yet within the com-
passe of some reasonable minde: therefore to
minister equity in this case, I will see how I
can worke the same,
which I set do thus: 12 monethes is 12, 12 mon.
thens, makinge thus 144 — 1200 by 8
I have not done wellly, for 1200, nothing
to be done the same.

Master. Proceed, you have not yett full.

Scholar. When I doubt not by the gift of
God but to end it: I multiply 1200 by 144, it
yeeldeth 172800, and the three other numbers
multiplied together produce 14400, which
I divide by 172800: and my Quotient is 2
pounds. Then according as you have taught
me heretofore, I take the 20 pence that
I left into shillings, and dividing it by
the first number, my Quotient is 12 shil-
lings

The Golden Rule compound: 197

ling. So I suppose, that the loan of 258 pounds for 5 months, after the rate of 3 pound in the 100 for a year comes to 2 pound 12 shillings.

Master. You say true, I commend your diligence: now behold the manner of the second part of this Rule.



The

The Golden Rule compounded
The Backer Rule, for the
second part of the Rule of
Proportion compound.
Master.



In the second part of this Rule of Proportion composed, the third number is like unto the first. And the Rule is to bee wrought thus: You shall now contrary to the last Rule, multiply the third number and the fourth together, and that product shall be your Divisor. Then multiply the fift by the second, and the product thereof by the first: and that is the number that shall be divided. For example, I propound this question, for a proove of my last question of Interest.

The proof of the last question.

A Merchant hath received 8 pound, 12 shillings for interest of certaine money for 5 moneths terme, which he received after the rate of 8 pound in the 100, for a year. The question is now, how much money was delivered to raise this interest.

Behold therefore the manner how the question is set forth.

li. moneths. li. moneths. li. l.
 100 — 12 — 8 — 5 — 8 — 12

Scholar. Sir, I perceiue it very well: and according

The Golden Rule compound

according to the working tables you presented for the working thereof: if it please you now it is set down. I thinke I can follow the works. 8 — 7 — 8 51 — 001

Master. Say again while, and before you work, mark well how I deliver a reason for the perfect understanding of this Rule, which is thus: If 8 pound in 12 moneths do yeeld mee 100 pound, to take 8 pound 12 shillings for 5 moneths, must needs yeeld a good deale more. 0002

Note.

So upon the knowledge that I have in this Art, The first part of this Rule is answerable to the rule of Three forward: and this latter part accordeth to the rule of Three backward. 0008214 00084

Schol. Sir, I reeld you most hearty thanks for these your last instructions, they have given me great light into these two rules, whereby I may the better by deliberation conceive how to use them hereafter when occasion shall require. 0008214 00084

Master. You say well, go to now if you will, and say your meaning in the question: But this Note take with you by the way, in as much as here is mention made of shillings, turne all your money as you work into shillings, for your more ease in working. 0008214 00084

Note.

Schol. If it please you to behold me a little, I will quickly end it: for I have but my first, my second, and my last number to be multiplied together for my dividend: And my third into

The Golden Rule compund

my fourth for my Division of gold corn
 100—12 8—5—8—

1000
 172
 48000 4128000
 1680000
 124000

quotient is 5160 shillings, which in pounds
 258, my pence

Master. I will have for this times in whole
 numbers and this Rule, and I will instruct
 you in the Rules of Fellowship. You may at
 your convenient leisure for your exercise
 make the same by the Rule of Three
 twice. And for your aid and encouragement
 therein, I set downe here a proffer, how to
 apply it.

| A | | B | |
|----------|-----|--------|-----|
| Moneths. | li. | Pound. | li. |
| 12 | 8 | 8 | 12 |

Ut now will shew you of the
 Rule of Fellowship or Comp-
 ny, which hath sundry opera-
 tions according to the differ-
 number of the Company. This
 Rule is sometime without difference of time,
 and some times there is not difference of time,
 First I will speak of that without difference of
 time, of which let this be an example.
 Let A & B partners of one Company make a bank
 of money thereby: for the first kind in company,
 the second 20 pound, the third 30 pound, and
 the fourth 40 pound, which they have
 long, till it was increased to 3000 pound. Where
 demand of you what should each share have the
 parting of this money.
The answer. A practice that this Rule is like
 the other; but yet there is a difference in this
 practice not.
 Answer. When shall I shew it to you: first
 by the Golden Rule, and the simple summe
 of the gains by that Rule shall be the
 cond summe, then for the third summe you
 shall



The Rule
 of Fellow-
 ship with-
 out time.

A question
 of compa-
 ny.

The Rule of Fellowship.

The Rule
of Fellow-
ship with-
out time.



Ut now will I shew you of the Rule of Fellowship or Company, which hath sundry operations according to the divers number of the Company. This

Rule is sometime without difference of time, and sometimes there is in it difference of time. First I will speak of that without difference of time, of which let this be an example.

A question
of compa-
ny.

Four Merchants of one Company made a bank of money diversly: for the first laid in 30 pound, the second 50 pound, the third 60 pound, and the fourth 100 pound, which stock they occupy so long, till it was increased to 3000 pound. Now I demand of you what should each receive at the parting of this money.

Scholar. I perceive that this Rule is like the other; but yet there is a difference which I perceive not.

Master. Then will I shew it to you: First by Addition, you shall bring all the particular summes of the Merchants into one summe, which shall be the first summe in your working by the Golden Rule, and the whole summe of the gaines by that stocke shall bee the second summe, Now for the third summe you shall

shall set the portion of each out of one
 each man one after another and so on
 ther, and then work as before by the Golden Rule, and
 the fourth summe will shew you each mans
 gaines: as in example. 240
 ple.

The parcels of these four Merchants made
 in one summe 240 pounds: set that in the
 first place, the gaines in the second, and the
 first mans portion of stocke in the third
 place, thus:

Now multiply the second by the third,
 and it will be 9000 , which you shall divide
 by 240 , and there will appear $37\frac{1}{2}$ pounds,
 thus:

And that is the gaines for the first man,
 for the first man, $37\frac{1}{2}$ pounds.
 Now for the second man, set the 50 pound that he brought, in the
 third place, and work as before: and his part
 will be $62\frac{1}{2}$ pound: as this figure sheweth.

And likewise for the third man, set his money
 which was 60 pounds, in the third place, and
 his part of gaines will be 75 pounds, as here appeareth.

And so for the fourth man; if you set his summe which is 100 pound, his gaires will bee 12 pound, as the work toller declare.

Scholar. This I perceive: but is there any way to examine whether

it be well done or not? Master. For the trial hereof, adde together all their four portions, and if their addition make the whole summe of their gaires, then is the work well done.

Scholar. What will I try by and by, the four parcels are these which added together make 300, which is the just summe of money that they gained, whereby I know the work is well done.

Master. Well; now another example will I put to you, not of gaires, but of losse, by one reason for both.

A question of losse.

If three merchants in one ship, and of one fellowship, had bought merchandise, so that the first had laid out 200 pound, the second 300 pound, the third 500 pound, and it happened by tempest that they did lose ever heard in the Sea, the merchandise of the value of 200 pound, how much should each man beare in this losse? Scholar. If I shall in this, as you did in the

pound 10 shillings. The second 82 pound, 17 shillings 10 pence. And the third paid 57 pound 5 shillings 6 pence. How many sheep must each of them have? Answer: The first shall have 840. The second 686. And the third 474. And that must you work thus.

Solution.

First, considering that your money is of divers denominations, you shall by reduction bring it all into the smallest denomination which is in it, that is to say, pence, and so will the Totall summe be 58000 pence.

Now if you turne each mans money into pence also, the first mans summe will bee 24360 pence. The second mans money will be 19894 pence; and the third mans money will be 13746 pence.

Now to know how many sheep every man shall have, let the whole summe of money, that is 58000 pence be set in the first place, and in the second place set the number of sheep, and then orderly in the third place set each mans money, and then multiplying the third and the second summe together, and dividing that that amounteth by the first, there will appear the number of sheep that each man ought to have. In these three figures do this.

Answey A
840

840

840

58000 **Z** 2000 : 58000 **Z** 2000
24360 **Z** 840 : 19894 **Z** 686

58000 **Z** 2000
13746 **Z** 474

Scholar. Why doe you set the money in the first place, seeing in the question you say 2000 sheepest, 58000 pence, and not thus: 58000 cost 2000 sheepest?

Master. You remember I taught you at the beginning of the Golden Rule, that the first and third numbers must be of one name, and of like things: and evermore the number that the question is asked of, must bee set in the third place.

Now is the question plainly this: If foure men bought 2000 sheep for 58000 pence, how many sheep shall each man have?

But seeing in this question, there ought more respect to be had to the summe of money then to the summe of the persons (for in the summe of money is their proportion toward the sheep, and not in the number of persons.)

If 58000 pence bought 2000 sheepe, how many did 24360 buy? Again, how many did 9894 pence buy? And how many bought 13746 pence?

Scholar. I perceiue it reasonable, and so

Ball 3 dot in all questions.

Note.

Master! Even so, But for easiness of the
worke, make this: Whencesoever the first
and second numbers have cyphers in the last
places, you may both in the Multiplication
and in the Division leave out those cyphers,
so that you leave out like many out of both
summes, as in this question, the first number
38000 hath three cyphers, and so hath the se-
cond, that is 2000: therefore cut away their
cyphers, and so will the first number be 38,
and the second 2: set them in their places,
and worke according to the Rule, and you
shall perceiue that will be all one, saving that
this is the shorter and easier way, as these
three figures do shew.

24360 **Z** 840 19894 **Z** 686

13748-474

And this you see is both easier, and also the more certain way to know the answer to this question.

Scholar. Truth it is as you say: But Sir
me feigneth I might aske a further question
here, not onely how many sheep each man
should have, but also what every sheep cost.

Master. That question doth not onely be-
long

The Rule of Fellowship

with time.

Master.

The Rule
of Fellow-
ship with
time.



Q the intent you may as well
perceive the same Rule with
diversity of time, I propole
this example.

Four merchants made a
common stocke, which at the
years end was increased to 35145 pound. Now
to know what shall be each mans portion of gain,
you must know each mans stock, and time of con-
tinuance.

Question
of a Bank.

The first man of these foure laid in 669 l.
which he did take from the stock againe at the
end of 10 moneths. The second man laid in
810 pound for 8 moneths. The third laid in
900 pound, for seven moneths. And the fourth
laid in 1040, for 12 moneths.

Note.
A generall
rule,

This question shall you examine as you
did the other before, saying that whereas in
the third place of the figure you did set each
mans summe alone, here you shall set the same
being multiplied by the number of their time:
and likewise in the first place of the figure you
shall set the number which amounteth of their
whole summes so multiplied by their time, and
added into one whole summe, as thus.

The

The Rule of Fellowship.

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The first mans summe is 669 pounds, which I multiply by 10 (that was the number of his time) and it maketh 6690. The second mans summe 810 pound, multiplied by 8 (which was his time) maketh 6480. The third mans sum 900 pound, multiplied by 7 (for that was his time) yeeldeth 6300. The fourth mans summe was 1040 pound, and his time 12: multiply the one by the other, and it will be 12480.

The foure summes thus multiplied by their times, must be set orderly in the third place of the figure; and in the first place must be set the whole summe of all foure, which is 31950; and the gaine must be in the second place, which is 35145. Now to end the question, I say first, 31950 did get

35145, what did 6690 get? Answer, 7359 pounds, as by this figure appeareth,

Likewise, the second man had to his part 7128 pound, the third must have 7930 pounds, and the fourth man shall have for his part 13728 pounds, as these figures do partly declare.

Math. 22. 37. 38. 39. 40. 41. 42. 43. 44. 45. 46. 47. 48. 49. 50. 51. 52. 53. 54. 55. 56. 57. 58. 59. 60. 61. 62. 63. 64. 65. 66. 67. 68. 69. 70. 71. 72. 73. 74. 75. 76. 77. 78. 79. 80. 81. 82. 83. 84. 85. 86. 87. 88. 89. 90. 91. 92. 93. 94. 95. 96. 97. 98. 99. 100.

parts behinde, of which I will not as now
make mention, because that without the
knowledge of Fractions they cannot bee
duely taught, and much lesse understood.
Therefore with I propose to you two or
three questions more, that thereby you
may better perceive the use of this Rule and
all other the like, and so make amends for this
Time, till my next book shall come forth.

¶ Three Partners by some ill adventure, suffer
some loss of 200 pound, whereof the first
said partner hath common stocke 100 pound, yett he
hath 100 pound, the second said partner hath 50 pound, and the
third 100 pound, by some accident the first partner
is taken down: so that he hath lost 80 pound, the first
partner hath 56 pound, the second partner hath 28 pound. The
question is for how much the first partner shall be
repaid, and the second partner shall be repaid.

A question
of losse.

For the solution hereof, and of such other
like, you must also multiply the first mans
200 pound, that hee put into the stock by his
time of continuance, which was 10 months,
and it maketh 2000: wherefore now I as-
sume, if his money that lost 80 pound multi-
plied by his time make 2000, what shall his
money make that lost 56 pound, and his that
lost 28 pound, which two numbers I admit
for the full of the rule of Three, as it is called
in these things, thus:

2000 : 80 :: 200 : x
2000 : 56 :: 200 : y
2000 : 28 :: 200 : z

To conclude, if you now divide upon the second mans portion, by 33, of which was his stocke that he laid into company, you shall finde in your quotient 4 moneths, and so for a long time did the second man put his money into the common stocke.

Lastly, if you divide the third mans rich laying in, which was 600 by 100, which was his stocke that he put into company, the quotient declareth his time of continuance, which was six moneths. And thus is the question resolved.

Scholar, Sir, I have attentively beheld
your working, and the more we travell here-
in, the more we thinke I am in love with this
excellent Art.

Master. When I say you to this question?

A question. There is in a Cathedrall Church 20 Canons,
of Canons and 30 Vicars, these may spend by year 1000
pound, but every Canon must have to support
fiftentimes so much as every Vicar hath by value
in every mans portion, say youe
Scholar. I pray you make the answer your
selfe also, so shall I perceiue best the manner
to answer to such other like.

Master. In this Question you must do
as in those before, that have liberty of
time.

The Rule of Fellowship.

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time, for there is diversity of portions. Therefore first you multiply the number of the portions by their difference of portions: (as you do in the other by time :) Then must you multiply the 20 (which is the number of Canons) by 5, (that is the number of their portion) so will it be 100. Then 30, (that is the number of Vicars) by 1 (that is the number of their portion) and it will be 30: put these two summes together, and they make 130. Then say thus; If 130 spend 2600 pounds, what may 100 spend? The Rule sheweth 1000 pounds.

Again for Vicars: If 130 spend 2600 pound what may 30 spend? Answer, 600 pound, as these figures shew.

$$\begin{array}{r} 130 \\ 100 \end{array} \begin{array}{l} \text{Z} \\ \text{Z} \end{array} \begin{array}{r} 2600 \\ 1000 \end{array}$$

$$\begin{array}{r} 130 \\ 30 \end{array} \begin{array}{l} \text{Z} \\ \text{Z} \end{array} \begin{array}{r} 3600 \\ 600 \end{array}$$

$$\begin{array}{r} 2000 \\ 600 \\ \hline 2600 \text{ pounds} \end{array}$$

But if every Canon should have so often times 4 pound as the Vicar should have 3 pound, then should I multiply 20 by 4, (that were 80) and 30 by 3, (that were 90) and then both were 170. Then should the figures be set as followeth.

$$\begin{array}{r} \text{li. s. d.} \\ 170 \\ 80 \end{array} \begin{array}{l} \text{Z} \\ \text{Z} \end{array} \begin{array}{r} 2600 \\ 1323, -10, 7. \end{array}$$

$$\begin{array}{r} \text{li. s. d.} \\ 270 \\ 90 \end{array} \begin{array}{l} \text{Z} \\ \text{Z} \end{array} \begin{array}{r} 26000 \\ 1376, -9, 5 \end{array}$$

But this sort is too hard for you, by reason

ion of the fractions, therefore I will let it rest to that place.

And by this rule you see what the 20 Canons may spend; which summe if you divide by 20, you shall see each Canons portion; and so of the Vicars, if you divide their summe by 30, the quotient will be their share Vicars portion.

The

The second Dialogue.

The accounting by Counters.

Master.



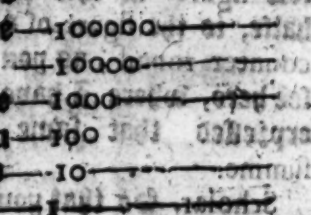
Now that you have learned the
kind of Arithmetick with the
Pen, you shall see the same Art
in Counters: which feat, doth
not onely serve for them that

cannot write and read, but also for them that can
do both: but have not at some time their pen, or ta-
bles ready with them.

This sort is in two formes commonly,
The one by lines, and the other without lines.
In that that hath lines, the lines do stand for
the order of places: and in that that hath no
lines, there must be set in their stead so many
Counters as shall need, for each line one: and
they shall supply the stead of lines.

Scholar. By examples
I would better perceive
your meaning.

Master. For example
of the lines; loe here you
see six lines, which stand
for six places, so that the



Numeration by
Counters.

nethermost standeth for the first place, and the next above is for the second, and so upward till you come to the highest, which is the sixth line and standeth for the sixth place.

Now what is the value of every place or line, you may perceiue by the figure which I haue set on them, which is according as you learned before in Numeration of figures by the Pen, for the first place is the place of unites or ones, and every counter set in that line, be-tokeneth but one: and the second line is the place of 10, for every counter there standeth for 10: the third line the place of hundreds, the fourth of thousands, and so forth.

Scholar. Sir, I doe perceiue that the same order is here of lines, as was in the other figures by places, so that you shall not need longer to stand about Numeration, except there be any other difference.

Master. If you do understand it, then how will you set 1543

Scholar. Thus as I suppose,

Master. You haue set the places truly, but your figures be not meet for this use: for the mee-test figures in this be-
 halfe, is the figure of a counter round, as you see here, where I haue expresse that same summe.

Scholar. So that you haue not one figure

for 2, for 3, for 4, and so forth, but as many
digits as you have, so many counters you set
in the lowest line, and so ever to you set one
in the second line, and so of other. But I know
not by what reason you set that one Counter
for 500, between two lines.

Master. You shall remember this, that
whenever you need to set downe 5, 50, or
500, or 5000, or set forth any number whose
numerator is 5, you shall set one counter for
it in the next place above the line that it hath
his denomination of: As in this example of
that 500, because the numerator is 5, it must
be set in a void space, and because the denomi-
nation is a hundred, I know that the place is
the void place next above hundreds, that is to
say, above the third line.

And further you shall marke, that in all
working by this sort, if you shall set downe
any summe between 4 and 10, *
for the first part of that num-
ber you shall set downe 5, and
then so many counters more,
as there rest numbers above
5. And this is true both of
digits and articles. And for
example, I will set down this
summe 297965, which
summe if you marke well, you
need none other examples for
to learne the numeration of
this sorte.

But this shall you mark, that as you see
in other kindes of Arithmetick, set a prick in
the places of thousands, in this work you shall
set a Starre, as you see before.
Scholar. When I perceiue Numeration:
But, I pray you, how shall I do in this Art,
to adde two summes or more together?

Master. I will shew you how to adde
two summes together, by way of example.
I will take these two summes, 123456789
and 987654321, and I will adde them
together, and you shall see the summe
which is 112222220.

Now I will shew you how to adde
three summes together, by way of example.
I will take these three summes, 123456789
and 987654321, and 543210987, and I
will adde them together, and you shall see
the summe which is 166666697.

Addition

Now I will shew you how to adde
four summes together, by way of example.
I will take these four summes, 123456789
and 987654321, and 543210987, and
210987654, and I will adde them together,
and you shall see the summe which is
187654320.

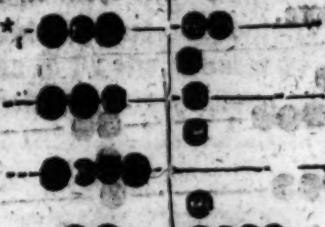
Addition.

Master.



The easiest way in this is to adde
but two summes at once toge-
ther: Howbeit you may adde
more, as I will tell you anon.

Therefore when you will
adde two summes, you shall
first set downe one of them, it forceth not which,
and then by it draw a line cross the other
lines. And afterward set downe the other
summe, so that the line may be betweene *
them: as if you
would adde 2659 to
8342, you set your
summes as you see
here.



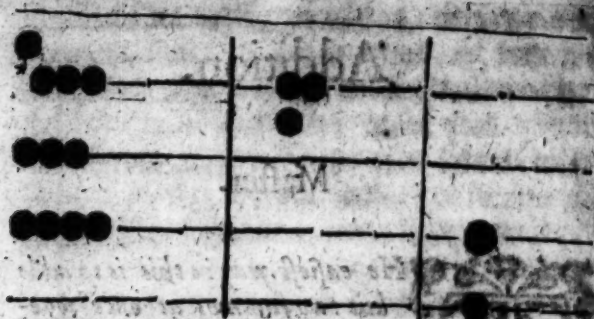
Addition
of two
summes.

And then if you
list you may then adde the one to the other in
the same place: or else you may adde them both
together in a new place: which way, because
it is most plain, I will shew you first.

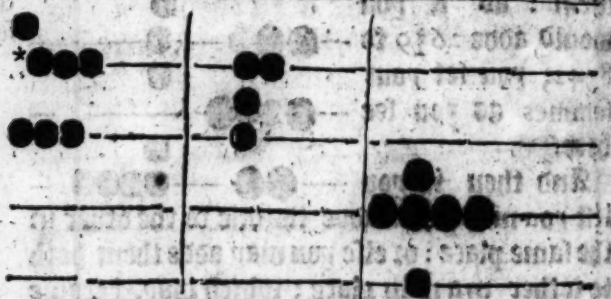
Therefore will I beginne at the Vnites,
which in the first sum is 9, and in the second
sum 2, the sum is 11: I write so I take up
and carry 1 to the next room, thus:

4

Then



Then doe I take up all the Articles under
a hundred, which in the first summe are 40,
and in the second summe 50, that maketh 90:
or you may say better, that in the first summe
there are foure Articles of 10, and in the se-
cond summe 5, which maketh 9, but then take
heed that you set them in their right lines, see
here.



Where I have taken a way 40 from the
first summe, and 50 from the second, and in
their stead I have set 90 in the third roome,
which I have set plainly, that you might
well

will perceive: becauſe ſee-
ing that 90 ſolth the 100
that was in the third room,
already both make 100, I
might better ſet theſe 6
Counters, ſet 1 in the third
line, thus:

For it is all in one ſum,
as you may ſee, but it is beſt never to ſet ſix
counters in any line, for that may be done
with one counter in a higher place.

Scholar. I judge that good reaſon, for nu-
mber are unneceſſary where one will ſerve.

Maſter. Well, then will I adde forth of
hundreds: I finde 3 in the firſt ſumme, and 6
in the ſecond, which maketh 6000, then doe
I take up, and ſet in the third room, where
is 100 already, to which I put 900, and it
will be 1000: therefore I ſet one counter in
the fourth line for them all, as you ſee here,



When adde I theſe ſummes together,
which in the firſt ſumme are, 8000, and in
the

To adde
summes
together.

the second 2000, and in the
doe I take up for those three places, and
then I set one counter in the fifth line, and
then it appeareth as you see them, that amount
bes 11001, for so many dots
amount of the Addition of
8342 to 2659.

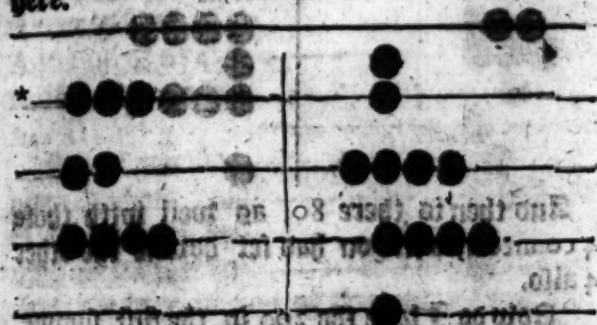
Scholar. Sir, this I do per
celve: but how shall I set one
summe to another, not chang
ing then to a third place?

Master. Marke well how
I doe it. I will adde together
65436 and 3245, which first
I set downe thus:

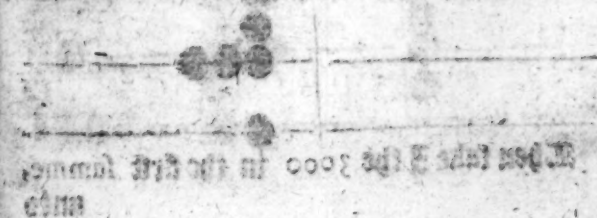


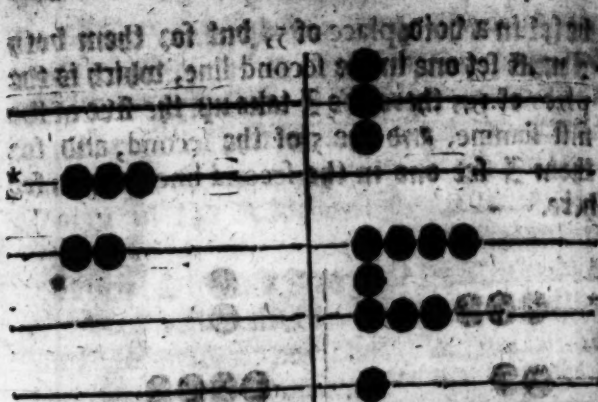
Then doe I begin with the smallest De
nomination, which is 1 in the second summe,
and set it in his place: then doe I finde 5 in
the first summe, and 5 in the second, which
put together, saving the two Counters, cannot

be set in a bold place of 5, but for them both
I must set one in the second line, which is the
place of 10; therefore I take up the five of the
first summe, and the 5 of the second, and for
them I set one in the second line, as you see
here.



Then do I likewise take the 4 Counters of
the first summe and second line, (which maketh
40) and addde them to the 4 counters of the
same line in the second summe, and it maketh
80: but as I said, I may not conveniently set
above 4 counters in one line, therefore to those
4 that I took up in the first summe, I take one
also of the second summe, and then have I taken
up 50: for which 5 counters I set downe one
in the space over the second line, as here doth
appeare.





And then is there 80, as well with those 4 counters, as if you had set downe the other 4 also.

Nowe do I take the 200 in the first summe, and adde them to the 400 in the second summe, and it maketh 600, therefore I take up the two counters in the first summe, and three of them in the second summe, and for them 5, I set 1 in the space above, thus :



Then take I the 3000 in the first summe, unto

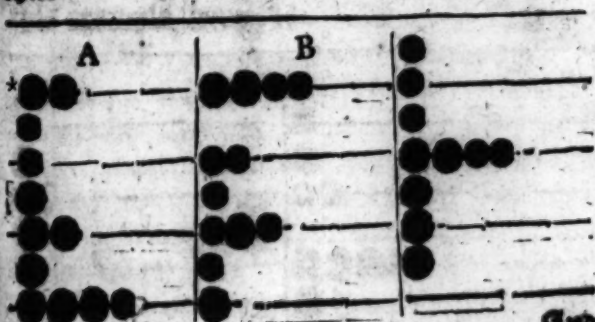
into which there are added to the second sum
agreesing, therefore I doe onely remove those
three counters from the first summe into the
second, as here becometh.

And you see the
whole summe that
amounteth of that
Addition of 65436
with 3245, to bee
68681.



And if you have
marked those two
examples well, you
need no further in-
struction in Addition of two onely summes:
but if you have more then two summes to adde,
you may adde them thus:

First adde two of them, and then adde the
third and fourth, or more, if there be so ma-
ny: As if I would adde 2679, with 4286,
and 1391. First I adde the two first summes
thus:



And

And then I hope the thing there's this

~~SECRET - NO FORN DISSEM~~

| | |
|--|--------------|
| | Total |
|--|--------------|

THE UNIVERSITY OF CHICAGO

[Faint, illegible markings]

[illegible]

~~SECRET~~

857 of 7456



But if more if you have the...

6. Let's say I think it's better that

School. John J. Louis is Dean of the

passage to subtraction, except that the

map to examine this manner of Administration

3 I think that were gonna be looking next.

Master: Where is the Dave piece here?

to the other Addition to the 22nd June

Subtraction: for that one is a four train.

Subtraction: $10 - 10 = 0$

...I will find from you the list of

[illegible]

traction, and that by using a large one. (1984)

10

21 3 1 6



100

1944

1940

100

— 300 —

100

SPRINT

Sub

1. The first part of the document is a list of names and titles, including "The Hon. Mr. Justice" and "The Hon. Mr. Justice".

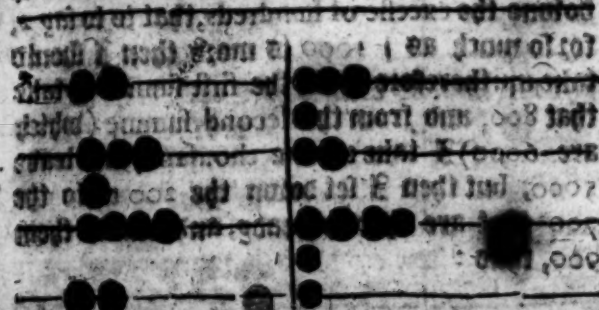
1990

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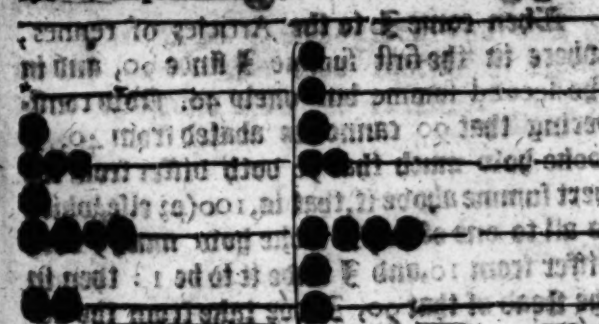
17

Subtraction.

These numbers first, thus 208 to subtract from 8746.

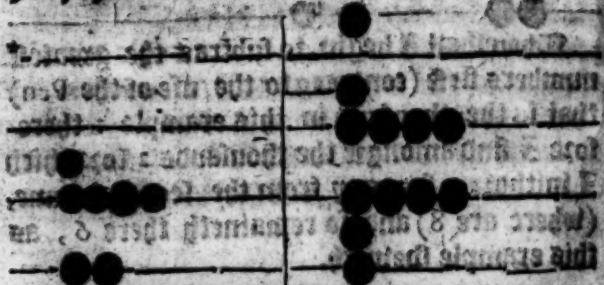


When shall I begin to subtract the greatest numbers first (contrary to the use of the Pen) that is the thousands in this example: therefore I find amongst the thousands 2, for which I withdraw 2 from the second 8, (where are 8) and so remaineth there 6, as this example sheweth.



Then

When doe I thinke to take the hundreds, of which in the first summe I finde 8, and in the second summe but 7, out of which I cannot take 1, therefore this must I doe: I will look how much my summe differeth from 10, which I finde here to be 2, then must I abate for my summe of 800, one thousand; and so below the excesse of hundreds, that is to say 2, so much as 1000 is more then I should take up: therefore from the first summe I take that 800, and from the second summe (which are 6000) I take up one thousand, and leave 5000, but then I set below the 200 into the 700 that are there already, and make them 900, thus:



When come I to the Articles of reynes, where in the first summe I finde 90, and in the second summe but onely 40. Now considering that 90 cannot be abated from 40, I look how much that 90 doth differ from the next summe above it, that is, 100 (or else which is all to one effect) I look how much 90 differ from 10, and I finde it to be 1: then in the stead of that 90, I doe take from the second

cond summe 100: but considering that is 10 too much. I set nothing in the next line. * worth for it, as you see here:

Saying that here I have set 1 Counter in the space in front of in the next line.

And thus have I subtracted all the 2 units I have wrote from 6 in the second summe and there will remain 4, thus:

So that if I subtract 2892 from 8746, the remainder will be 5854.

And that this is truly wrought, prove by Addition: for if you adde to this remainder, the same summe that you did subtract, then will the former summe 8746 amount againe.

And thus will I prove, and will I prove the same that was subtracted, which was 2892, and then the remainder: thus:

And

R

Then

[illegible]

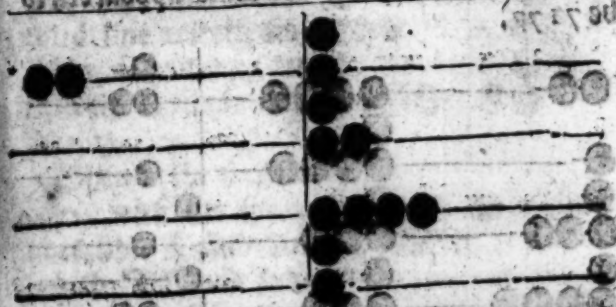
Columns 3 and 4 are the first 2 of 4 which make
here 5; to this I up 5 of hole counters, and
in their head 3 let 1 in the space, and one in
the lowest line, as here appears.

2001-2002

Alben



When we come to the hundreds, at which
I stand in the first summe, and in the se-
cond, that maketh 1600, therefore I take up
those 8 counters, and in their stead I set 1 in
the fourth line, and 1 in the space next beneath,
and in the third line, as you may see here.



Then is there left in the first summe but
only 2000, and in the second 5000, which
is 7000, which I shall take up from thence,
and set in the same line in the second summe
to the one that is there already: and there
will the whole summe appeare, as you may
well see; to bee 8746, which was the first

grosse summe, and
therefore I do per-
ceive that I had
well subtracted be-
fore.

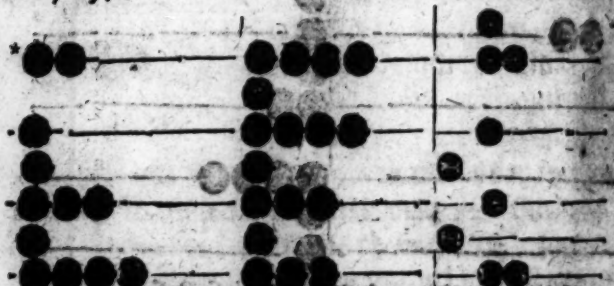
And thus may
you see, how Sub-
traction may bee
tried by Addition.

Scholar. I perceive the same order there
with counters, that I learned before in figures.

Master. Then let me see how you can try
Addition by Subtraction.

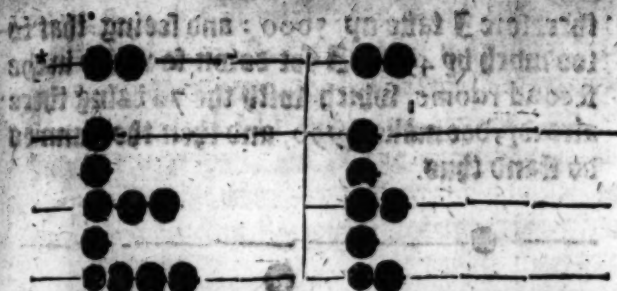
Scholar. First, I will set forth this exam-
ple of Addition, where I have added 2189
to 4988, And the whole summe appeareth to
be 7177.

Proof of
Addition
by Subtra-
ction.



Now to try whether that summe bee well
added or no, I will subtract one of the first two
summes from the third. And if I have well
done, the remainder will bee like that other
summe: as for example, I will subtract the
first summe from the third, which I sett thus
in order.

Then



Then do I subtract 2000 of the first summe, from the second summe, and then remaineth there 5000, thus :

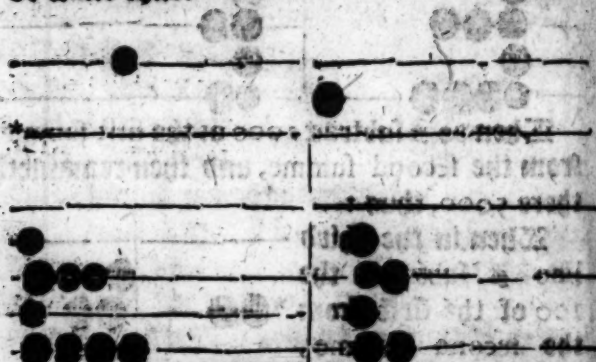
Then in the third line I subtract the 100 of the first from the second summe, where is onely 100 also : and then in the third line resteth nothing, as you may see in this example following.

Then in the second line, with his space over him I find 80, which I should subtract from the other summe : then seeing there are but onely 70, I must take it out of some higher summe, which is here onely 5000 :

3R 3

there,

therefore I take up 5000 : and seeing that is too much by 4990, I set down so much in the second roome, which with the 70 being there already, doe make 4990, and then the summes do stand thus.



Yet remaineth therein the first summe 5, to be abated from the second summe 10, which place of units both appear only 7: in the next I abate a higher summe, that is to say 10, the feeling that 10 is more then 9 (which

I should abate) by 1, wherefore shall I take 10 from the second, and set down the same in the first line; by which most lines as you see here.

And for this: I ended this book, and the summe of this Addition, which was the second sum of this Addition, and thereto, I perceive I have well done.

Master.

Master, To stand longer about this, it is Another
but toll: except that this you may also un- way of
derstand, that man doe begin to subtract in the Addition.
Counters, not at the highest summe as I
have taught you, but at the next, as
they doe use to adde; and when the summe to
be abated, in any line, reacheth unto then

the other, they do
they borrow out of
the next higher

I should abate
 1846, from 5378
 They set the four
 things
 First they take 6
 which is the lower line, and his space from 8
 in the same roomes in the second summe, and
 yet there remaineth two Counters in the
 lowest line. When in the second line must 4 be
 subtracted from 7, and so remaineth there 3.
 When 800 in the third line, and his space, from
 300 of the second summe cannot be, therefore
 do they abate it from a higher roomes, that is,
 from 1000, and because 1000 is too much by
 200, therefore must I set down 200 in the
 third line. After I have taken up 1000 from the
 fourth line. When is there yet 1000 in the
 fourth line of the first summe, which if I with-
 draw from the second sum, then do all figures
 stand in order, thus: 532.

Another way of Addition.

Another
way of
adding

[illegible]

So that (as you see) it differeth not greatly whether you begin Subtraction at the higher lines, or at the lower.

best, as some men like that one way
best, so some like the other: therefore you shall
knowing both, may use which you list.

Multi-

Multiplication.

Now touching Multiplication: you shall see your numbers into two roomes (as you did in those other kindes) but so that the multiplier bee set in the first roome: then shall you begin with the highest numbers of the second roome, and multiply them first after this sort.

Take the obermost line in your first working as it were the lowest line; setting on it some moveable marke (as you list) and looke how many Counters be in him, take them up, and for them set downe the whole multiplier so many times as you tooke up counters: reckoning (I say) that line for the unites. And when you have done with the highest number, then come to the next line beneath, and doe so even with it, and so with the next, till you have done all. And if there be any number in a space then for it shall you take the multiplier five times, and then must you reckon that line for the unites, which is next beneath that space. Or else after a shorter way, ye shall take onely halfe the multiplier, but then shall you take the line next above the space for the line of unites. But in each working, if by chance your multiplier bee an odd number, so that you cannot take the halfe of it justly, then must

must you take the greater halfe, and set downe that, as if that it were the just halfe: and further, you shall set one counter in the space betwene that line, which you reckon for the line of unities: or else, onely remove forthwarte the same that is to be multiplied.

Scholar. If you set forth an example, be-
of, I think I shall perceive you.

Master. Take this example: I would mul-
tiply 154 by 365, therefore I set my num-
bers thus,

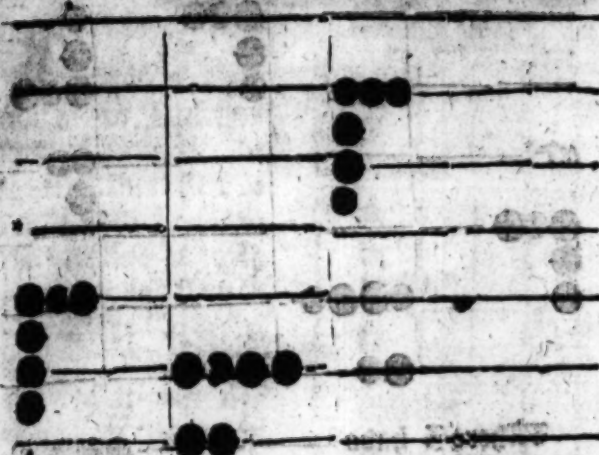
154
365

9220
92200
462000

5611000

Then first, I begin at the 1000 in the high-
est roome, as if it were the first place, and I
take it up, setting down for it so often (that
is once) the multiplier, which is 365, thus
as you see here: where, for the one Counter
taken up from the fourth line, I have set down
other five which make the summe of the mul-
plier, reckoning the fourth line, as if it were
the first; which thing I have marked by the
large set at the beginning.

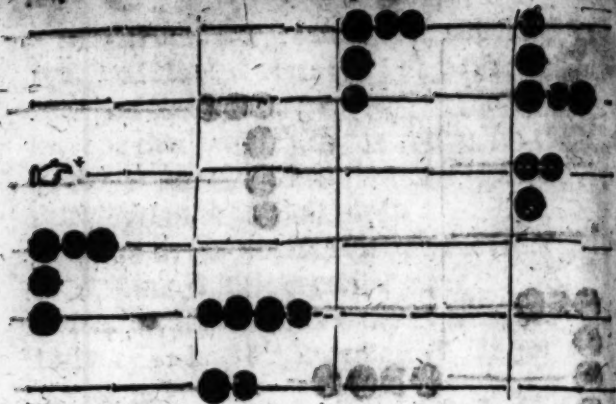
Scholar.



Scholar. I perceive well, for indeed this summe that you set down, is, 365000: for so much both amount of 1000, multiplied by 365.

Master. Well then go forth, in the next space I finde one Counter, which I remove forward, but take it not up, but (as in such a case I must) set downe the greater halfe of my multipliee (seeing it is an odde number) which is 181. and here I doe still let that fourth place stand as if it were the first, as in these examples you shall see.

And here



And here I have
 set the multipli-
 cation with other,
 but for the ease of
 your understand-
 ing, I have set a
 little line between
 them. Now would
 they both in
 one frame stand
 thus.



Another
forme of
Multipli-
cation.

Wherewith another
forme to multiply
such Counters in
space, is this: first to
remoue the finger to
the next line beneath
the space, and then to
take up the Counter,
and to set downe
the Multiplier five
times, as here you
see.

Which summes if
you doe adde toge-
ther into one summe,
you shall perceiue
that it will bee the
same that appeareth
of the other way
before, so that both
ways are to one ef-
fect: but as the other
is shorter, so this is
plainer to reason, for
such as have had
small exercise in this
Art.

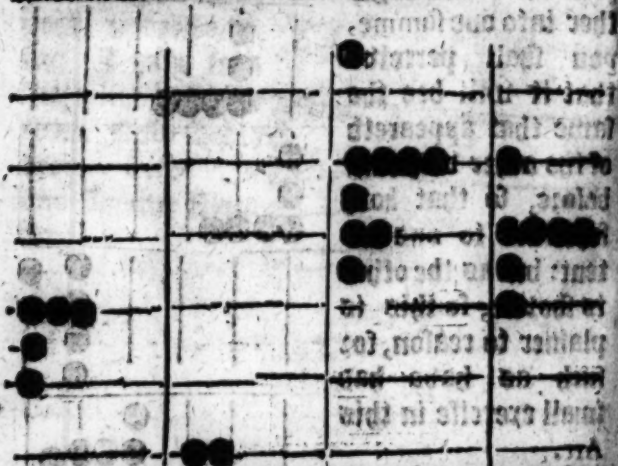
Notwithstanding
you may note them
in your minde before

you set them downe : as in this example you
might



might have said, five times 300 is 1500,
and five times 60 is 300, also five times five
is 25, which all put together, do make 1825
which you may at one time set downe if you
list.

But now to go forth, I must remove the
hand to the next counters which are in the se-
cond line, and there must I take up those
four counters, setting downe for them my
multiplier four times severally, or else I may
gather the whole summe in my minde first, and
then set it downe: as to say, four times 300
is 1200: four times 60 are 240: and four
times 5 make 20, that is in all 1460: that I shall
I set downe also, as here you see.



Which if I joine in one summe with the
former numbers, it will appear thus.

Will hereby you see, that 1542 (which is the number of years since Christ his Incarnation) being multiplied by 365, (which is the number of the dayes in one year) doth amount to 562830, which declareth the number of dayes since Christs Incarnation, unto the end of 1542 years, beside 385 dayes, and twelve houres for leape yea.

Example
of wages.

Scholar. Now will I prove by another example, as this: 40 Labourers (after 6 dayes the day for each man) have wrought 28 dayes. I would know what their wages doth amount unto.

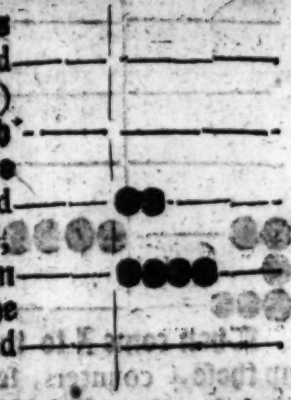
In this case must I worke doubly: First I must multiply the number of the Labourers by the wages of a man for one day, so shall the charge of every day amount.

Then Secondly I shall multiply the charge of one day by the whole number of dayes, and so shall the whole sum appeare: First there fore I shall set the sums thus.

Will here in the first place is the number (that is one dayes wages for one man) and in the second place is set the number of the workmen to be multiplied,

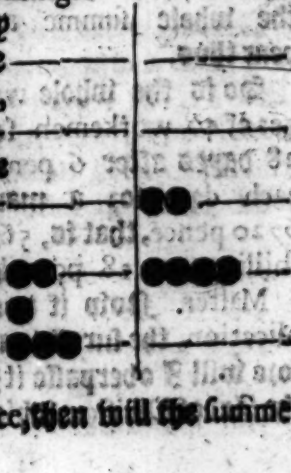
Then

Then say: If 6 times
4 (reckoning that second
line as the line of unites)
maketh 24, for which
summe I would set two
counters in the third
line, and 4 in the second,
therefore do I set two in
the third line, and let the
4 stand still in the second
line thus.



So appeareth the whole dayes wages to be
240 pence, that is 20 shillings.

Then do I multiply
again the same summe
by the number of dayes,
and first I set the num-
bers thus: then because
there are counters in di-
vers lines, I shall begin
with the highest, and
take them up, setting for
them the Multiplier to
many times as I took
my counters, that is twice, then will the summe
stand thus.



Division

Then

Then come I to the second line, and take
up those 4 counters, set-
ting so, then the Mul-
tiplicier 4 times, so will
the whole summe ap-
pear thus.

So is the whole wages of 40 workemen for 28 dayes after 6 pence each day for a man, 6720 pence, that is, 560 shillings, or 28 pounds.

Master. Now if you would prove Multi-
plication, the surest way is by Division; there-
fore will I overpasse it till I have taught you
the Art of Division, which you shall work thus.

Division:

Division.

First, set down the Divisor, for feare of forgetting, and then set that number that shall be divided at the right side, so farre from the Divisor, that the quotient may be set between them: as for example.

If 225 sheep cost 45 pound, what did every sheep cost? To know this, I would divide the whole summe, that is 45 pound, by 225, but that cannot be: therefore must I first reduce that 45 pound, into a lesser Denomination, as into shillings; then I multiply 44 by 10, and it is 900: that summe shall I divide by the number of sheep, which is 225, these two numbers therefore I set thus:

An example of sheep.

| | |
|-----|----|
| 44 | 10 |
| 900 | |
| 225 | |
| 4 | |
| 16 | |
| 00 | |
| 00 | |
| 00 | |

Then begin I at the highest line of the dividend, and seek how oft I may have the divisor therein, and that I may doe four times:

then say 3, four times 2 are 8, which if 3 take
from 9, there resteth but 1, thus:

[illegible]

And because I found the Divisor 4 times in the dividend, I have set, as you see, 4 in the middle room, which is the place of the quotient: but now must I take the rest of the divisor as often out of the remainder: therefore, come I to the second line of the divisor, saying two times 4 make 8, take 8 from 16, and there remaineth 2, thus: $\begin{array}{r} 4 \\ 4 \overline{) 16} \\ \underline{8} \\ 8 \\ \underline{8} \\ 0 \end{array}$

Then come I to the lowest number, which is 5, and multiply it 4 times, so to it 20, that take I from 20, and there remaineth nothing, so that I see my quotient to be 4, which are in value shillings, for so was the dividend: and thereby I know that if 225 sheepe cost 45 pound, every sheep cost 4 shillings,

Scholar.

Scholar. This can I do, as you shall perceive by this example. If 160 Souldiers spend every moneth 68 pound, what spendeth each man?

Example of souldiers wages.

**Example
of fouldi-
ers wages.**

First, because I cannot divide the 68 by 160, therefore I will turn the pounds into pence by Multiplication, so that there be 16320 pence: now must I divide the summe by the number of Souldiers, therefore I let them in order thus:

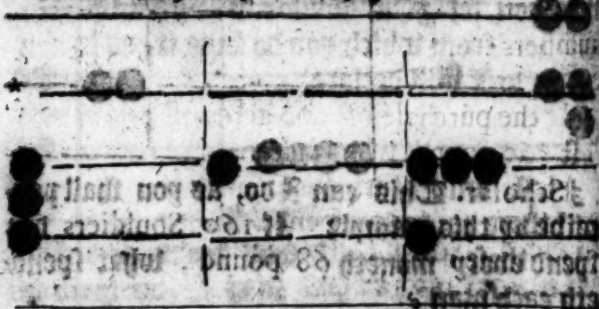
Then begin I at the highest place of the di-
vidend, seeking my Division there, which I
finde once, therefore I set 1. in the nether line.

Master,

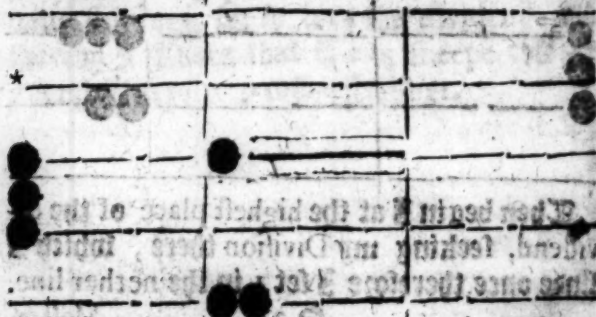
Master. Not in the nether line of the whole summe, but in the nether line of that 100, which is the third line.

Scholar. So standeth it with reason.

Master. When thus do they stand.



When I seeke I againe the ten, how often I may finde my divisor: and see that in 300 I might finde 100 three times: but then the 60 will not be so often found in 20, therefore I take 2 for my quotient: then take I 100 twice from 300 and there resteth 100, out of which with the 20 that maketh 120, I may take 60 also twice, and then stand the numbers thus:



will here

let the quotient of this work in the Exponent
be that is the line of units in respect to
Divisor in this work, and 8 equalled 8 of the

When I see both often the Divisor that be-
 comes in the dividend, and then I set 3, which
 then let 3, in the third line for the quotient,
 and take away that 6000 from the Dividend,
 and further I set the Divisor one line below,
 as you see here.

Let the hunter two lines higher than the other
to take him and no more you let. Insects I have
amongst these flowers and leaves which I have
it ought, and now the hunter on the leaf stands
alive let him be taken. The night comes on
down these flowers, I shall the insect
kill in place I can in the
dark, with
and add some more did one more collect.

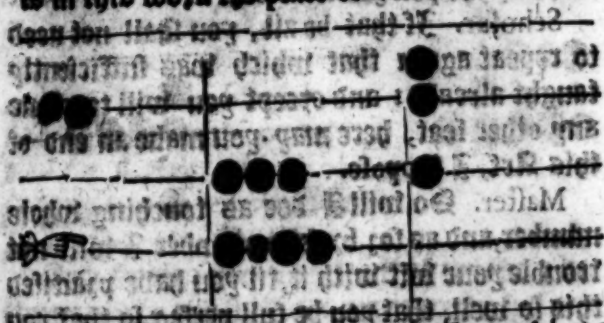
And then seek I how often the Divisor will be taken from the number against it, which will be four times and a remaining.

Scholar. But what if it chance that when the Divisor is so removed, it cannot be once taken out of the dividend again? it?

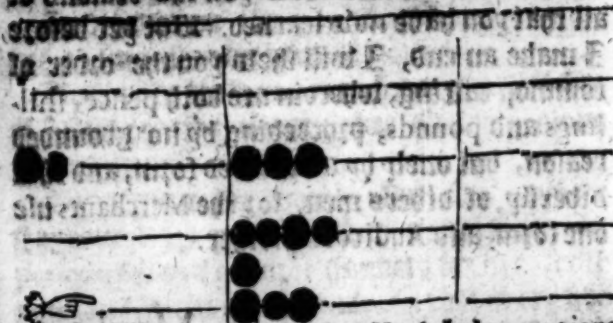
4 Master. Then must the Divisor be set in another line lower.

Scholar. So was it in Division by the pen, and therefore was there a cypher set in the quotient: but how shall that be noted here?

which makes tripling of the Divisor. But
now to returne to the example: I finde the di-
visor four times in the Dividend, and 1 remai-
ning: so 4 times I make 8, which I take
away, and there resteth 1, as this figure fol-
lowing sheweth: and in the middle space set
the quotient: I set 4 in the second line, which
is in this work the place of quires.



Then remove 3 the Divisor to the next low-
er line, and seek how often I may have it in
the dividend, which I may do here 8 times just,
and nothing remain, as in this forme.



Where you may see that the whole quotient
is 348 pence, that is 29 shillings, whereby I
know

know that to which cost the purchase of an
Arre. *Arre. is the name of a thing that is bought or sold*

Scholar. I do not require the proofs of multi-
plication, and also division. *Arre. is the name of a thing that is bought or sold*

Master. Those best proofs are such as be
the other; for multiplication is proved by di-
vision, and division by multiplication, as for the
work by the pen you learned. *Arre. is the name of a thing that is bought or sold*

Scholar. If that be all, you shall not need
to repeat again that which was sufficiently
taught already: and except you will teach me
any other feat, here may you make an end of
this Art, I suppose. *Arre. is the name of a thing that is bought or sold*

The rea-
son of all
the former
rules.

Master. So will I doe as touching whole
number, and as for broken number I will not
trouble your wit with it, til you have practised
this so well, that you be full perfect, so that you
need not to doubt in any point that I have
taught you, and then may I boldly instruct
you in the Art of fractions or broken numbers:
wherein I will also shew you the reasons of
all that you have now learned. But yet before
I make an end, I will shew you the order of
common casting, wherein are both pence, shil-
lings and pounds, proceeding by no grounded
reason, but onely by a received form, and that
differently, of divers men, for the Merchants use
one form, and Auditors another. *Arre. is the name of a thing that is bought or sold*

Merchants

Merchants use. A

BYs first for Merchants
form, mark this exam-
ple here, in which I
have expressed this
sum, 108 pounds, 10 shil-
lings, 15 pence. So that you
may see that the lowest line
serveth for pence, the next a-
bove for shillings, the third
for pounds, and the fourth for
scores of pounds.

Merchants'
Account
A



And further you may see that the space be-
tween pence and shillings may receive but one
counter, (as all other spaces likewise doe) and
that one counter in that place for 6 pence.

And the space betwene the shillings and the
pounds one counter standeth for 10 shillings.

And between the pounds and 20 pounds,
one counter standeth for 10 pounds.

But beside thole, you may see at the left side
of shillings, that one number standeth alone
and betokeneth 5 shillings.

So against the pounds, that one counter
standeth for 5 pound. And against the 20
pounds, the one counter standeth for five score
pounds, that is 100 pounds: so that every side
counter is five times so much as one of them a-
gainst which he standeth.

Auditors

Auditors Accompt.

Auditors
Accompt.

Now for the Accompt of Auditors, take this Example.

Where I have exprested the same summe,
198 pound—19 shillings—11 pence.

But here you see the pence stand towards
the right hand, and the other increasing order-
ly towards the left hand.

Againe you may see, that Auditors will
make two lines (one and more) for pence,
shillings, and all other values, if their summes
extend thereto. Also you see that they set one
Counter at the right end of each row, which
so set there, standeth for five of that room, and
on the left corner of the row, it standeth for 10
of the same row.

But now if you would add or subtract af-
ter any of both these sorts, if you mark the or-
der of the other feat which I taught you, you
may easily doe the same here without much
teaching: for in Addition you must first set
down one summe, and to the same set the other
orderly, and in like manner, if you have ma-
ny; but in Subtraction, you must set down first
the

the greater summe and from it must you abate
the other, every Denomination from his due
place.

Scholar. I do not doubt but with a little
practice I shall attain these both: but how shall
I multiply and divide after these sort?

Master. You cannot truly do any of both by
these sorts, therefore in such case you must re-
sist to some other way.

Scholar. They that use such Accounts that
it exceed 200 in the summe, they set not 5 at
the left hand of the scores of pounds, but they
set all the hundreds in another farther row, and
500 at the left hand thereof, and the thousands
they set in a farther row yet, and at the left side
thereof they set the 5000, and in the space over
they set the 10000, and in a higher row 20000,
which all I have expressed in this example,
which is 97869 pounds, 12 shillings, 9 pence,
or Ninety seven thousand, eight hundred
threescore and nine pounds, twelve shillings
and nine pence half peny farthing, for I had

not

not sola you before, where
neither bea you: thus
set downe farthings
which (as you see here)
must bee set in a double
place fideling beneath the
pence, for a farthing, one
counter ob, 2 counters
for ob, farthing 3 coun-
ters, and more there can
not bee: for 4 farthings
make a penny, which must
be set in his due place.

And, if you desire the same summe after Auditors manner, to have it is.

But in this thing you shall take this for sufficient, and the rest you shall observe as you may see by the working of each sort, for the divers wits of men have invented others and sundry wages, almost innumerable.

THE
SECOND PART OF
ARITHMETICK,

touching Fractions, brief-
ly set forth.

Scholar.



When I perceive your manifold businesses doth so occupie, or rather oppresse you, that you cannot as yet complaisantly and the Transcription of Fractions Arithmetically which you have prepared wherein not onely sundry Works of Geometry, Musick, and Astronomy be largely set forth, but also divers conclusions and naturall

Arithmetically fractions.

naturall Works, touching mixtures of Metals, and compositions of Medicines, with other strange examples. Yet in the mean season, I cannot say my most earnest desire, but importunately crave of you some briefe preparation toward the use of Fractions, whereby at the least I may be able perfectly to understand the common workes of them, and the vulgar use of those rules, which without them cannot well be wrought.

Master. If my leasure were as great as my will is good, you should not need to use any importunate cravling, for the attaining of that thing, whereby I may be perswaded that I shall any wayes profit the Common-wealth, or help the honest studies of any good Members in the same: wherefore while mine attendance will permit me to walk and talk, I am well willing to help you as I may.

Wherefore, first to begin with the explication of this name Fraction, what take you it to be?

What a
Fraction is

Scholar. Happy sir, I thinke a Fraction (as I have heard it often named) to be a broken number, that is to say, to be no whole number, but part of a number.

Master. A Fraction indeed is a broken number, and so consequently the part of another number: but that must be understood of such another number as cannot be divided into any other parts then Fractions: for although I may take the third part of 6, or the fourth

part of it, and so of other parts diversly, yet those parts be not properly nor ought not to be called Fractions, because they may be expressed by whole numbers, for the third part of it is 20, the fourth part is 15, the twelfth part is 5, and so forth of other parts, all which be whole numbers.

Therefore properly a Fraction expresseth the parts of part onely of a unite, that is to say, that the number which is the whole or entire summe of any Fraction, may not bee greater then one: and therefore it followeth that no one Fraction alone can bee so great, that it shall make 1: as by example I will declare, as soon as I have taught you to know the forme how a fraction is expressed or represented in writing.

What a Fraction is properly.

T Nume-

Numeration.

The ex-
pressing of
fractions.



*I*t first to begin with expressing by a Fraction; which is the numeration of it: you must understand that a fraction is represented by two numbers set one over the other, and a line drawn between them, as thus, $\frac{1}{2}$, $\frac{2}{3}$, $\frac{3}{4}$, which four fractions you must pronounce thus, $\frac{1}{3}$ one third part, $\frac{2}{4}$ three quarters, $\frac{2}{5}$ two fifth parts, $\frac{10}{17}$ ten seventeenth parts.

Scholar. I understand this forme of their expression and pronounciation, but their meaning or valuation seemeth more obscure. Yet I think that by the two first fractions I understand the valuation of the two latter fractions, and consequently of other.

Master. Value them then, that I may perceive your taking of them.

Scholar. $\frac{2}{5}$ betokeneth two fift parts, that is to say, if one be divided into 5 parts, that fraction doth expresse two of those 5 parts: $\frac{10}{17}$ doth signifie, that if one be divided into 17 parts, I must take ten of them. And thus I gather of the two first examples: for $\frac{1}{3}$, that is, one third part, doth easily declare, that if one thing be divided in to three parts, I must take out one of them: so $\frac{3}{4}$, that is three quarters, doth declare that one being divided into four quarters, I must take (for this Fraction) three of

of those quarters.

If there be no more difficulty in their Numeration, then I pray you go forward to their Addition and Subtraction, and so to the other kindes of works. For I understand that the same kindes of works be in fractions, that bee in whole numbers.

Master. There are the same kindes of works in both, albeit the order of them is divers, as I will shortly declare: but yet more in Numeration before we leave it. You must understand, that those two numbers which expresse a Fraction, have severall names, the *numerator*, which is above the line, is called the *numerator*, and the other beneath the line, is called the *denominator*.

Numerator.
Denominator.

Scholar. And what is the reason of their divers names? For (in mine opinion) both bee Numerators, seeing both they doe expresse the numeration of the Fraction.

Master. You are deceived: for one onely (which is the overmost) doth expresse the Numeration, and the Denominator doth declare the number of parts, into which the unite is divided, as in this example; when I say: divide a pound weight of Gold between foure men, so that the first man shall have $\frac{1}{4}$, the second $\frac{1}{4}$, the third $\frac{1}{4}$, and the fourth $\frac{1}{4}$.

Now do you perceiue that by the Denominator (which is one in all foure fractions) it is intended that the pound weight should be divided into so many parts, I meane 4.

and by the foure feuerall Numerators, is limited the diuers portion that each man shall have, that is, that when the whole is parted into 15, the first man shall have two of those 15 parts: the second man three of them: the third man foure: and the fourth man six. And so may you see the feuerall offices, as it were) of those two numbers, I meane of the Numerator and the Denominator.

And hereby you perceiue that a man can have no more parts of any thing, then it was diuided into, neither yet apply so many: so that it were vnaptly said: You shall have $\frac{15}{15}$, that is 15, fifteen parts of any thing, seeing it were better said, you shall have the whole thing.

Scholar. So both it appeares reasonably, so the labour is vaine to diuide any thing, and then to apply the diuision to no use. And much lesse reasonable were it to say $\frac{16}{15}$: for if the whole be diuided in 15 parts onely, it is not possible to take 16 of them, that is to say, more then all together.

Master. This is true touching the proper and apt use of the name of a fraction: yet improperly (and after a vulgar acceptation, for easinesse in work) both those formes bee called fractions, because they be written like fractions, although they be none in deed: so $\frac{15}{15}$, and generally in such other, where the numerator and denominator bee equall, are not fractions, but the whole thing with all his parts: And so $\frac{1}{2}$ is not to be called a fraction,

tion, but a mixt number, of a whole number and a fraction, for it is as $1\frac{1}{2}$, that is one whole and $\frac{1}{2}$ parts, as shall be declared in Reduction. Therefore they doe abuse the names that call them fractions, where the numerator is either equal, or greater then the denominator.

Scholar. But is there any needfull cause, why they should so abuse the names?

Master. There is cause why they shall sometimes for easinesse in worke write some numbers after that sort like fractions: but they needed not to call them fractions, but (as they be) whole numbers, or mixt numbers; (that is, whole numbers with fractions) or expressed like fractions, or as improper fractions.

Now must you understand, that as no fraction properly can be greater then one, so in smallnesse under one the nature of fractions doth extend infinitely, as the nature of whole numbers is to increase above one infinitely, so that not onely one may be divided into infinite fractions or parts, but also every fraction may be divided into infinite fractions or parts, which commonly be called fractions of fractions: and they be expressed diversly: as for example, $\frac{1}{2}$ of $\frac{1}{3}$ of $\frac{1}{4}$, that is, three quarters, of two third parts, of one halfe part. Whereby is signified, that if one bee divided into two halves, and the one halfe into three parts, and two of those

An improper fraction of a mixt number.

$$\frac{2}{12}$$

three parts be divided jointly into foure quarters, this fraction of fractions both represent three of those quarters.

Scholar. I pray you let me prove by example in common money; whether I doe rightly understand you or no. One Crowne which I take for an unke, both containe 60 pence; therefore the half of it is 30 pence, $\frac{2}{3}$ of that halfe is 20 pence, whereof is fifteen pence, so then 15 pence is $\frac{1}{4}$ of $\frac{1}{2}$ of a Crowne: and so is 3 pence $\frac{1}{4}$ of $\frac{1}{2}$ of a shilling.

Master. You perceiue this well enough: per this note I giue you by the way, that the forme of expressing these fractions is voluntary, and hath no other reason then the will of the Diuisor, which forme many follow: so some expresse them thus, $\frac{2}{3} \frac{1}{2} \frac{1}{4}$ without any signe of distinction between them, which forme also many follow. Some other do make lines betweene every fraction, and adde words of distinction, after this sort, $\frac{1}{4}$ of $\frac{1}{2}$ of $\frac{1}{4}$ which forme is best.

Some other expresse them thus, in slope forme, to distinguish them from fractions of one whole numbers, so if they were set in one right line thus, $\frac{2}{3} \frac{1}{2} \frac{1}{4}$ then ought it to be pronounced, three quarters and two chird parts, and a halfe, which maketh almost two whole unkes, lacking but one twelfth part. And so is it nothing agreeable with

with the other fractions of fractions: wherefor it is a great oversight in certaine learned men which do expresse them so confusedly with such severall fractions, that a man cannot know the one from the other.

Therefore some men (as Scifelius) do expresse without a line, numbers of proportion, being applied to Addition, or Subtraction, because they must be taken as two, where the line, in fractions, maketh them to be taken for one: For of the Numerator and Denominator is made one number.

Scholar. When I perceiue there bee three Three se-
vera l va-
rieties. severall varieties in fractions: First, when one onely fraction is set for one number, as $\frac{4}{5}$, that is, foure fifth parts. The second is, when there be set two or more severall fractions of one number, as $\frac{4}{5}, \frac{1}{3}$, that is, foure ninth parts, and two fifth parts. The third sort is fractions of fractions, as $\frac{4}{5}$ of $\frac{1}{3}$, that is, foure ninth parts of two fifth parts.

Master. You have said well, if you understand well your own words.

Scholar. If it shall please you, I will by an example in the parts of an old English Angel, expresse my meaning.

Master. Let me heare you.

Scholar. The old English Angel did containe 7 shillings 6 pence, that is 90 pence: Now $\frac{4}{5}$ of it is 72 pence: And of the same 90 pence, if I take $\frac{1}{3}$ and $\frac{1}{5}$, that is, foure ninth parts, and two fifth parts, $\frac{4}{5}$ is 40, and $\frac{1}{3}$ is 36 which both make 76: but if I take $\frac{4}{5}$ of $\frac{1}{3}$, that

is foure nine parts of two fifth parts, being $\frac{2}{5}$ is but 36, then $\frac{1}{3}$ of 36, will yeeld but 16, $\frac{1}{2}$ of 36 is but 18, and that taken foure times maketh 72.

Master. This is plainly exprest, and truly, and hereby (I doubt not) but you doe perceiue, that as great a difference as is between 16 and 72, so much difference is between those two fractions $\frac{2}{5}$ and $\frac{1}{3}$; and $\frac{1}{2}$ of $\frac{2}{5}$.

And now that you understand these varieties, I will proceed to the rest of the works: First, admonishing you, that there is another order to be followed in fractions then there was in whole numbers: for in whole numbers, this was the order: Numeration, Addition, Subtraction, Multiplication, Division, and Reduction: but in fractions, (to follow the same aptnesse in proceeding from the easiest works to the harder) we must use this order of works, Numeration, Reduction, Addition, Subtraction, Multiplication, and Division.

The order
of works
in fractions.

Scholar. That Addition and Subtraction should goe together, and Division to follow Multiplication, naturall order doth perswade: but why Reduction should be first in order here, next to Numeration and Addition, and Subtraction in the middle, I desire to understand the reason.

Master. As in the Art of whole numbers, Order would reasonably begin with the easiest, and so goe forward by degrees to the hardest.

hardest : even reason teacheth in Fraction the like order. And consider that Addition or Subtraction of Fractions, can very easely be wrought without Reduction : and contrariwise, Reduction may be wrought in the same form of Addition or Subtraction. Therefore was it orderly required that Reduction should goe before Addition and Subtraction, and this reason serveth for the placing of Reduction before the other.

Scholar. Then, if Reduction be the easiest, I pray you declare the forme of it, first by rule, and then by example.

Master. Your request is good.

Redu-

Order of Fractions
to be reduced
before Addition
or Subtraction

1

2

2

Reduction of Fractions

Of reduction of Fractions, there are five varieties.



Therefore will I now declare the five varieties of reduction of fractions, which commonly hath five varieties, in formes.

I

First, when there bee sundry fractions of one intire unite, they must be reduced to one denomination, and also into one fraction.

2

Secondly, when there be proponed fractions of fractions, they must be reduced likewise into one fraction: for otherwise they cannot be brought into one denomination.

3

Thirdly, when an improper fraction is proponed, that is to say, a fraction in form, which indeed is greater then an unite: it must be reduced into apt form, expressing the unite or unites of it, and the proper fraction distinctly. And sometimes also it shall be needfull to convert such a mixt number of unites with fractions, into the form of a fraction, that is, into an improper fraction: which two forms I esteem but as one, because they work one kind of number.

4

Fourthly, there happeneth sometimes fractions to be written in great numbers, which might be written in lesser numbers, therefore is there a mean to reduce such great numbers into their smallest termes.

5

Fifthly, when any fraction betokeneth the parts of a whole thing, which hath by common partition certain

certain parts, but none of like denomination with that fraction, then may you reduce the said fractions into another, whose denomination shall expresse the common parts of that whole thing.

Scholar. This distinction in Doctrine be-
lightens me much, but more will hope their
present fruit: for as yet I doe not understand
scarcely the varieties, and much less the use
of it, and use of these methodes.

Master. Reduction is a wonderful alteration
of Numbers out of one forme into another,
which is never done utterly, but for some need-
full use, as for every of the said five severall
formes, I will distinctly declare.

First therefore, when two, or more severall
fractions of any unite be proponed: as, for ex-
ample, $\frac{1}{2}$ and $\frac{1}{3}$, because it is hard to tell
what proportion of the intire number those
two fractions doe expresse, therefore was Re-
duction devised, to be a mean whereby these
severall fractions might be brought into one
denomination and fraction.

The first
form of
Reduction

And in these fractions, this is the Art for
bringing them to one denomination.

Multiply first the denominators together, and
the totall thereof you shall set twice down under
two severall lines for two new denominators, or
rather for one common denominator. Then multi-
ply the numerator of the first fraction, by the de-
nominator of the second, and set the totall thereof
for the Numerator over the first line. Likewise
multiply the Numerator of the second fraction

How to
reduce fra-
ctions of
divers de-
nominati-
ons into
one deno-
mination.

by

by the denominator of the first; and set that total over the second line for the Numerator of that fraction: & so are these two first fractions of several denominations, brought to one denomination.

Scholar. If I understand you, as I think I doe, my Example shall declare the same. The Fractions which you proposed were these, $\frac{3}{16}$ and $\frac{4}{6}$ whose Denominators (being 16 and 6) I multiply together, and there amounteth 96, which I set under two lines, thus:

When I multiply the Numerator of the first fraction by the Denominator of the second, saying, 3 into 6 maketh 18, that I set over the first line for a new Numerator, and it will be thus: $\frac{18}{96}$

Also likewise I multiply the Numerator of the second fraction, by the Denominator of the first, saying, 4 times 16 maketh 64, that I set for the second Numerator, and the fraction will appear thus: $\frac{64}{96}$

So that both fractions brought to one denomination, must stand thus, $\frac{18}{96}$ and $\frac{64}{96}$.

Master. You have done well.

Scholar. I beseech you let me examine it after my accustomed forme, by common parts of coyne or other measure.

Master. Go to.

Scholar. I have a peece of Gold which is accounted worth 8 shillings, and containeth 96 pence, whereof $\frac{1}{2}$, that is, the sixteenth part is 6 pence, and $\frac{1}{4}$ is 18 pence, that is

is 11. And the 11 of the same pence of gold is 16 pence, is that 11 pence maketh 164 pence, that is 11. And so 3. And the 11 pence is agree with the other before.

Master. So have you now the Art to bring two such fractions into one denomination. And if there be more then two, then must you multiply all the Denominators together, and set the totall thereof so many times down as there bee fractions; and then to get for each one a new Numerator, multiply the Numerator of the first, by the Denominator of the second, and the totall thereof multiply by the Denominator of the third, and so forth, if there be more. Likewise multiply the Numerator of the second, by the Denominator of the first, and the totall thereof, by the Denominator of the third. And in the same sort multiply the Numerator of the third into the Denominator of the first, and the totall thereof into the Denominator of the second, and so forth if there were more. So these three fractions $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{4}$ do make by Reduction these other three fractions of denomination 12: $\frac{6}{12}$, $\frac{4}{12}$, $\frac{3}{12}$.

All which you may bring into one Fraction by adding the Numerators together, and putting the totall for the totall Numerator, reserving still that same common Denominator. And those three Fractions make one improper Fraction, thus:

Scholar. All this I perceve, and also that this last Fraction is more then an unite, and therefore you did call it an improper fraction.

Master.

Note the Reduction of three fractions, or more, into one.

Master, I have retained other Rules for working in this Reduction, which I will briefly touch also, to give you more exercise in the exercise your wilt therein.

The first variety of Reduction

The first variety is this: When you have made and written down your common denominator (as I have taught before) then multiply your numerator for the first, do thus: Divide the common denominator by the denominator of the first fraction, and the quotient multiplied by the numerator of the same, yieldeth a new numerator for the first new fraction. So likewise do with the second and the third, and with all the residues, if there be more.

Scholar. What will I prove in your last example of these three fractions $\frac{1}{5}$, $\frac{2}{3}$, $\frac{3}{4}$. When the denominators be multiplied, they make 60: for 5 into 4 maketh 20, and 20 by 3 yeeldeth 60, that I set down three times thus: then to have a numerator, for the first, I must divide 60 by 5 (the denominator of the first) and the quotient is 12, which I must multiply by 2 (the numerator first) and that maketh 24, and so have I for the first fraction, $\frac{24}{60}$.

Likewise for the second fraction: I divide 60 by 4, and there cometh 15, which I multiply by 3, and so have I 45, for the second fraction $\frac{45}{60}$. Then for the third in like sort will come $\frac{45}{60}$.

The second variety.

Master. Another way is this: If it happen so, that the lesser denominator, can by any multiplication make the greater, then note the multiplier, & by it multiply the numerator over that lesser denominator,

for, & for the lesser denominator put the greater, as thus in these two fractions $\frac{1}{2}$ and $\frac{2}{3}$, three being the lesser denominator multiplied by 4, will make 12, which is the greater denominator: therefore by the same 4 I do multiply 2, which is the numerator over 3, and that maketh 8: under which I do put 12, being the greater denominator, which is also made by multiplication of 4 into 3, and so have I these two fractions $\frac{8}{12}$ and $\frac{12}{12}$ thus shortly reduced, without altering the one fraction.

Scholar. This I understand.

Master. Then mark this third way: If the denominators do not happen so, that one by multiplication may make the other then look whether they both may be parts of any other one number, as in $\frac{1}{2}$ and $\frac{1}{3}$, although the lesser taken but twice, be now much to make 18, yet they both may be parts into 36: therefore look how many times twelve is in 36, & that quotient being multiplied by the numerator over 12, the total shall be put in stead of the Numerator over 12, and for 5 put 15, thus $\frac{15}{12}$. So likewise look how often is 18 in 36, because it is twice, therefore by 2 multiply 7, which is over 18, and it will be 14: set that for the Numerator, and in stead of 18 put 36. and then your fractions reduced stand thus $\frac{14}{36}$ and $\frac{15}{36}$ in stead of $\frac{1}{2}$ and $\frac{1}{3}$.

And if you will prove whether you have wrought well or no, that may be proved by reduction of them againe to their former denominations, which Art shall be taught in the fourth kinde of Reduction, where greater termes of Fractions be reduced into smaller in number

The third variety.

Proofs.



number, but no smaller in proportion. And if in such Reduction the same termes or numbers come againe that were before, then is the worke good, else not.

Scholar. Sir, I heare your words, but I doe not understand many of them: which if it please you, declare.

Master. With a good will, when convenient place serveth, but that must bee in the last fourth kinde of Reduction, which teacheth how to reduce fractions of fractions into one fraction, and so to one denomination.

The second forme of Reduction of fractions into one fraction and Denomination.

When fractions of fractions be proponed, you shall multiply the numerators of each into other, and set the totall for the new numerator, and then multiply all the denominators likewise, and take their totall for the new denominator, and so are they speedily reduced.

Scholar. If that be all, then I understand it already, as by this example I will declare. These bee the fractions, $\frac{1}{2}$ of $\frac{2}{3}$ of $\frac{3}{4}$ of $\frac{4}{5}$ which I would reduce to one denomination, and proper simple fraction:

Therefore begin I with the Numerators and multiply them together, saying, 3 by 2, maketh 6: and 6 by 6, maketh 36, which multiplied by 7, yeeldeth 252: that I set over a line for the Numerator, thus:

Then I multiply the Denominator, 4 by 3 maketh 12, and that by 7 bringeth 84, which multiplied by 9, yeeldeth 756, the new

into Denominator. And so the whole fraction is thus reduced, which is too hard a fraction for me to understand yet.

Master. You think so, and no marvell, but anon you shall learne to judge it easily, for this fraction is no more indeed then $\frac{1}{9}$, although it bee in greater termes, and therefore more stranger and more obscure.

And this sufficeth for this Reduction, save that I will shew you by a figure of measure the just rate and reason of this kinde of fractions, and also the due understanding of their Reduction.

The entire measure parted into 9.

| | | | | | | | | |
|---|---|---|---------------|---------------|---|---|---------------|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | $\frac{8}{2}$ | |
| 1 | 2 | 3 | | | | | | |
| 1 | 2 | 3 | 4 | $\frac{5}{2}$ | | | | |
| 1 | 2 | 3 | $\frac{4}{2}$ | | | | | |

Here you see the longest measure, (which standeth for the whole and entire quantity) first parted into 9 divisions, whereof 7 are severed by the second measure: and thereof againe are parted out 6, and that 6 being divided into three parts, two of them are parted by the fourth measure, of which fourth measure being divided into four parts, the lowest measure

measure doth containe $\frac{1}{2}$, so that the same must bee named, not $\frac{1}{2}$ of the whole measure, but indeed is $\frac{1}{2}$ of $\frac{1}{2}$ of $\frac{1}{2}$.

Scholar. This example is so sensible, that I cannot choose but see it. And furthermore see also, that the same fraction is equall to $\frac{1}{4}$ of the entire measure, as the lines which run up and down do expressely set forth. Also I see here that $\frac{1}{2}$ of $\frac{1}{2}$ is equall to $\frac{1}{4}$. And further yet, that $\frac{1}{2}$ of $\frac{1}{4}$ is equall to $\frac{1}{8}$.

Master. I am glad that you see it so well, not doubting but you will gather greater light of knowledge hereby.

The third
forme of
Reduction
of improp-
er fracti-
ons.

But now it is time that wee come to the third forme of Reduction, which teacheth of improper Fractions, that is to say, mixt numbers of unites and fractions although they appear like fractions, as this $25\frac{1}{2}$, which doth conclude 25 unites wholly, and $\frac{1}{2}$ over. Wherefore first you shall know them, by that the numerator is greater then the denominator.

Scholar. Indeed Sir, that appeareth reasonable, that if the Numerator do expresse more parts to be taken of any unite, then the Denominator doth signifie that unite to be divided into, it must needs follooth, that such a fraction importeth more then the whole, that is to say, the whole with certaine parts over: but what Reduction is there to it?

Two sever-
all waies
in this Re-
duction,

Master. There be two severall kindes of Reduction, concerning such fractions. Some

times it shall bee needfull to convert these Fractions into unites, and the proper Fraction, that will remaine. And sometimes contrariwise, it shall bee meet to reduce mixt numbers, that is, unites writen with Fractions, into the forme of one simple Fraction, and so be there two wayes.

Scholar. What is the meane of the first way, to turn improper fractions into unites with their proper fractions?

Master. That is thus; Your Numerator being greater then the denominator, must be divided by the same denominator, and the quotient thereof expresseth the unites: the remainder shall bee put for the Numerator of the fraction that resteth, and the Denominator must bee the same that was before.

Scholar. For example, I take $\frac{17}{5}$, and dividing 17 by 5, the quotient will be 3, and there will remaine 2.

Master. That you must write thus, $3\frac{2}{5}$, where (you see) I have written 3 without any line, as entire numbers ought to bee written, and the 2 that remained, I have set over the former Denominator, with a line, as a proper fraction. And this number doth signifie nely three unites, and $\frac{2}{5}$ of one.

Scholar. When it I would by unites here understand Crownes, so it were 3 Crownes, and $\frac{2}{5}$ that is 2 s.

Master. Even so, and therefore $\frac{2}{5}$ did signifie the same: But this happeneth sometimes

The fifth way. Reduc-
tion of
improper
fractions
into
unites,
and
their
proper
fractions.

that when the Reduction is so wrought, there remaineth nothing: And then it is not a mixed number, but a simple intire number, represented like a fraction.

The second way.

Scholar. As 4 will make 3 just, and 2 will make even 6. This I will remember. But now, what is the second forme of Reduction that you speake of to these sorts of fractions?

Reduction of whole numbers either alone, or joyned with fractions into improper fractions.

Master. Whensoever you have any of these two sorts of numbers, that is to say, whole numbers without fractions, or whole numbers with fractions, and you would turne them into the forme of a fraction, you must multiply the whole number by that denominator which you will have to remain still, and to the totall thereof adde the Numerator, which you have already, and all that shall you set for the new Numerator, keeping still the former Denominator: As if you have $6\frac{1}{4}$ which you would convert into an improper fraction, you must multiply 6 by 4, whereof cometh 24, and thereto adde the numerator, which is 1, and so have you 25 for the numerator, & 4 stil for the denominator.

Scholar. Then is $6\frac{1}{4}$ equall to $6\frac{1}{4}$?

Note.

Master. Even just, and so backward (as appeareth by the former Reduction) $6\frac{1}{4}$ maketh 7. And thus one of their reductions may be the prooofe of the other worke.

Scholar. This I perceiue: But now if you would turn whole numbers without fractions into any fractions, I see not how that may be done, because there is no denominator to make the multiplication by.

Master.

Master. That is well marked: but this you know, that no man intendeth to turne any whole number into a fraction, but he hath in his minde that denominator by which the multiplication must be made: so; the p[ro]cess whereof I set down 7, which is a whole number. And if you will have this number converted into any certain fraction, will mee to doe it.

Scholar. I may you reduce 7 into a Fraction.

Master. When you care not what the Fraction be, so it be some Fraction.

Scholar. No, I passe not for the sort of the Fraction.

Master. Then how can you thinke that you require me to doe any thing certaine, when you leave me to doe as I list? And seeing you stand at that stay, whether thinke you that I must first intend in mind what Fraction I will make of it before I can do it indeed?

Scholar. Else you should do ignorantly.

Master. Then will I limit my selfe (seeing you will not) to turne it into quarters. And therefore I multiply 7 by 4 (which is the denomination by quarters) and there amounteth 28 to be set for the numerator, and the 4 must be set for the denominator, and the Fraction will be thus $\frac{28}{4}$.

Scholar. Indeed I percieve this to be reasonable, for without much triall I understand that $\frac{28}{4}$ of any thing doth make 7. And so then

If I would turne 8 into 5 parts, it will make
 40 which is all one with 8: for 8 Crowns turn-
 ned into 5 parts, (that is, into shillings) will
 make 40 shillings, that is, $\frac{40}{5}$ of a Crown.

The fourth
 forme of
 Reduction

Master. Seeing you understand now these three
 kinde of Reduction, I will declare unto you the
 fourth kinde, that is, when fractions be written in
 greater termes then they need, how they may be
 brought to lesser terms.

Scholar. To write any thing in greater
 terms then needeth, seemeth to be a fault, and
 to this Rule seemeth to amend that fault.

Master. It were a fault to doe any thing
 without need, which after must be redressed:
 but in this case it is not so, neither did I say
 absolutely (as you doe) that it needeth not to
 expresse those fractions in so great terms, but
 that the fractions doe not need. I meant to
 their valne, to be understood: but yet it may be
 needfull for the sake of these works, to doe so
 they be applied: as for example: In the first
 kinde of Reduction this was your owne ex-
 ample, $\frac{1}{2}$ and $\frac{1}{3}$, which when you would re-
 duce, you were faine to turne them first into
 one denomination, and so appeared they thus:
 $\frac{2}{6}$ and $\frac{2}{6}$, where the fractions for their owne
 understanding needed not to be turned out of
 smaller termes into greater, but yet the easiness
 of working needed it.

Scholar. Sir, I understand now, not on-
 ly the difference of this need (for the fracti-
 ons might better be understood as fractions
 severall

for all such in his name, when they were in
 lesser terms, although they could not so well
 be reduced: but also I understand what you
 mean by greater terms and lesser terms, where-
 of before I was in doubt: for I see you call
 the Numerator and Denominator, the terms of
 the fraction.

Terms of
 fractions.

Master: I am glad you understand it so well:
 now when then you would reduce any fractions (be-
 cause they may best be done when the terms are
 smallest) you shall reduce them to the smallest that
 you can, which thing you may do thus: Divide the
 greatest of any such two terms by the lesser, and if
 any thing remain by that remainder divide the last
 divisor: not if any thing remain yet, by that di-
 vider the first divisor, so still divide the reman-
 der of the last division) and so continue still till
 nothing do remain in the division: and then make
 your last divisor for it the number that will ease
 your fraction: if you divide both the nu-
 merator and the denominator by the same number
 and put for the numerator the quotient of his di-
 vision, and for the denominator his quotient;
 that will ease his division.

Scholar: I take for example $\frac{96}{18}$, and because
 96 is the greatest number, I divide it by 18,
 and the quotient is 5, and there resteth 6, what
 shall I do with this quotient?

Master: Nothing in this worke, but note
 seeing there remaineth somewhat, by that re-
 mainer must you divide the last Divisor.

Scholar: If I shall divide 18, (which was
 the

the last Divisor by 6, that was the remainder
so is the quotient 3, and nothing resteth.

Master. As for the Quotient, I must have
yet: but because there doth remaine nothing
therefore is 6 (which was your last Divisor)
that number by which you may reduce the
Fraction proposed.

Scholar. When as you taught mee, I must
divide the Numerator 18 by 6, and the quoti-
ent is 3, which I must put for the
Numerator over a line, thus:

And then by the said 6 must I di-
vide also the Denominator 96, and the Quo-
tient will be 16, which I must take for the
Denominator, and so is the Fraction $\frac{3}{16}$. And
some thinketh this rule doth prove the works
of the first Reduction.

Master. That is true, if the first Reduction
were made of fractions into their least termes,
and else not, without some help, as the second
number in that place will declare.

Scholar. The second number was 6, which
was turned into 64 by that Rule. Now if I
shall by this Rule reduce it againe into the
least termes, I must divide 96 by 64, and there
remaineth 32, wherefore I must take that 32
for the Divisor, to reduce the said Fraction.
Then do you divide 64 by 32, and the quoti-
ent is 2, which I set for my Numerator.
Again, I divide 96 by 32, and the quotient
will be 3, and so I have but $\frac{2}{3}$.

Master. Pause not at the matter, for you
have

have some small wrong: but you think you have not the fraction that you looked for, that is, $\frac{1}{2}$; yet have you one equal to it; as by the parts of a shilling you may prove.

Scholar. *Writhe it is, to each of them writte bying forty 8 pence* that is, and; and; be all three equal. *I perceive that be- cause; how not to write in the least termes that it might be; therefore this Reduction brought forthout it, but that other which is written in the last termes. I do understand this Rule well. But is there any other way to write this Reduction?*

Master. Yes, but first note this, that if you finde no such Divisor, to reduce the fraction to your come to it, because one doth make no Division, therefore that fraction is already in his least termes, as by $\frac{1}{2}$; you may prove, and so $\frac{1}{3}$; and many other like.

Another way to work this Reduction

But now for your better aid to find the due proportion in least termes, with more ease for a young learner, you shall mediate or take the half of the numerator, and also of the denominator as long as you may upon a line, alwaies parting them with a right down dash of your Pen as you work, which may easily be done, if the numbers be even: as 2. 468, or 10, but if they be odd, (though it be but one of them) then must you abbreviate them by 3. 5. 7. or 9, &c.

Note that to mediate any number is to divide by two.

And because examples do most instruct, I have here set downe the manner of two or three, whose last number at the end of the line shew.

between the least terms, or valuation of the fractions. As for example, I would reduce $\frac{1}{2}$ into his least terms, or value, whereupon I should say, with a long line between them, thus:

$$288 \mid 1 \mid 288 \mid 288 \mid 144 \mid 144 \mid 72 \mid 72 \mid 36 \mid 36 \mid 18 \mid 18 \mid 9 \mid 9 \mid 4 \mid 4 \mid 2 \mid 2 \mid 1$$

And because both the Numerator and the Denominator still in excess, and of these the same be abridged by 2, at 4, at 8, at 16, at 32, at 64, at 128, at 256, at 512, at 1024, at 2048, at 4096, at 8192, at 16384, at 32768, at 65536, at 131072, at 262144, at 524288, at 1048576, at 2097152, at 4194304, at 8388608, at 16777216, at 33554432, at 67108864, at 134217728, at 268435456, at 536870912, at 1073741824, at 2147483648, at 4294967296, at 8589934592, at 17179869184, at 34359738368, at 68719476736, at 137438953472, at 274877906944, at 549755813888, at 1099511627776, at 2199023255552, at 4398046511104, at 8796093022208, at 17592186044416, at 35184372088832, at 70368744177664, at 140737488355328, at 281474976710656, at 562949953421312, at 1125899906842624, at 2251799813685248, at 4503599627370496, at 9007199254740992, at 18014398509481984, at 36028797018963968, at 72057594037927936, at 144115188075855872, at 288230376151711744, at 576460752303423488, at 1152921504606846976, at 2305843009213693952, at 4611686018427387904, at 9223372036854775808, at 18446744073709551616, at 36893488147419103232, at 73786976294838206464, at 147573952589676412928, at 295147905179352825856, at 590295810358705651712, at 1180591620717411303424, at 2361183241434822606848, at 4722366482869645213696, at 9444732965739290427392, at 18889465931478580854784, at 37778931862957161709568, at 75557863725914323419136, at 151115727451828646838272, at 302231454903657293676544, at 604462909807314587353088, at 1208925819614629174706176, at 2417851639229258349412352, at 4835703278458516698824704, at 9671406556917033397649408, at 19342813113834066795298816, at 38685626227668133590597632, at 77371252455336267181195264, at 154742504910672534362390528, at 309485009821345068724781056, at 618970019642690137449562112, at 1237940039285380274899124224, at 2475880078570760549798248448, at 4951760157141521099596496896, at 9903520314283042199192993792, at 19807040628566084398385987584, at 39614081257132168796771975168, at 79228162514264337593543950336, at 158456325028528675187087900672, at 316912650057057350374175801344, at 633825300114114700748351602688, at 1267650600228229401496703205376, at 2535301200456458802993406410752, at 5070602400912917605986812821504, at 10141204801825835211973625643008, at 20282409603651670423947251286016, at 40564819207303340847894502572032, at 81129638414606681695789005144064, at 162259276829213363391578010288128, at 324518553658426726783156020576256, at 649037107316853453566312041152512, at 1298074214633706907132624082305024, at 2596148429267413814265248164610048, at 5192296858534827628530496329220096, at 10384593717069655257060992658440192, at 20769187434139310514121985316880384, at 41538374868278621028243970633760768, at 83076749736557242056487941267521536, at 166153499473114484112975882535043072, at 332306998946228968225951765070086144, at 664613997892457936451903530140172288, at 1329227995784915872903807060280344576, at 2658455991569831745807614120560689152, at 5316911983139663491615228241121378304, at 10633823966279326983230456482242756608, at 21267647932558653966460912964485513216, at 42535295865117307932921825928971026432, at 85070591730234615865843651857942052864, at 170141183460469231731687303715884105728, at 340282366920938463463374607431768211456, at 680564733841876926926749214863536422912, at 1361129467683753853853498429727072845824, at 2722258935367507707706996859454145691648, at 5444517870735015415413993718908291383296, at 10889035741470030830827987437816582766592, at 21778071482940061661655974875633165533184, at 43556142965880123323311949751266331066368, at 87112285931760246646623899502532662132736, at 174224571863520493293247799005065324265472, at 348449143727040986586495598010130648530944, at 696898287454081973172991196020261297061888, at 1393796574908163946345982392040522594123776, at 2787593149816327892691964784081045188247552, at 5575186299632655785383929568162090376495104, at 11150372599265311570767859136324180752990208, at 22300745198530623141535718272648361505980416, at 44601490397061246283071436545296723011960832, at 89202980794122492566142873090593446023921664, at 178405961588244985132285746181186892047843328, at 356811923176489970264571492362373784095686656, at 713623846352979940529142984724747568191373312, at 1427247692705959881058285969449495136382746624, at 2854495385411919762116571938898990272765493248, at 5708990770823839524233143877797980545530986496, at 11417981541647679048466287755595961091061972992, at 22835963083295358096932575511191922182123945984, at 45671926166590716193865151022383844364247891968, at 91343852333181432387730302044767688728495783936, at 182687704666362864775460604089535377456991567872, at 365375409332725729550921208179070754913983135744, at 730750818665451459101842416358141509827966271488, at 1461501637330902918203684832716283019655932542976, at 2923003274661805836407369665432566039311865085952, at 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Scholar: Sir, I thank you much. The is
very easy and good for a young learner.

Miller: And it is, but yet notwithstanding, if you can without that division by memory give the greatest number that may divide equally both termes by your fraction proposed, then need you not in all that division, as in this fraction $\frac{1}{2}$. I see that 2 is the greatest number that can divide them both: and therefore without any worke, or memory onely, I turne that into $\frac{1}{2}$; but this ability in knowledge is got by exercise.

Let one other way of easie Reduction in this kind be shew'd, when your fraction hath any cyphers in the first places of both termes, then may you by cutting away the Cypher, make a facile reduction as thus: $\frac{20}{75}$ here take away the cyphers, and it will be $\frac{2}{7}$, which is the same in value with $\frac{20}{75}$.


Scholar, And is it I have ... it will be
Master, You are detoured, for you take a
your male cyphers from the Numerator then
you too from the Denominator, which you
must not do.

Scholar. I confesse my fault, which came
of too much haite, I was more gladder of the
Rul

Rule then telle in what it is: but now I will stand it I trust.

Master. When may I goe in hand with the fifth or last kind of Reduction, which teacheth how to turne any fraction proposed into any other Denomination that you like, or into any part of common comes weights, or measures, or such like.

The fifth
kind of
Reduction


To reduce
fractions
to a deno-
mination
appointed.

For declaration whereof, first you shall mark whether your fraction be a simple fraction, either else a fraction of sundry parts, I meane of more termes then two. And if your fraction be a fraction of fractions, or otherwise compound, you must reduce it to one simple fraction: And then mark well the Denomination of that other fraction into which you would turne this: for by that denominator you must multiply the numerator of your first fraction, and the totall product thereof shall you divide by the denominator of your first fraction, and that quotient shall be the numerator of the denominator proposed; as for example, I have this fraction $\frac{1}{5}$, which I would turne into ten parts: therefore I multiply this 10 by 3, that is the numerator of my fraction, and there ariseth 30, which I divide by 5, and the quotient is 6, which must be the numerator to 10, and so $\frac{6}{10}$ will be $\frac{3}{5}$.

Scholar. This is easie enough to doe.

Master. When shall you see another example of the same fraction that is not so easie: as if I would turne $\frac{1}{5}$ into 8 parts, prove you that worke.

Scholar. I must multiply 8 by 3, and there amount.

amounteth 24 , which I divide by 5 , and the quotient is 4 , then is the new fraction $\frac{4}{5}$.

Master. And see you nothing doubtful in this work?

Scholar. I see that when 24 was divided by 5 , there remained 4 , which I did not passe of, because ye spake nothing of any remainder but onely of the quotient.

Master. By likelihood you remember what I said to you in Division of whole numbers, that you should not passe of the remainder there but onely note it as a summe that could not be divided without knowledge of Fractions. Wherefore now make this, that in all divisions of whole numbers, when there is any remainder, you shall set it over a line as a Numerator, and set the Divisor for the Denominator, and that Fraction doth make the Division compleat, and is part of the quotient. As if I would divide 48 by 5 , the quotient will be $9\frac{3}{5}$: so in your former work when 24 was divided by 5 , the quotient should be $4\frac{4}{5}$, and so the new fraction should be thus, $\frac{4}{5}$ and $\frac{4}{5}$ of $\frac{4}{5}$, that is, $\frac{4}{5}$ of the entire number, and $\frac{4}{5}$ of $\frac{4}{5}$ part of any thing, which you may prove by example of some Coyne.

Scholar. When I take a Croone, whose value is 3 s. Now if I would prove whether the 3 s. be $\frac{4}{5}$ and $\frac{4}{5}$ of $\frac{4}{5}$, I shall have a cumbersome work to doe.

Master. Indeed for whole pence, your example is a little troublesome: yet turning the

croon

Scholar. I want to know how to add fractions, and the Master says, that is the first thing to be done, and the second is to reduce them to one denomination.

Master. What is 12 shillings, and one penny, part of a shilling, that is 4 pence, as by the same Rule you may prove. And this for this time shall suffice for Reduction. And now I will proceed to Addition.

Addition.



Whosoever you have any Fractions to be added, you must consider whether they be of one denomination or not, and if they be of one denomination, then adde the numerators together, and set that that amounteth for the numerator over the common denominator, and so have you done. The reason is, because that such differ little in Addition or Subtraction from the worke of vulgar denominations, Where the denominators be of the number, as 3 pence and 5 pence, make 8 pence, where the denomination is not altered. But if the fractions be not of one denomination, or any of them be mixt of whole numbers and fractions, then must you first reduce them to one denomination, and after adde them. And if they be many, then adde first two of them, and so the summe that doth amount of the Addition, and the third, and then the fourth, &c. if you have so many.

Addition of fractions of one denomination.

Scholar.

Scholar. This seemeth well enough, now that I have already learned to reduce, without which I could never have brought this: And therefore now I see good reason why you did place Reduction before Addition.

Master. It is well considered; but yet not to express your understanding of it by an example.

Scholar. When would I adde first $\frac{7}{4}$ with $\frac{5}{4}$, and because the Denominators are like (and so needeth no reduction) I adde 7 to 5, which maketh 12, and then is my summe $\frac{12}{4}$ that is, in smaller numbers being abbreviated.

To adde
fractions
of divers
denomi-
nations.

And if I have many numbers to be added, as here $\frac{1}{2} + \frac{1}{3} + \frac{1}{4}$, first I must reduce them (because they have divers denominators) into one Denomination, and then they will be thus, $\frac{2}{4} + \frac{1}{3} + \frac{1}{4}$, or in lesser terms $\frac{1}{2} + \frac{1}{3} + \frac{1}{4}$; which by Addition do make $\frac{13}{12}$, that is $1 \frac{1}{12}$.

Master. Now may we go to Subtraction.

Sub-

Subtraction of Fractions.

Subtraction
of fra-
ctions.



Subtraction hath the same pre-
cepts that Addition had, for if
the Denominators be like, then
must you subtract the one Nu-
merator from the other, and the
rest is to be set over the common
Denominator, and so your subtraction is ended:
but and if you have many fractions to be subtra-
cted out of many, then must you reduce them to
one Denomination, and into two severall fracti-
ons, that is, all that must be subtracted into one
fraction, and the residue into another fraction,
and then worke as I said before.

Scholar. For the first example I take $\frac{1}{2}$ to
be subtracted out of $\frac{1}{2}$, and the rest will be
 $\frac{1}{2} - \frac{1}{2} = 0$.

For another example, I take $\frac{1}{2}$ to be sub-
tracted out of $\frac{1}{2}$, which I must reduce, and it
will be thus $\frac{1}{2}$ and $\frac{1}{2}$.

Then do I subtract 24 out of 28; and there
remaineth 4, which I set over the common
Denominator for a Remainder, thus, $\frac{4}{7}$: that
is.

Now for the third example, I take $\frac{1}{2}$ and
 $\frac{1}{3}$ to be subtracted from $\frac{1}{2}$ and $\frac{1}{3}$: and because
these Denominators be others, I doe reduce
them into one denomination thus $\frac{1}{2} = \frac{3}{6}$ and $\frac{1}{3} = \frac{2}{6}$

Then

Then doe I adde the two first, & they make $\frac{1}{2} + \frac{1}{2} = 1$. Also I adde the two last, and they yeeld $\frac{1}{2} + \frac{1}{2} = 1$. Then doe I subtrakt 3040 out of 3408, and there resteth 368, so is the remainder, that is in smaller termes $\frac{1}{2}$. And thus have I done with Subtraction, except you have more to teach me.

Master. Prove one example or more out of fractions of divers denominations.

Scholar. I take the two fractions $\frac{7}{8}$ to be subtracted from $\frac{9}{8}$, which being reduced, will stand thus $\frac{168}{72}$ and $\frac{72}{72}$: Now would I subtrakt 168 out of 72, but I cannot.

The greatest of two fractions.

Master. When may you perceiue that you mistook the fractions: for you can neuer subtrakt the greater out of the lesser, although you may adde, multiply or diuide the greater with the lesser. And albeit that $\frac{7}{8}$ hath both his terms lesser then $\frac{9}{8}$, yet is $\frac{7}{8}$ the lesser fraction: for generally if you multiply the Numerator and the Denominators of two fractions crosswise, that fraction is the greatest of whose numerator cometh the greatest summe, as in this example: 7 multiplied by 24 maketh 168, and 9 being multiplied by 8 yeeldeth but 72, therefore is the first fraction $\frac{7}{8}$ the greatest of these two, so can you not subtrakt it out of a lesser fraction.

But if you would subtrakt a fraction out of a whole number, what should you doe?

Scholar.

Subtraction of Fractions. 297

Scholar. *Ques* I would reduce the whole number into a fraction of the same denomination that my fraction is, and then worke by Subtraction.

Master. So may you doe, but it is much easier, if your fraction be a proper fraction, that is to say, lesse then an unite, to take an unite from the whole number, and then turn it into an improper fraction, and so worke your Subtraction. As if I would subtract $\frac{3}{4}$ from 4, I may take 1 from 4, and turn it into $\frac{4}{4}$, from which I bate $\frac{3}{4}$, there will remaine $\frac{1}{4}$. And if the first fraction be an improper fraction, then may I take so many unites from the whole number, that they may make an improper fraction greater then that first, and then worke by Subtraction. As if there bee proposed $\frac{4}{3}$ to be subtracted from 6, because $\frac{4}{3}$ is more then 3, and not so much as 4, I must take 4 from 6, and turn them into thirds thus $\frac{8}{3}$, then abate $\frac{4}{3}$, and from $\frac{8}{3}$, there resteth $\frac{4}{3}$: so the whole remainder is $2\frac{2}{3}$. Or else you may at your pleasure take $3\frac{1}{3}$, which is $\frac{10}{3}$ from 6 whole: then set 1 under 6, as thus $\frac{6}{1}$: And then to reduce those two fractions into one Denomination, as here appeareth $\frac{6}{1}$ from $\frac{10}{3}$. When $\frac{10}{3}$ from $\frac{6}{1}$ resteth $\frac{8}{3}$, which maketh $2\frac{2}{3}$ your desire. And thus will I make an end of the work of Subtraction of fractions, and proceed to Multiplication.

Multiplication of Fractions.

Multiplication of fractions.



Herefore when any two fractions be proponed to be multiplied together, the Numerator of the one must be multiplied by the Numerator of the other : and the summe that amounteth thereof must be set for a new Numerator : likewise the Denominator of the one must be multiplied by the Denominator of the other, and that that amounteth shall be set for the Denominator, & this new third fraction expresseth the product of the multiplication of the two first fractions proponed, whereof take this example, $\frac{3}{4}$ multiplied by $\frac{5}{12}$ doth make $\frac{15}{48}$.

Scholar. I perceiue then that 3 being the Numerator of the first fraction, is multiplied by 5 being the numerator of the second fraction, whereof amounteth 15, the numerator of the third fraction, and so likewise 5 being the denominator of the first fraction, is multiplied by 12 the denominator of the second fraction, whereof amounteth 60 the new denominator, so that I perceiue how the worke is done, but I doe not perceiue how $\frac{15}{48}$ is greater then $\frac{1}{4}$, for if I shall use my former manner of examination by the parts of some coine, I see that $\frac{1}{4}$ of a Crowne is 36 pence, and $\frac{1}{3}$ of a Crowne is 25 pence, whereof the one multiplied by the other, doth make 900 pence, which is 15 Crownes, but by your Multiplication

lication there amounteth $\frac{1}{2}$, which is but 15 pence, and that is much lesse then any other of both the first fractions.

Master. What difference is between multiplication in whole numbers, and multiplication in broken numbers; that in whole numbers, the sum that amounteth is greater then both the other whereof it came, but in fractions it is contrariwise: for the sum that amounteth is lesser then any of the other two fractions whereof it is produced.

Scholar. I desire much to understand the reason thereof.

Master. Although I purposed to reserve the reasons of works Arithmetick for the perfect Book of Arithmetick, yet I will shew you this because of the strangeness of the work.

For see in whole numbers, that of two numbers being multiplied together, is made the third number, which third number doth beare the same proportion to the number multiplied, that the multiplier doth beare to an unite. And so in fractions the third number which amounteth of multiplication, beareth the same proportion to each of the two first fractions that the other of those two fractions doth beare to an unite.

Scholar. Sir, I understand your words thus: when 40 is multiplied by 12, there doth amount 480, which 480 doth containe 40 so many times in it, as 12 doth containe units, that is to say, twelve times. And so it

appeareth that 40 doth containe twelue 1/3 many times also as 40 doth containe unites: that is 30 times. But now I see not how the third number in this example of Fractions can contain any of the two former (as it happened in whole numbers) seeing it is lesser then either of them.

Master. Do you saydell If you cannot see that thing which is not possible to be seen of any man, how the third number in Multiplication of Fractions should be greater then any of the two former Fractions: but yet this may you see (which I said) that the third number in fractions so multiplied, doth beare the same proportion to any of the two former fractions that the other of those two fractions doth beare to an unite, as in your example, 1 being multiplied by 1/2, doth make 1/2. Now say I that 1/2 doth beare the same proportion to 1 that 1/4 doth beare to an unite, as you may in your own forme of examination by Coine, try the for in an old Angel (which in times past was current for 7 shillings six pence) are 180 halfe pence, which I set for the intire unite, whose parts (according to the fractions aforesaid) are these, for 1/2 set 45 halfe pence, for 1/4 take 108 halfe pence, and for 1/8 put 75 halfe pence. Now doth 45 bear the same proportion to 108, that 75 doth bear to 180, for 45 is 1/4 of 108, and so is 75 also 1/4 of 180.

But these reasons may be better referred till another time, when the knowledg of
pro-

proportions in this order shall be taught; yet in the mean season I will shew you how it cometh to passe, that in fraction the third summe must needs be lesse then any of the other two.

Consider this, that when a fraction is pro- Note
 portioned as in the former example; if it be mul-
 tiplied by more then 1, it will make more
 then one entire number. As if I multiply $\frac{1}{2}$ by
 5, that is to say, if I take it 5 times, it will
 make three entire unites. Example: In a Crown
 $\frac{1}{2}$ of it maketh 3 shillings, which if I take five
 times, it will amount to 15 shillings, that is,
 three entire Crownes; so if I take the same
 $\frac{1}{2}$ but twice, it will yeeld 6 shillings; that is
 one entire Crown, and $\frac{1}{2}$. Now if I take it
 but once, it cannot be more then it was before,
 that is 3 shillings. And if I take it lesse then
 once, it cannot be so much as it was before.
 When seeing that a Fraction is lesse then one,
 if I multiply a fraction by another fraction,
 it followeth that I doe take the first fraction
 lesse then once, and therefore the summe that
 amounteth, must needs be lesse then the first
 Fraction.

Scholar. Sir, I thank you much for this
 reason. And I trust I do perceiue the thing,
 as by example of this same fraction $\frac{1}{2}$, I will ex-
 presse. If I take $\frac{1}{2}$ of a Crown once, that is to
 say, if I multiply $\frac{1}{2}$ by 1, it will be as it was
 before, but 3 shillings; so if I doe multiply it
 by $\frac{1}{2}$, that is, if I take but halfe one time, then

will it be but half so much : Wherofte if I multiply it by 3 that is, if I take but the third part of one, it will yeeld but 12 pence; that is, the third part of the first fraction.

And so to make an end : if I take but the twelfth part of one, that is, if I doe multiply it by 12 it will yeeld but the twelfth part of the first fraction, which is but 3 pence. And it followeth, that if I make three pence, then I must needs make five times so much, that is, 15 pence, which was the summe that hath given the occasion of all this doubt.

Master. When I perceiue you haue sufficient understanding in this sort of multiplication for this time, wherfore I will proceed to the rest.

To multiply a whole number into a fraction.

In multiplication it happeneth sometime, that there be whole numbers to be multiplied with fractions, and may bee in two sorts : for either the whole number is severall from the fraction, and is the multipliyer, or else the whole number is joyned with one, or both of the Fractions, and so maketh a mixt number thereof. If it be in the first sort, then needeth there no reduction, but onely multiply the Numerator of the fraction by that whole number, and the totall thereof set for the new numerator.

Scholar. I understand you thus. If I have 6 to be multiplied by 16, then must I multiply that 16 with 6, which is the numerator, wherof commeth 96, and that must I set for the new Numerator : keeping still 13

for the denominator, and so the fraction will be; that is $\frac{1}{2}$.

Master. And in this sort of work you may abridge the labour thus. If it happen the denominator to be such a number as may evenly be divided by the said whole number proposed, then divide it thereby, and set the quotient of that division for the former denominator, but reserve still the Numerator, and so is the multiplication ended.

Scholar. When I sawe this example $\frac{1}{2}$ to be multiplied by 5, and because 5 will justly divide 20, therefore I take the quotient of that division which is 4, and set instead of 20, and so the fraction will be $\frac{1}{4}$ that is $\frac{1}{4}$.

Master. Which is all one with $\frac{1}{4}$ that would have followed of the other sort of work.

Scholar. I perceiue it very well.

Master. Now then for the other sort, where the number is mixt, take this way: first to reduce the said whole number and fraction into one improper fraction (as I shewed you in Reduction) and then multiply them together, as if they were proper fractions.

How to multiply mixt numbers

Scholar. $13\frac{3}{4}$ being set to be multiplied by $\frac{1}{2}$ first I must reduce the mixt number, as in this example appeareth, by multiplying 13 by 5, and $13\frac{3}{4}$ that maketh 65, whereof I $\frac{3}{4}$ by $\frac{1}{2}$ must adde the numerator 3,

and

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and so the fraction will be $\frac{1}{2}$, which two Fractions now I shall multiply after the accustomed forme, and it will be $\frac{1}{4}$.

Master. You have done well: And so may you see, that although most part of the formes of Multiplication may be wrought without Reduction, yet some cannot, as namely, mixed numbers.

And yet one note more I will tell you of Multiplication before we leave it: That is, whensoever you would multiply any Fraction by 2, which commonly is called Duplation, you may do it not only by doubling the Numerator, but also by paring the Denominator into half, if it be even.

Scholar. Then if I would double $\frac{1}{2}$, I may chuse whether I will make it $\frac{2}{2}$: or else $\frac{1}{1}$. And indeed I see that is all one, but that the dividing of the Denominator seemeth the better way to make smaller termes of the Fraction, and so they shall need the lesse Reduction.

Master. It is so: and now I shall not need to tell you that Multiplication is proved by Division, and Division likewise by multiplication: but the like work that I shewed you in Multiplication, will I shew you in Division also.

Divi-

Division of Fractions.



Hensoever two fractions be Division
proposed, that one should of Fracti-
be divided by the other, I ons.

must set down first the
fraction that shall be di-
vided (which is called the
Dividend) & then after it

the other which is the Divisor. Then shall I multi-
ply the Numerator of the Dividend by the De-
nominator of the Divisor, and that which a-
mounteth I must put for a new Numerator. Again
I shall multiply the Denominator of the Dividend
by the Numerator of the Divisor, and the number
that amounteth thereof I must put for the new
Denominator. And this thing Fraction is the quo-
tient of the said division.

Scholar. This seemeth easie in forme, as for
example thus: If I would divide $\frac{5}{6}$ by $\frac{3}{8}$, first
I multiply 5, (being the Numerator of the Di-
vidend) by 8, which is the Denominator of the
Divisor, and thereof riseth 40; then
I multiply 8 (being the Denomi-
nator of the dividend) by 3, being
the Numerator in the divisor, and
so riseth 16, the which I must
make a third fraction thus $\frac{40}{16}$.

Master. As seemeth you are quicker in un-
derstanding now, then you were when I
taught

taught you the Art of whole numbers, but that is no marvell: for the more knowledge that a man getteth, the readier shall he finde his wit, and quicker in understanding: but yet of two things I will admonish you, which you might have obserued here for the ease of work and lightnesse of understanding, the nature of the Quotient.

Whensoeuer you diuide one Fraction by another, either they be both equall together, or else the one is greater then the other: if they be equall, their quotient shall be such, that the Numerator and the Denominator of it shall be equall also. And if the two first fractions bee inequall, their quotient shall declare the same by the inequality of the Numerator, and denominator, as in these examples following shall appeare.

First, if equall fractions $\frac{1}{2}$ and $\frac{1}{2}$ be equall together, and if the one be diuided by the other, the quotient will be $\frac{2}{2}$, as you may perceiue by that Rule aforesaid.

Now in the inequall fractions, as $\frac{3}{2}$ and $\frac{1}{2}$, the quotient will be $\frac{3}{1}$, where the numerator is greater then the denominator.

Scholar. I see it is so: but I see not the reason why it should be so.

Master. The reason is this: when any fraction is diuided by another, the quotient declareth what proportion the diuidend beareth to the diuisor. So $\frac{3}{2}$ diuided by $\frac{1}{2}$, maketh 2, which must be sounded, not 2, but twice

Note how
to know
the pro-
portion
between
two num-
bers.

twice, declaring that $\frac{1}{2}$ is contained twice

in $\frac{1}{2}$. And note this, that the Numerator in the quotient representeth the Dividend, and the Denominator representeth the Divisor. And this is alwayes true, whether the greater fraction be divided by the lesser, or the lesser by the greater. But this proportion will not be exactly knowne, till you have learned the Art of proportions: notwithstanding somewhat of it I have declared in the Rule of Reduction. But now for the easie remembrance of the quotient in division, as soone as you have set downe your two fractions the one against the other, then make a straighe line for the quotient: and as soone as you have multiplyed the Numerator of the Dividend, by the Denominator of the Divisor, set the number that amounteth over the said line, and then multiply the other two numbers, and set theire totall under the same line.

Scholar. I perceiue you would not have me trust to memory till I were better expert, lest oftentimes I happen by misse remembrance to be abused. This example I take for that declaration.

If I would divide $\frac{1}{2}$ by $\frac{1}{3}$ I must set the numbers one against the other.

(as here doth appeare) and then make another line for the quotient in some good

$$\begin{array}{r} \frac{2}{3} \text{ by } \frac{3}{4} \\ \hline \end{array}$$

distance,

distance where I may set the numbers of the quotient, as soon as any of them is multiplied: So then as soon as I have multiplied $\frac{1}{2}$ by 4, which maketh 8, I shall set that 8 over that line, thus: And then multiply 3 by 3, which yeeldeth 9: and that 9 shall be set under the same line, and then with the whole quotient appeare thus: whereby it appeareth (as I remember your words) that $\frac{1}{2}$ is in proportion to $\frac{1}{3}$ as 8 is to 9, but how may I perceiue that?

Master. Although you might better perceiue it by the Rule of Reduction, yet this example may be declared in common coines, as in a common shilling of 12 pence, of which $\frac{1}{2}$ maketh 8 pence, and $\frac{1}{3}$ doth make 9 pence, and so you may easily see that those proportions doe agree. And if you had taken this example before, when you took the example of $\frac{1}{2}$ and $\frac{1}{3}$, your quotient should appeare (as this doth) more easie to understand: whereas that Quotient being $\frac{1}{2}$, is not an easie proportion for you to perceiue, being yet little acquainted with proportions.

Scholar. If there be whole numbers to be diuided by a Fraction, how shall I performe it?

To diuide
a whole
number by
a fraction.

Master. When any whole number shall be diuided by a Fraction, you must multiply the said whole number with the Denominator of the Fraction, and set the totall thereof for the new Numerator, and for the Denominator

see

for the Numerator of the fraction.

Scholar. When 20 divided by 4, it will make 5, as here ap-
peareth 5.

Master. Even so: but if you would divide the Fraction by the whole number, then multiply the Denominator by the same whole number, and set the totall for the Denominator, without changing the Numerator.

To divide the fraction by the whole number.

Scholar. When to divide $\frac{20}{23}$ by 4, it will be $\frac{5}{23}$, as here
appeareth $\frac{20}{23}$ by 4 in this ex-
ample $\frac{20}{23}$.

Master. You say well. And by the same ex-
ample you give me cause to remember ano-
ther briefe way to doe the same: for if you
but divided the said Numerator by 4, and set
the quotient for the numerator, keeping still
the old denominator, it would have been not
onely as well done, but also in a fraction of
lesser termes.

Another
briefe way.

Scholar. I guesse it to be even so, by a like
work that you taught me in Multiplication:
And for proove thereof $\frac{20}{23}$ being the dividend,
and 4 the divisor, I divided the Numerator 20
by 4, and the quotient is 5, which I set for
20 over 23, thus $\frac{5}{23}$: and I see that it is all
one with $\frac{20}{23}$, as by dividing or abbreviating
both these termes by 4, and so reducing them
to

to their least Denomination, I may easily
probe, as appeareth by this example, $\frac{1}{2} \div \frac{1}{4}$.

Master. You can tell it well. And if there
be mixt numbers, (either one or both) you must
first reduce that mixt number into an improp-
per fraction, & then work as you have learned.

Scholar. That was sufficiently taught in
Multiplication. Therefore I pray you goe for-
ward to some other thing.

Master. Then take this note yet for Divi-
sion: if the Denominators be like, then divide
the numerators as it were in whole numbers,
and the quotient, whether it be fraction, whole
number, or mixt, is a good quotient for that
division. And generally, if one of the numera-
tors may justly divide the other by that quo-
tient, multiply the Denominator of the lesser
Numerator, and set it that doth amount in the
roome of the same denominator, and then for a
numerator to it, set the Denominator of the
other fraction.

Scholar. When if I would divide $\frac{1}{2}$ by $\frac{1}{4}$ I
see that 3 will divide 12, and the quotient will
be 4, by which I must multiply the other 4,
that is the Denominator under 3, and then it
is 16, which is set for the denominator 4, and
over it in stead of 3 I must set 17 the other
Denominator, & so is it thus $\frac{1}{2} \div \frac{1}{4} = \frac{17}{16}$.

Master. And so is $\frac{1}{2}$ in stead of $\frac{1}{4}$
of $\frac{1}{2}$, which would have risen by $\frac{3}{4}$
the common work as here ap-
peareth, $\frac{1}{2} \div \frac{1}{4} = \frac{3}{4}$.

And

And for the Mediation which is to divide by
2) Mark this if the Numerator be a prime num-
ber fear to divide of it in his place without the di-
visor, and so have you done: and if the Numerator
be not even, then double the Denominator
3) Scholary What is, if I would mediate? I
may write the quotient, and if I would me-
diate, I shall make it, or I shall proceed the
Myser. And thus will I make an end of the
works of common fractions for this time, not
doubting but you can apply them both to the
Rule of Proportion, and also to the Golden
Rule, without any other teaching then you
have learned before, which might seem tedious
to repeat, in regard you have sufficient know-
ledge in Reduction, Addition, Subtraction,
Multiplication, and Division. And therefore
will I go in hand with the Rule of proporti-
on, or Golden Rule, which now will appear
easier enough.

The Golden Rule direct in Fractions

Herefore as touching the Golden Rule for the placing of the number, proponed in the question, whereby to finde the fourth, and for the forme of their worke, with other like notes, I referre you to that ready learned.

But

Note this
for a gene-
rall Rule,

But this rule is for working by fractions shall you note, that if you have numbers be fractions, for example work with fractions, multiply the numerator of the first number in the question, by the denominator of the second: And all that again multiply by the denominator of the third number, and the totall thereof shall you keep for to be the divisor. Then multiply the denominator of the first number by the numerator of the second, and the whole thereof by the numerator of the third, and the totall thereof shall be your dividend.

Now divide this dividend by the divisor which you found out before, and that number shall be the fourth number of the question which you seek for, as in this example.

A question
of velvet.

If $\frac{1}{2}$ of a yard of velvet cost $\frac{1}{2}$ of a Sovereign, esteemed at 20 shillings, what shall $\frac{1}{2}$ cost?

Scholar, If it please you to let me write the answer, I would first place these three numbers as I learned in the whole numbers, thus:

And then according to your new rule, I must multiply 3, being numerator in the first number, by 3 the denominator of the second, and thereto cometh 9, which I multiply again by 6, the denominator of the third number, and so have I 54, which I keep for a divisor. Then multiply I 4 the denominator of the first, by 2 the numerator of the second, and there ariseth 8, which againe I multiply

but the numerator of the third, and it maketh
 40. Then must I divide 40 by 4
 and it will be 10, that is 10 in silver
 terms; and then the figure will be 10.
 And thus: 40 is 10 times more than 4.
 But what that is in money, I cannot tell,
 except I shall worke it by Reduction, as you
 taught mee.

Maker. It maketh not melle, you may reduce
 it when you list, but it were disorderly done
 here, to mingle diverse worke together, where
 we do not seeke the value of the thing in com-
 mon money, but in apt number, which you
 have well done: and therefore will I get
 into you another if the way of exercise in
 worke, how you may change your three frac-
 tions into three whole numbers, by which you
 shall worke, as if the question were proposed
 in whole numbers. The first number you shall
 finde as I taught you: now to finde the divi-
 sor of the second number, take the numerator
 for the second fraction: and for the third num-
 ber, take that that resulteth of the multiplicati-
 on of the denominator of the first by the nume-
 rator of the third; and then worke your que-
 stion.

Scholar. For example hereof, let the questi-
 on be: of a pound weight of silver, be worth
 of a Sovereigne, what is of a pound
 weight worth.

A question
 of silver.

For the answer, first I place the
 fractions in order, thus:

2

Then

When to turne these fractions into whole numbers, I multiply 11, which is the numerator of the first by 4 (the denominator of the second) and there cometh 44, which I multiply by 2 the denominator of the third, and so amounteth 88, which I set for the divisor in the first place. Then in the second place I set 12, which is the numerator of the second fraction, and in the third place I set the sum that amounteth of 12 being the denominator of the first number, multiplied by one, being numerator in the third of 88. **Z** Now stand as here posted. Then to work it forth, I multiply 22 by 12, and there amounteth 144, which I divide by 88, and the quotient will be 1 $\frac{4}{11}$, or in lesser terms, 1 $\frac{4}{11}$, and then the figures will stand thus. **Z** Master. These two formes now you understand well enough, and as for any other at this time I will not repeat, onely this shall you mark for the proof of this Rule; whether you work well wrought or no. Multiply the first number by the fourth, and note what amounteth; then multiply the second by the third, and mark what amounteth also. Now if those two numbers so amounting be equall, then is your work well done; else you have erred. And this shall suffice for the former Rule.

The proof
of the gol-
den Rule.

noisup
will to

The Backer Rule, or Re-

soluer Rule on Fractions.

U^e in the Backer Rule, this shall
 you note for ease of work, that
 you multiply the Numerator of the
 first by the Numerator of the se-
 cond, and the whole thereof by the

The bac-
 ker Rule
 in Fracti-
 ons.

denominator of the third, and that amounteth
 thereof shall be the dividend. Then multiply
 the denominator of the first by the denomina-
 tor of the second, and that whole by the nume-
 rator of the third, and that that ariseth there-
 of, shall be the divisor. Example of this.

Note this
 also for a
 generall
 Rule.

I did lend my friend $\frac{1}{2}$ of a Porteguisse, seven
 Moneths upon promise that he should doe as much
 for me againe; and when I should borrow of him,
 hee could lend me but $\frac{1}{12}$ of a Porteguisse: now I
 demand how long time I must keepe his money in
 just recompence of my loane, accounting 12 Mo-
 neths in the year?

A question
 of Loan.

Scholar. The first number must be the first
 money borrowed, that is $\frac{1}{2}$ of the Porteguisse:
 the second number the 7 moneths, that is $\frac{7}{12}$ of
 a year: and the third number the money
 that was lent in recompence, that is $\frac{1}{12}$ of a
 Porteguisse: then I set the

$$\frac{\frac{1}{2}}{\frac{7}{12}} = \frac{Z}{\frac{1}{12}}$$

Then

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Then (as you taught me) I multiply 3 (being numerator in the first number) by 7, the numerator of the second number, and it maketh 21, which I multiply by 12 the denominator of the third, and it maketh 252 for the dividend: then I multiply 4, the denominator of the first, by 13 the denominator of the second, and it yieldeth 52, which I multiply againe by 5, the numerator of the third, and it will make 260, that is the divisor. Then I divide 252 by 260, so it will be in the small fraction $\frac{252}{260}$ of a year.

Master. And thus do you see some ease in working, better then to multiply and divide feynfully so many Fractions.

Another question yet will I propose, to the intent you may see thereby the reason of the Statute of Assise of Bread and Ale, which in all Statute Books, in Latine, French, and English is much corrupted for want of knowledge in this Art: for the right understanding whereof, I propose this question.

When the price of a quarter of Wheat is 2 shillings, the farthing white loafe shall weigh 68 shillings: then I demand what shall such a loafe weigh, when a quarter of Wheat is sold for 3 shillings.

Scholar. This question must bee wrought as it is proposed in whole numbers, and not in Fractions.

Master. You seeme to say reasonably, notwithstanding in the Statute of Assise, the rate is made
by

Statute of
Assise of
bread and
ale.

Question
of bread.

by the proportion of pence to a pound weight
 Troy, as it was by a Scarce of any long
 continuance, seeing the shillings doe change
 often, so all other moneys doe but this Scarce
 being well understood, for a continuall Rule for
 any use, it shall after declare by a new Table of
 Aunce, converting the shillings into ounces, and
 parts of ounces, as it shalbe necessary.
 And because here by a shilling you must
 understand $\frac{1}{2}$ of a pound weight, and so by
 a penny, $\frac{1}{4}$ of an ounce: wherefore although
 you might think this question proposed by
 whole numbers well enough, for that time
 when the Scarce was made, yet to apply it
 to your use, and to make it serve for all times
 generally, it is best to worke it by fractions,
 setting for 2 shillings $\frac{1}{2}$, and for 68 shillings
 $\frac{68}{2}$, and so for the third $\frac{1}{2}$, and then with the
 figure of the question. **Z**
 stand thus.

In which question, because all the denomi-
 nators be like, you shall worke onely with the
 numerators.

Scholar. When shall I multiply 68 by 2,
 whereof cometh 136, which if I divide by
 3, the quotient will be $45\frac{1}{3}$: but how shall I
 make a fraction of that, to stand with the
 other?

Master. Have you so soone forgot:
 ten what was taught you so lately?
 This is his forme.

$$\begin{array}{r} 45\frac{1}{3} \\ 20 \end{array}$$

Note what
a shilling
is.

Scholar: I understand it with you, then it
is twenty pence, and the third delle
of the twenty part, so I miss
Master: So is it that miseth the shilling as
a shilling a pence, whereby you may know one
great error in the Statute Book, which have
constantly a shilling to that miseth: And by
this Rule, if you examine the Statute, you shall
find many mistakes: And therefore for the
true understanding of that Statute, and for
time, as I have made mention of it, and for
that recognized it, so did I with that all Gen-
tlemen and other students of the Lawes
shall not neglect the Art of Arithmetick,
as unlearned to their studies, and therefore to
encourage them thereto, I have gathered both
them and others in generall, I will compile
a Table of that part of the Statute into two co-
lumes, the first a third column: And I have
the correction of those errors which have
crept into it.



and thus
in words of the Statute, because all the
errors be like you shall easily find the
differences.

Scholar: When shall I multiply
of the Statute? I shall multiply
Here followeth the Table.
I shall multiply of the Statute
make a fraction of that to stand for the
other.

Master: Have you found some
for that was taught you to help
the in his time.

| The price
number of
Wares | The weight of a
thing, when
the Statute Bookes | The weight of a
thing, when
loose by
the Statute Bookes | The Question
by just Alike |
|---------------------------------|--|--|-------------------------------|
| 5. 0. | 1. 8. 0. | 6. 16. 0. | 1. 5. 0. |
| 1. 0. | 4. 16. 8. | 3. 8. 0. | 6. 16. 0. |
| 2. 0. | 2. 14. 4. | 2. 8. 0. | 3. 8. 0. |
| 3. 0. | 2. 8. 0. | 1. 18. 0. | 2. 3. 4. |
| 4. 0. | 1. 16. 0. | 1. 18. 0. | 1. 18. 0. |
| 5. 0. | 1. 10. 0. | 1. 14. 0. | 1. 14. 0. |
| 6. 0. | 1. 8. 2. | 1. 10. 0. | 1. 10. 0. |
| 7. 0. | 1. 4. 8. | 1. 7. 0. | 1. 7. 0. |
| 8. 0. | 0. 2. 8. | 1. 4. 0. | 1. 4. 0. |
| 9. 0. | 0. 16. 11. | 1. 2. 8. | 1. 2. 8. |
| 10. 0. | 0. 19. 1. | 1. 0. 0. | 1. 0. 0. |
| 11. 0. | 0. 18. 1. | 0. 19. 5. | 0. 19. 5. |
| 12. 0. | 0. 7. 0. | 0. 18. 1. | 0. 18. 1. |
| 13. 0. | 0. 16. 0. | 0. 17. 0. | 0. 17. 0. |
| 14. 0. | 0. 15. 0. | 0. 16. 0. | 0. 16. 0. |
| 15. 0. | 0. 14. 0. | 0. 15. 0. | 0. 15. 0. |
| 16. 0. | 0. 13. 7. | 0. 14. 3. | 0. 14. 3. |
| 17. 0. | 0. 12. 11. | 0. 13. 7. | 0. 13. 7. |
| 18. 0. | 0. 12. 4. | 0. 12. 11. | 0. 12. 11. |
| 19. 0. | 0. 11. 10. | 0. 12. 4. | 0. 12. 4. |
| 20. 0. | 0. 11. 4. | 0. 11. 10. | 0. 11. 9. |
| | | 0. 11. 4. | 0. 11. 4. |

In the common Bookes there is no further rate of Assise made, then into 12 s. the quarter of wheat, but in an ancient Copy of 100 years old (which I have) there is added the rate of Assise unto 20 s. the quarter, but yet was that Assise also either wrong cast at the first penning, or else corrupt since that time, for lack of just knowledge in the Rule of Proportion, which I will add here also to gratifie such as be desirous to understand such exactly.

| The price of
a quarter of
Wheat. | | The weight of a far-
thing white loafe by
the Statute Bookes. | | The Correction
by just Assise. | |
|--|----|---|----|-----------------------------------|----|
| s. | d. | l. | s. | l. | s. |
| 12 | 6 | 0 | 11 | 0 | 0 |
| 13 | 0 | 0 | 11 | 6 | 0 |
| 13 | 6 | 0 | 10 | 1 | 0 |
| 14 | 0 | 0 | 9 | 7 | 0 |
| 14 | 6 | 0 | 9 | 7 | 0 |
| 15 | 0 | 0 | 9 | 1 | 0 |
| 15 | 6 | 0 | 9 | 1 | 0 |
| 16 | 0 | 0 | 9 | 0 | 0 |
| 16 | 6 | 0 | 8 | 6 | 0 |
| 17 | 0 | 0 | 8 | 3 | 0 |
| 17 | 6 | 0 | 7 | 10 | 0 |
| 18 | 0 | 0 | 7 | 6 | 0 |
| 18 | 6 | 0 | 7 | 3 | 0 |
| 19 | 0 | 0 | 7 | 2 | 0 |
| 19 | 6 | 0 | 5 | 10 | 0 |
| 20 | 0 | 0 | 5 | 6 | 0 |

These two Tables I have set forth, be-
cause the many people think that I have set
forth such exorbitant rates from my Law these
parts which might of right seem either in-
personable or diminutive: but yet I may not
be so careless as to neglect manifest errors,
which is not only my part, but every good
Subjects duty with sobriety to correct. And
for avoiding of offence, I have rather done it
in this private Book, than in any Book of the
Statutes it self, trusting that all Men will take
it in good part.

Scholar. I would wish so, but I dare not so
hope; for never good man that would receive
enough could escape the venomous tongues of
envious detractors, which because they either
cannot, or like not to see any good themselves,
do delight to bark at the things of others, but
I beseech you to say nothing for their per-
verse behaviors.

Master. I consider many things that some
may object, to wit, that I am not impowered
of full answers, but I will not then so happy
to name the answers, but I shall shew their
reasons, but as I trust that men are of a better
nature, and more gratefull than men some
have been in times past. As I have done in
the Statute of Assize for Bread in rate of shil-
lings, so will I set forth the like Table in
pounds and ounces, and the parts thereof, that
it may be easily applied to all times: But I
meane not by this to alter any word of the
Statute

Concern-
ing the fol-
lowing
Tables.

322 Tho Golden Rule reverse

A pound
weight.

Statute, being so good in Ordinance, and of so
great consequence, had I only to make it an
kind of exposition and declaration of the said
Statute, trusting that thereby the Statute may
be better understood, and consequently better
put in execution. And here you shall note that
I have accounted the shillings after the rate of
60 shillings to the pound weight, because I
esteem it the most apt for use. Thus here-
fore in the first Column you finde the price of
Wheat directly against it; in the second Co-
lumn, you may finde the weight of a farthing
white Loaf. To this but three can I if you dou-
ble the number (as I have done in the third
Column) then have you the weight of the half
penny white loaf; and so in the fourth Co-
lumn to see the weight of a penny white loaf.
It needeth not to tell that the sight doth tell
for both the other Columns; is parted into
three smaller pillars, whereof the first Column
tells the three rules, pounds, ounces, and
penny weight. And as in the first Column
10 pence make a shilling and 20 shillings make
a pound; so in the other three Columns 20
pence weight maketh an ounce, and 12 ounces
do make a pound. Thus is it done, and more
shall be done in time past. And I have done
the Statute of A.D. 1534 for Bread in rate of full
weight, as it is set forth like the Table in
pounds and ounces, and the price thereof. But
it may be easily applied to all times: but
I have not been able to alter any two of the
Statute.

Common
weight
Table

Considering the understanding of the Table following, wherein according to our time, *Master Record* alloweth 60 pence to the ounce, and 3 pound or 6 shillings to the pound, and thereupon after the rate of 60 shillings to the pound Troy, doth here frame or introduce this his Table, beginning at 3 shillings the quarter, till he come to 40 shillings 6 pence the quarter. And this his proportion (for that he hath not set down any one Example to continue the work) hath been hard for many to conceive or comprehend, and therefore the onely chief cause why I have written this digression, for the better understanding of him therein.

The first thing therefore that is sought for in this Table, as in the other aforesaid, is a *Maxime* grounded upon the *Statute*, which is this. When the quarter of *Wheat* is sold for two shillings, then the *farthing white loafe* shall weigh 68 shillings, whereby a shilling is meant of a pound, and by a penny, of an ounce. Now therefore for a generall Rule, to finde what weight the *farthing white loafe* shall weigh at 3 shillings the quarter, till you come to 40 shillings 6 pence the quarter, is thus to be wrought. Comming to the first ground, and working by the *Backer Rule*, say; If two shillings the quarter give, or allow the *farthing white loafe* to weigh 68 shillings, what weight ought the *farthing white loafe* to weigh at 3 shillings the quarters? Worke, and you shall find 45 shillings 4 pence,

as before in the correction of the first Table is noted. Then for the second work, say by the Rule of 3 direct; if 20 pence give one ounce, what giveth 45 shillings 4 pence? multiply and divide, and you shall finde 544 ounces, which 544 ounces being multiplied by 3, for 3 pounds, or 60 shillings, yeeldeth 1632 ounces, which divided by 20, produceth 81 ounces, and $\frac{12}{20}$ or rather $\frac{3}{5}$ of an ounce, equall unto 12 penny weight, which is halfe an ounce, and 2 penny weight, and so maketh in all 6 pounds, 9 $\frac{1}{2}$ ounces, and 2 penny weight. Now the next way to continue this Table, to know the weight of the halfe penny white loafe, is thus, multiply 1632 ounces by 2, and it bringeth forth 3264 ounces, and divided by 20, it yeeldeth 163 ounces, and $\frac{4}{20}$, which is equall to 13 pounds, 7 ounces, and 4 penny weight, as M. Record his Table noteth,

Thirdly, for the weight of the penny white loafe, multiply 1632 ounces by 4, and divide by 20, and after by 12, as before, and you shall find 27 pounds 2 ounces, and 8 penny weight, &c. This Method, or else by doubling the farthing white loafe, for the weight of the halfe penny white loafe, and so doubling the halfe penny white loafe, for the weight of the penny white loafe, is the order to continue the Table to the end thereof.

The

The price of a quarter of Wheat.

| li. | s. | d. |
|-----|----|----|
| 0 | 3 | 0 |
| 0 | 4 | 0 |
| 0 | 6 | 0 |
| 0 | 7 | 0 |
| 0 | 9 | 0 |
| 0 | 10 | 0 |
| 0 | 12 | 0 |
| 0 | 13 | 0 |
| 0 | 15 | 0 |
| 0 | 16 | 0 |
| 0 | 18 | 0 |
| 0 | 19 | 0 |
| 1 | 1 | 0 |
| 1 | 2 | 0 |
| 1 | 4 | 0 |
| 1 | 5 | 0 |
| 1 | 7 | 0 |
| 1 | 8 | 0 |
| 1 | 10 | 0 |
| 1 | 11 | 0 |
| 1 | 13 | 0 |
| 1 | 14 | 0 |
| 1 | 16 | 0 |
| 1 | 17 | 0 |
| 1 | 19 | 0 |
| 2 | 0 | 6 |

The weight of a farthing white loaf.

| po. | oun. | penny |
|-----|------|-------|
| po. | oun. | penny |
| 6 | 9 | 12 |
| 4 | 6 | 8 |
| 3 | 4 | 16 |
| 2 | 8 | 12 |
| 2 | 3 | 4 |
| 1 | 11 | 6 |
| 1 | 8 | 8 |
| 1 | 6 | 2 |
| 1 | 4 | 6 |
| 1 | 2 | 16 |
| 1 | 1 | 12 |
| 1 | 0 | 11 |
| 1 | 0 | 4 |
| 10 | | 17 |
| 10 | | 4 |
| 9 | | 12 |
| 9 | | 1 |
| 8 | | 11 |
| 8 | | 3 |
| 7 | | 15 |
| 7 | | 8 |
| 7 | | 1 |
| 6 | | 16 |
| 6 | 10 | 1 |
| 6 | | 5 |
| 6 | 0 | 2 |

The price of a quarter of Wheat.

DO. CH. DEBIA

| li | sh | de | po | oun | penny |
|----|----|----|-----|--------|-------|
| | | | ces | weight | |
| 0 | 3 | 0 | 13 | 7 | 4 |
| 0 | 4 | 6 | 9 | 6 | 16 |
| 0 | 6 | 0 | 6 | 9 | 8 |
| 0 | 7 | 6 | 5 | 5 | 8 |
| 0 | 9 | 0 | 4 | 6 | 8 |
| 0 | 10 | 14 | 3 | 10 | 13 |
| 0 | 12 | 0 | 3 | 4 | 16 |
| 0 | 13 | 6 | 3 | 0 | 14 |
| 0 | 15 | 0 | 2 | 8 | 12 |
| 0 | 16 | 6 | 2 | 5 | 12 |
| 0 | 18 | 0 | 2 | 3 | 4 |
| 0 | 19 | 6 | 2 | 1 | 2 |
| 1 | 1 | 0 | 2 | 0 | 9 |
| 1 | 2 | 6 | 1 | 9 | 15 |
| 1 | 4 | 0 | 1 | 8 | 8 |
| 1 | 5 | 6 | 1 | 7 | 4 |
| 1 | 7 | 0 | 1 | 6 | 2 |
| 1 | 8 | 6 | 1 | 5 | 3 |
| 1 | 10 | 0 | 1 | 4 | 6 |
| 1 | 11 | 6 | 1 | 3 | 10 |
| 1 | 13 | 0 | 1 | 2 | 16 |
| 1 | 14 | 6 | 1 | 2 | 3 |
| 1 | 16 | 0 | 1 | 1 | 12 |
| 1 | 17 | 6 | 1 | 1 | 1 |
| 1 | 19 | 0 | 1 | 0 | 11 |
| 2 | 0 | 6 | 1 | | |

The weight of a half penny white loak.

| po | oun | penny |
|-----|--------|-------|
| ces | weight | |
| 13 | 7 | 4 |
| 9 | 6 | 16 |
| 6 | 9 | 8 |
| 5 | 5 | 8 |
| 4 | 6 | 8 |
| 3 | 10 | 13 |
| 3 | 4 | 16 |
| 3 | 0 | 14 |
| 2 | 8 | 12 |
| 2 | 5 | 12 |
| 2 | 3 | 4 |
| 2 | 1 | 2 |
| 2 | 0 | 9 |
| 1 | 9 | 15 |
| 1 | 8 | 8 |
| 1 | 7 | 4 |
| 1 | 6 | 2 |
| 1 | 5 | 3 |
| 1 | 4 | 6 |
| 1 | 3 | 10 |
| 1 | 2 | 16 |
| 1 | 2 | 3 |
| 1 | 1 | 12 |
| 1 | 1 | 1 |
| 1 | 0 | 11 |
| 1 | | |

The weight of a penny white loak.

| po | oun | penny |
|-----|--------|-------|
| ces | weight | |
| 17 | 3 | 8 |
| 18 | 1 | 12 |
| 13 | 7 | 4 |
| 10 | 10 | 11 |
| 9 | 0 | 16 |
| 7 | 9 | 5 |
| 6 | 9 | 12 |
| 6 | 0 | 10 |
| 4 | 5 | 3 |
| 4 | 11 | 6 |
| 4 | 6 | 3 |
| 4 | 2 | 4 |
| 3 | 0 | 9 |
| 3 | 7 | 10 |
| 3 | 4 | 16 |
| 3 | 2 | 8 |
| 2 | 0 | 5 |
| 2 | 10 | 7 |
| 2 | 8 | 12 |
| 2 | 7 | 1 |
| 2 | 5 | 13 |
| 2 | 4 | 7 |
| 2 | 3 | 4 |
| 2 | 2 | 2 |
| 2 | 1 | 2 |
| 2 | 0 | 0 |

Having spoken before for the understanding of the Table, placed by M. Record, a man indued with rare knowledge in Arithmetical & Geometrical Proportions, touching the Statute of Coynage, and the Standard thereof, as appeareth in his Epistle of this Book, dedicated to K. Edward the sixth, insinuating unto his Highnesse, that the Standard of Coyne, is much altered from the 14 year of K. Edward the third (when this Statute and Assise was confirmed) to the Standard of this our time. For it appeareth that in K. Edward the thirds time, when the Assise of Bread and Drink was established, that a Sterling penny, round without clipping, did then weigh 32 cornes of Wheat dry, and taken out of the middle of the ear, and 20 of these pence made an ounce, & 12 ounces made a pound Troy. And so from the weight, of a penny, to 20 shillings sterling, which then weighed 12 ounces, tooke Bread his weight and proportion. And now finding 60 pence is an ounce: That onely cause (I perceive, for the zeale of a Common-wealth) moved him to set downe the same Table in this private Booke meaning not thereby to alter any word of the Statute, being so good an Ordinance, and of so long continuance, but as a kind of exposition by the way that thereby the Statute may be better understood, and so consequently better put in execution: Which Assise of his, is three times greater then the Statute now alloweth: Therefore also (to gratifie such as are desirous of knowledge, according to these prices of a quarter of Wheat) I have added to this Author these three other new Tables following, and reduced their prices into their just proportions of sterling money, and also reduced the money into knowne weight Troy, according to the Statute. And thereafter according to proportion in my other three Tables, have I noted the just weight, that a Farthing, Halfe-penny, and Penny white-loafe ought to weigh by the Statute.

The price of a quarter of Wheat.

| li. | s. | d. |
|-----|----|----|
| 0 | 3 | 0 |
| 0 | 4 | 6 |
| 0 | 6 | 0 |
| 0 | 7 | 6 |
| 0 | 9 | 0 |
| 0 | 10 | 6 |
| 0 | 12 | 0 |
| 0 | 11 | 6 |
| 0 | 15 | 0 |
| 0 | 16 | 6 |
| 0 | 19 | 0 |
| 0 | 0 | 6 |
| 1 | 1 | 0 |
| 1 | 2 | 6 |
| 1 | 4 | 0 |
| 1 | 5 | 6 |
| 1 | 7 | 0 |
| 1 | 8 | 6 |
| 1 | 10 | 0 |
| 1 | 11 | 6 |
| 1 | 13 | 0 |
| 1 | 14 | 6 |
| 1 | 16 | 0 |
| 1 | 17 | 6 |
| 1 | 19 | 0 |
| 2 | 0 | 6 |

The weight of a farthing white-loafe in Sterling money by Assise.

| po. | oz. | penny
ces. | weight. |
|-----|-----|------------------|---------|
| 2 | 5 | 4 | |
| 1 | 10 | $2\frac{1}{2}$ | |
| 1 | 2 | 8 | |
| 0 | 18 | $1\frac{1}{2}$ | |
| 0 | 15 | $1\frac{1}{3}$ | |
| 0 | 12 | $15\frac{1}{4}$ | |
| 0 | 11 | 4 | |
| 0 | 10 | $0\frac{1}{2}$ | |
| 0 | 9 | $0\frac{1}{4}$ | |
| 0 | 8 | $2\frac{11}{11}$ | |
| 0 | 7 | $6\frac{1}{2}$ | |
| 0 | 6 | $11\frac{1}{2}$ | |
| 2 | 6 | $9\frac{1}{2}$ | |
| | 6 | $0\frac{1}{2}$ | |
| | 5 | 8 | |
| | 5 | 4 | |
| | 5 | $0\frac{1}{2}$ | |
| | 4 | $9\frac{1}{2}$ | |
| | 4 | $6\frac{1}{2}$ | |
| | 4 | $3\frac{1}{2}$ | |
| | 4 | $1\frac{1}{4}$ | |
| | 3 | $11\frac{1}{2}$ | |
| | 3 | $9\frac{1}{2}$ | |
| | 3 | $7\frac{1}{2}$ | |
| | 3 | $5\frac{1}{2}$ | |
| | 3 | $4\frac{1}{2}$ | |

The weight of a farthing white-loafe in Troy weight by Assise.

| po. | oz. | penny
ces. | weight. |
|-----|-----|----------------|---------|
| 2 | 3 | 4 | |
| 2 | 6 | $2\frac{1}{2}$ | |
| 1 | 1 | 12 | |
| 0 | 10 | 17 | |
| | 9 | 1 | |
| | 7 | 15 | |
| | 6 | 16 | |
| | 6 | $0\frac{1}{2}$ | |
| | 5 | 8 | |
| | 4 | 18 | |
| | 4 | 10 | |
| | 4 | 3 | |
| | 4 | 1 | |
| | 3 | 12 | |
| | 3 | 8 | |
| | 3 | 4 | |
| | 3 | $0\frac{1}{2}$ | |
| | 3 | 17 | |
| | 2 | 16 | |
| | 2 | 11 | |
| | 2 | 9 | |
| | 2 | 7 | |
| | 2 | 5 | |
| | 2 | 3 | |
| | 2 | 1 | |
| | 2 | $0\frac{1}{2}$ | |

The price of a quarter of Wheat
 The weight of the half-penny white-loafe in Troy weight by Assise

| po. | oun | penny |
|------|--------|------------------|
| ces. | weight | |
| 4 | 6 | 8 |
| 3 | 0 | 5 $\frac{1}{2}$ |
| 2 | 3 | 4 |
| 1 | 9 | 1 $\frac{1}{2}$ |
| 1 | 6 | 2 $\frac{1}{2}$ |
| 1 | 3 | 10 $\frac{1}{2}$ |
| 1 | 1 | 12 |
| 1 | 0 | 12 |
| 0 | 10 | 17 $\frac{1}{2}$ |
| 0 | 9 | 17 $\frac{1}{2}$ |
| 0 | 9 | 1 $\frac{1}{2}$ |
| 0 | 8 | 7 $\frac{1}{2}$ |
| 0 | 8 | 3 $\frac{1}{2}$ |
| 0 | 7 | 5 $\frac{1}{2}$ |
| 0 | 6 | 16 |
| 0 | 6 | 8 |
| 0 | 6 | 0 $\frac{1}{2}$ |
| 0 | 5 | 14 $\frac{1}{2}$ |
| 0 | 5 | 8 $\frac{1}{2}$ |
| 0 | 5 | 3 $\frac{1}{2}$ |
| 0 | 4 | 19 |
| 0 | 4 | 14 $\frac{1}{2}$ |
| 0 | 4 | 11 $\frac{1}{2}$ |
| 0 | 4 | 7 $\frac{1}{2}$ |
| 0 | 4 | 3 $\frac{1}{2}$ |
| 0 | 4 | 0 $\frac{1}{2}$ |

The weight of the penny white-loafe in Troy weight by Assise

| po. | oun | penny |
|------|--------|------------------|
| ces. | weight | |
| 9 | 0 | 16 |
| 6 | 0 | 10 $\frac{1}{2}$ |
| 4 | 6 | 8 |
| 3 | 7 | 10 $\frac{1}{2}$ |
| 3 | 0 | 5 $\frac{1}{2}$ |
| 3 | 7 | 1 $\frac{1}{2}$ |
| 2 | 3 | 4 |
| 2 | 0 | 3 $\frac{1}{2}$ |
| 1 | 9 | 15 $\frac{1}{2}$ |
| 1 | 7 | 15 $\frac{1}{2}$ |
| 1 | 6 | 3 $\frac{1}{2}$ |
| 1 | 4 | 14 $\frac{1}{2}$ |
| 1 | 4 | 3 $\frac{1}{2}$ |
| 1 | 2 | 10 $\frac{1}{2}$ |
| 1 | 1 | 12 |
| 1 | 0 | 16 |
| 0 | 0 | 1 $\frac{1}{2}$ |
| 0 | 11 | 9 $\frac{1}{2}$ |
| 0 | 10 | 17 $\frac{1}{2}$ |
| 0 | 10 | 7 $\frac{1}{2}$ |
| 0 | 9 | 18 |
| 0 | 9 | 9 $\frac{1}{2}$ |
| 0 | 9 | 2 $\frac{1}{2}$ |
| 0 | 8 | 14 $\frac{1}{2}$ |
| 0 | 8 | 7 $\frac{1}{2}$ |
| 0 | 8 | 1 $\frac{1}{2}$ |

neiloup A
 -uisant to
 to gait
 to gait

Scholar. Sir, I do thanke you most heartily for this, not onely in mine owne name, and in the name of all Students, but also in the name of the whole Commons, to whom the restitution of this Aulse (I trust) shall bring restitution of the weight in Bread, which long time hath been abused. And if you know any like things more, wherein you would vouchsafe to declare the errors, and set forth the truth, you cannot but obtaine great thanks of all good hearted men that love the Common-wealth.

Master. I have sundry things to declare, but I have reserved them for a private Booke by it selfe, yet notwithstanding because the Statute of the rate of measuring of ground is so common, that it toucheth all men, and yet no more common then needfull, but so much corrupt, that is, too farre out of all good rate, not onely in the English Books of Statutes, commonly printed, but also in the Latine Books, and in the French also (for I have read of each sort, and conferred them diligently). I will give you a Table for the restitution of those errors, as may suffice for this present time. And first I will propose one question to you, touching the use of that Statute, whereby you may perceibe the order how to examine the whole Statute, and every parcell thereof, and the question is this.

A question
of measu-
ring of
ground.

Whether the Acre of ground doth contain four
Perches in breadth, then must it contain 40 Per-
ches

How long? Then do I demand of you, how much shall the length of an Acre be, when there is the breadth of 13 Perches. But before you answer to this question, I will declare unto you another Statute, which is the Ground of the former Statute. And that Statute is this:

It is ordained that three Barley corns dry and bruised, shall make up the measure of an inch; twelve inches shall make a foot, and three foot shall make a yard, (the common English Books have an Ell) five yards and an halfe make a Perch, and forty Perches in length, and four in breadth shall make an Acre. This is that Statute, whereby you may perceive, that the intent of the Statute is, that one acre should containe 160 square Perches. Now let us here give answer to the question.

Statute measure.

An Acre.

As I perceive by the words of the Statute, a Perch to be the $\frac{1}{160}$ part of an Acre, so will I make those numbers all in Fractions, and so worke the question: but seeing I may doe it also in whole numbers, I take that way for the most ease. therefore thus I let the question sit to me. When

do I multiply 40 by 4, and it maketh 160, which I divide by 13, and the quotient is

$$\begin{array}{r} 40 \\ 13 \overline{) 520} \\ \underline{52} \\ 0 \end{array}$$

12. Now turne that $\frac{1}{13}$ into the common parts of a Perch, as they be named in the former Statute: howbeit it shall be best to take one of the least parts in denomination

for abolding of much labour, as Feet whereof the Perch containeth 16

Scholar. When to returne 4 faine Feet, I multiply 16 by 4, and it maketh 66, which I must divide by 13, and the quotient is 5.

Master. So I finde, that if the acre hold in breadth 13 Perches, it shall contain in length 12 Perches 5 Foot, and $\frac{1}{4}$ of a Foot, which is not fully an Inch, for the Inch is $\frac{1}{12}$ of a Foot. But here all the Statute Books in Latine and English (that I have seene) do note it to bee 13 Perches, 5 Foot, and one Inch, which maketh above 13 Perches too many in the Acre: so that I would have thought the error so have crept into the printed Books; by the great negligence that Printers in our time do use, save that in written Copies of great antiquity, I do finde the same: yet have I one French copy which hath 12 Perches, and one Foot, and that misseth very little of the truth.

Note this
error.

Scholar. Then I see it is true that I have often heard say, that the truest copies of the Statutes, be the French copies.

Master. That is often true but not generally, as I have by conference tryed diversly: but in this Statute the French Book is most corrupt: in all other places lightly.

But now to performe my promise, I will set forth the Table for measuring of an Acre of ground, onely by such parts as the Statute doth mention, because at this time I doe not

purpose write it for the better understanding of that Statute, and hereafter with other things intend to set forth this same more at large.

In this Table following, I have not done as in the other Statute before compared by restitution with the faults crept into the Statute, but onely have written that true measure, which the equity of the Statute doth pretend. For it were vile to judge of so noble Princes and worthy Counsellours, as have authorised and set forth this Statute, that they would make one Acre in any form greater then another, but every one to be just and equall with each other, which is the ground also of my Worke: and hereby may all men perceive how needfull Arithmetick is to the Students of Law. But now I think best to make an end of these matters for this present time, sith the Table hath in it none obscurity that I should need to declare.

The breadth of the Acre. The length of the Acre.

| Perches | Perch e Feet | Inches | parts of an Inch |
|---------|--------------|--------|------------------|
| 10 | 16 | 0 | 0 |
| 11 | 14 | 9 | 0 |
| 12 | 13 | 5 | 0 |
| 13 | 12 | 5 | $\frac{10}{11}$ |
| 14 | 11 | 7 | $\frac{6}{7}$ |
| 15 | 10 | 11 | 0 |
| 16 | 10 | 0 | 0 |
| 17 | 9 | 6 | $\frac{17}{17}$ |
| 18 | 8 | 14 | 0 |
| 19 | 8 | 6 | $\frac{7}{15}$ |
| 20 | 8 | 0 | 0 |
| 21 | 7 | 10 | $\frac{2}{7}$ |
| 22 | 7 | 4 | 0 |
| 23 | 6 | 15 | $\frac{2}{15}$ |
| 24 | 6 | 11 | 0 |
| 25 | 6 | 6 | $\frac{1}{5}$ |
| 26 | 6 | 2 | $\frac{6}{13}$ |
| 27 | 5 | 15 | $\frac{1}{3}$ |

The

| The breadth of the Area | The length of the Area | | | |
|-------------------------|------------------------|------|--------|---------------|
| Pence | pence | Far. | Inches | an Inch |
| 28 | 5 | 11 | 9 | $\frac{1}{4}$ |
| 29 | 5 | 8 | 6 | $\frac{1}{2}$ |
| 30 | 5 | 5 | 6 | 0 |
| 31 | 5 | 2 | 7 | $\frac{1}{4}$ |
| 32 | 5 | 0 | 0 | 0 |
| 33 | 4 | 14 | 0 | 0 |
| 34 | 4 | 11 | 7 | $\frac{1}{4}$ |
| 35 | 4 | 9 | 5 | $\frac{1}{4}$ |
| 36 | 4 | 7 | 4 | 0 |
| 37 | 4 | 5 | 4 | $\frac{1}{4}$ |
| 38 | 4 | 3 | 5 | $\frac{1}{2}$ |
| 39 | 4 | 1 | 8 | $\frac{1}{4}$ |
| 40 | 4 | 0 | 0 | 0 |
| 41 | 3 | 14 | 10 | $\frac{1}{4}$ |
| 42 | 3 | 13 | 4 | $\frac{1}{4}$ |
| 43 | 3 | 11 | 10 | $\frac{1}{4}$ |
| 44 | 3 | 10 | 6 | 0 |
| 45 | 3 | 9 | 2 | 0 |



Scholar. Indeed, Sir, I understand the Table (as I think) by those other tables you set forth before. For in the first Colunne is set the Perches of the breadth of an Acre, & then in the two Colunnes following appeareth how many Perches and how many Foot that same acre must have for his length.

Master. You take it well: howbest to speak exactly of breadth and length, and the first Colunne doth sometime betoken the breadth, and sometime the length: for properly the longest side of any square doth limit his length, and the shorter side doth betoken the breadth, yet it is no great abuse in such Tables, where a man cannot well change the title, solet the name remain, although the proportions of the numbers do change: for still by the first Colunne is expressed the measure of the one side, and by the two other Pillars in one Colunne is set forth the measure of the other side. And this shall bee sufficient now for the use of the Golden Rule.

The Rule of Fellowship.



Ow somewhat wil I touch certaine other Rules which for their severall names may seem divers Rules, and distinct from this, but indeed they are but branches of it: yet because they have severall workings in appearance, but

but also pleasant in use, I will give you a taste of each of them. As for the Rule of Fellowship, both single and double, with time, and without time, I shall need to say little more then I have already said in teaching the works of whole numbers: yet an example or two will we have to refresh the remembrance of the same; and to declare certain proper uses and applications of it, as this for one.

The Rule of Fellowship with our time.

Four men got a booty, by prize in time of war, the price is in value of money, 8100 pound, and because the men bee not of like degree, therefore their shares may not be equal: but the chiefest person will have of the booty the third part, and the tenth part each: the second will have a quarter, and the tenth part each; the third will have the sixth part: and so there is left for the fourth man a very small portion, but such as he is not (where the baptised or un baptised must be content with one 20 part of the prey). Now I demand of you, what shall every man have to his share?

A question of inequall society.

Scholar. You must be faine to answer to your own question, for it is not like to be answered at this time.

Master. We forme to understand the solution of this question, and all such like, is this: Reduce all the Denominators into one number by multiplication, except that any of them bee parts of some other of them: so all such parts you may overpass, and take for them all those numbers, whose parts they be: As in this example the shares be these,

If I multiply all the Denominators together
 beginning with 3, and so go on unto 20, it will
 make 14400: but considering that 3 is a part
 of 6, I will chaunge that 3, and likewise ten,
 which is a part of 20, I may onequally divide,
 and then there is but 3 Denominators to mul-
 tiply, that is, 4, 6, & 20, which make 480, which
 summe I take for my work, because all the
 Denominators will be found in it. When I
 take such parts of it as the question importeth,
 that is, for the first man $\frac{1}{3}$, and $\frac{1}{4}$, the $\frac{1}{3}$ is 160,
 the $\frac{1}{4}$ is 48, which I put in one summe for the
 first mans share, and it maketh 208. Then
 for the second mans share, I take $\frac{1}{6}$, which is
 120, and $\frac{1}{20}$, which is 48, and that maketh 168.
 Then for the third man which
 must have $\frac{1}{5}$, I take 80. And for the fourth
 man there remaineth but 24, which is $\frac{1}{5}$ of
 the whole summe: so that if the whole prop-
 had been but 480 pound, then were the ques-
 tion answered: but because the summe was
 of greater value, by this meanes how shall I
 know the partition of it? I must set my num-
 bers by the order of the Golden Rule, putting
 in the first place the number of that I sought
 by multiplying the Denominators, and in the
 second place the summe of the body. And
 looke what proportion is between the first
 number and the second, the same proportion
 shall be between the part of that first num-
 ber, and the part of the second, comparing
 each to his like. Wherefore I will put in the
 third

The reason
 of this
 Rule.

third place, one of the parts or shares, and then
work by the former Rule of Proportion, or
Golden Rule. And because I have four feve-
rall parts of the first number, by which I
would find out four like parts of the second
number, therefore must I make four severall
figures.

Scholar, Now I trust I can answer to your
question, as by your favour I will prove.

And to try it, I let the four figures thus,
marked with A, B, C, D, to shew their order :

| | | | |
|-----|-------------------------------|-----|-------------------------------|
| 480 | $\frac{208}{480} \times 8190$ | 480 | $\frac{160}{480} \times 8190$ |
| 208 | $\frac{208}{480} \times 8190$ | 160 | $\frac{160}{480} \times 8190$ |
| 80 | $\frac{80}{480} \times 8190$ | 24 | $\frac{24}{480} \times 8190$ |

Thus then friends of them I multiply the se-
cond number by the third, and divide their
total by the first, and so amounteth the fourth
number which I seek for: For if I do multi-
ply 8190 by 208, it maketh 1733520, which
being divided by 480, maketh in the quotient
3611 for the first mans portion.

And to working with the other three fi-
gures, I finde for the second man 2865, and
for the third man 1365, and then for the fourth
man 409, and so every mans share is set
forth in the figure here annexed.

A

31:07

| | | | |
|----------|----------|----------|----------|
| A | | B | |
| 480 | Z | 8190 | Z |
| 208 | | 3549 | |
| C | | D | |
| 480 | Z | 8190 | Z |
| 80 | | 1365 | |

And thus much I think I have done well.

The proof
by Addition.

Master. If you misdoubt your working, and list to prove it, add all the shares together, and if they make the totall, then seemeth it well done.

Scholar. I may set them thus: and then by Addition, the just sum both amount, that is, 8190, and therefore (as you say) it seemeth to be well wrought.

3549
8190
8665
1365
4095
8190

But I beseech you, is there any doubt in this triall, that you use that word, seemeth?

Master. You may easily conjecture, that if you did assigne the first mans share to the last, and so change all the rest, and ordered another share, yet would the Addition appeare alwaies, and therefore is not the prooffe good.

The just
proof.

But if you will make a just prooffe for the first mans part, take 1 and 1/2 of the whole summe, and if it agree with the number in the figure, then it is well done. And so do for the second, third, and fourth summes, and this prooffe faileth not. Now will I propound certaine other questions, which have been set forth

forth by certaine learned men, albeit not without
 out some oversight, which questions I protest
 heartily, I do not repeat to deprave these good
 men; whose labours and studies I much praise
 and greatly delight in. But onely according
 to my profession, to seek out truth in all things;
 and to remove all occasions of error as much
 as in me lieth: and for that cause I will onely
 name the questions without hurting the Au-
 thors name.

The first question is this.

Four men did build an house which cost them 1000 crowns, their shares were such that the first should pay $\frac{1}{2}$ of the summe, and the second $\frac{1}{3}$ of the residue, the third man must lay out $\frac{1}{4}$ of the residue, and the fourth man should pay 200 crowns more. Can you answer to this question?

A question
 of building

Scholar. No, I cannot Sir, and that you
 know best of any man, for I know no more
 than you have taught me.

Master. Then I dare say you cannot do it,
 neither yet the best learned man that ever did
 propose it: for the question is impossible. For
 declaration whereof I will be bold to use first
 the representation of the numbers in their
 apertest forme (although I have not yet taught
 that manner of worke) because it may ap-
 peare plainly that the question is not possi-
 ble. For here I have set the parts, and added
 them, and they make the whole summe,
 and 4 and 30 more. Now, how is it possible

An impos-
 sible que-
 stion.

to

to do the truly either grates, and the 10 direct
 either charges, for that the 10 charges are
 particulate: 12 shall be more of 12, then
 then the total 12, and the 12 charges are
 in Scholer. It is against the
 forme of proof by addition, nor the 12 of
 of parties, more to the 12 charges of the
 Master. You say truth. And (because you
 shall perceive it the better) I will say it after
 the vulgar forme, as in
 this figure you see where the 12 is 1206
 with 6 over, is 1506, for the
 total as you heard before, is
 3000, the 12, and the 12 more is
 1012: the 12 would be 2000,
 but then abating 8, it is but
 1992, and then left of all, the 12 is 750, and the
 20 more maketh 770: which all being added
 to the summe, doe make 3280, where the
 total summe should be but 3000, which summe
 of 3000, if you divide by 12, you shall
 have 250 of it, that is 250, and thereto doe
 30 more, then will these 3 summes
 make 3280. Whereby you may see
 how this forme (as well as the
 other) both declares that the particu-
 lars in that question would make
 more then the whole summe by 280,
 and thirty more, and therefore
 can that question not bee accepted as a possible
 thing, but yet doe certayne leached men pro-
 pound such questions, and answer to them:

Where.

Therefore is somewhat to say to their excuse (rather of their good meaning, then for their doing) I will anon declare what may be said for their defence: but in the meane season, I will propound the Question as it may bee wrought by good possibility.

As if foure men build a house together, and it cost them 3000 crowns, and then for the partition they agree thus: that as often as the first man doth pay 6 crowns, so often the second man shall pay 4, the third man 8, and the fourth man 3. Or else thus, that the first man shall pay double so much as the fourth, and the second man shall pay $\frac{1}{2}$ of the first mans charge: the third man shall double so much as the second: (and these two wayes are to one end) but further for their agreement it is appointed also, that the first shall give 6 crowns overplus, and the second 12, and the fourth shall give 20, but the third man shall give no overplus but shall have 8 crowns abated of his charge.

The former question of building how possible.

Now is the question possible to be assayed, and this is the way to doe it. Mark the proportion of the severall charges, and set out small numbers in that rate, by which you may reduce the work to the Golden Rule, as here in the first form, the numbers are already named, 6, 4, 8, 3: and in the second forme (although they be but plainly named, yet they may bee the same numbers: for 6 is double to 3, and 4 is $\frac{1}{2}$ of 8: and again 8 is double to 4. Now adde these together, and they make 21, which 21 must be set for the first number in the Gol-

den Rule: for if it with the charging of each mans charge, would make the totall summe of the charges, then were those severall summes the charges of each man, besides his overplus: but now it is not so.

The Rule.

But yet this is true: (so excellent are conclusions Arithmericall) that look what proportion each of their severall sums doth beare to 21, the same proportion doth the just charges of every man (besides his overplus) beare to the totall of the charges, the overplus being deducted: wherefore this may you note, that before you doe apply the totall of his charges to the Golden Rule, you must deduct the overplus, which is 6, 12, and 20 that is, in the whole, 38: but then 8 must be restored for the abatement of the third man, and then remaineth to be deducted 30: take 30 therefore out of 3000, and there will rest 2970 which I must set in the Golden Rule, for the second summe: and for the third summe, I must put each of the small numbers before mentioned, which although they be not severall charges, yet they represent them in proportion. And so making for every mans charge a severall question, the figures will be 4, which I mark with foure letters, A, B, C, D, thus:

| | |
|--|---|
| <p>A</p> <p>21 $\overline{) 2970}$</p> <p>6 $\overline{) 8484}$</p> <p>8 $\overline{) 11314}$</p> | <p>B</p> <p>21 $\overline{) 2970}$</p> <p>4 $\overline{) 10644}$</p> <p>3 $\overline{) 14245}$</p> |
|--|---|

Where I have set for by the summe
of every mans charge in the fourth place, pre-
supposing that you can tell how to try out that
fourth summe by so many Examples as yet
have had.

Scholar. As I think that I understand this
forme, so I desire much to know what may
be said for them that mistake this Que-
stion. Master. I am so desirous to know this
ermong that you have forgotten to examine,
whether this work be without fault.

Scholar. I am somewhat this work to be well
done, because the Addition of the four seve-
rall numbers both make the totall summe of
2720, which was to be divided into such four
parts.

Master. But then have you forgotten that
the first man must pay for Crownes more be-
cause his share, & the second man the Crownes
more, the third man 4 Crownes more, and the
fourth man 12 Crownes more. For without
these your first totall of 2720 Crownes will
not be made.

Scholar. Then must I add to the first mans
summe 6 more, and it shall be 2726, and
to the second I must add 12, and
it shall be 2738. Then the third summe I
must add 4, and then shall the summe be
2742, then adding unto the fourth summe
12, shall be 2754.

20, it will be 444, and these
four summes will make 3000
which is the whole charge,
in this example it may apper
where first I gather the 4 that
maketh 2, and so proceede in

the Addition to the end, in
- Master. Now have you well done, and the
work in the same summes, is brought of other
learned men for the resolution of the que-
stion, as it was first proposed; (which as I
said) was impossible: and now examining
these severall summes, and see whether it both
agrees with the summes in the question propo-
sed.

He be first man must pay; and is other of the
totall summe: how think you, is 854; the hal,
and 6 more of 3000

Scholar. So that is not; for it should be
1506; and for the second man 1014; and for
the third man 1992; and for the fourth man 790;
whereof not one summe agreeth to this work.
But I marvel, that so wise men could be so
much overseen.

Master. It is commonly seen, that when
men will receive things from elder Writers,
and will not examine the thing, they stand
rather willing to erre with their Ancients in
company, then to be bold to examine their
works or writings. Which scrupulosity
hath ingendred infinite errors in all kinds of
know-

knowledge, and in all civill administration, and so in every kind of Art. But these learned men did not mean any other thing by this question, then to find such numbers as should beare the same proportion together, as those numbers in the question proportioned did beare one to another: which thing you shall perceiue more plainly by another question of this, that is this.

A question
of a Testa-
ment.

A man lying upon his death-bed, bequeathed his goods (which were worth 3600. Crownes) in this sort. Because his Wife was great with child, and he was uncertain whether the Child were male or female, he made his bequest conditional-ly, that if the Wife bare a Daughter, then should the Wife have halfe his goods, and the Daughter $\frac{1}{2}$; but if she were delivered of a Sonne, then that Sonne should have $\frac{2}{3}$ of the goods, and his Wife but $\frac{1}{3}$. Now is changed her to bring forth both a Sonne and a Daughter; the question is: How shall they part the goods agreeably to the Testator his Will?

Scholar. If some cunning Lawyers had this matter in scanning, they would determine this Testament to be quite void, and so the Man to die intestate, because the Testament was made insufficient, sith this condition was not expressed in it, and also it might have chanced that she should have brought forth neither Sonne nor Daughter, as often hath bin seen: so is the Will insufficient to that point also.

Master. Much Scanners would seem too cunning, and yet not so cunning as craft: to the mind of the Testator is to be taken into account for the sake of the Legatorie, when there is such such doubt. But let us say this is to be not by force of Law, but by proportion Geometrical, leaving the Testator's will to be followed, each sort of them.

Scholar. If the Sonne shall have $\frac{1}{2}$ by force of the Testament, so must the Mother have $\frac{1}{2}$. Again because she hath a Daughter also, therefore ought she to have $\frac{1}{2}$, and the Daughter, that is both wayes $\frac{1}{2}$, and $\frac{1}{2}$, which cometh to the whole goods, and more.

And therefore it seemeth also impossible.

Master. In this matter, the mind of the Testator is to be understood, that such proportion should be between the portion of the Wife and the Sonne as is between 2 and 3 , that is, the Sonne must have 3 to 2 his Mother, so shall he have 3 to 2 , that is, as much as his Mother, and halfe as much more; and the Mother must have the like rate in comparison to her Daughter. Then must I finde out three numbers in such proportion, that the first may have as much as the second, and halfe as much more (that is) in proportion sesquialters, and the second to the third, in that same proportion; such numbers be $9, 6, 4$.

Scholar. I pray you Sir, how shall I find out these numbers?

Master. That will I gladly tell you.

What

To find 3
numbers
in any pro-
portion.

To find
the pro-
portion
between
two num-
bers.

Whosoever the proportion be of any three numbers, multiply the Terms of that proportion together, and the number that amounteth shall be the middle number of the three: then multiply that middle number by the lesser term, and divide that total by the greater, and the least number of the three will amount: So if I multiply that middle number by the greater extreme, and divide the total by the lesser extreme, then will the greatest number of that Progression amount.

Scholar. When in this example to find the proportion of 1 to 3, I must divide (as you taught me in division) 3 by 1, and the quotient will be 3, that is, 3, whereby I perceive that the proportion in this question, is as 1 to 3. Therefore as you taught mee even now, I multiply 3 by 1, and the summe is 3, which must be the middle number: then I multiply the middle number 3 by 3, which is the least terme, and the summe is 9, that I doe divide by 1, being the greater terme, and the quotient is 9: so is 9 the least number of the three. When I multiply 3 by 3, whereof cometh 9, and that I divide by 2, and so have I 4.5, which is the greatest number of the three.

Master. Another way yet may you finde the third number in any Progression, if you have two of them: for if the middle number be one of them which you have, then multi-

ply it by it selfe (as in their example, 6 by 6, maketh 36) and that totall divide by the other number which you have, and the third number will be the quotient.

Scholar. When I divide 36 (which cometh of 6 multiplied by it selfe) by 4, the quotient will be 9; and if I divide 36 by 9, the quotient will be 4. But what if I knowe the first number and the third, and would have the middle number?

Master. Multiply the two numbers together, and in their totall you must seek the root of that number, and it shall be the middle number: but because as yet you have not learned to extract Roots, therefore use the first forme which I have taught you, till I teach you to extract Roots. And now goe forward with the answer of the same question.

Scholar. I perceiue then, that the Sonne must not have; of the goods, neither the Mother; nor yet the Daughter; but yet must the goods be divided into such Proportion, that the Sonne shall have 9 Crownes for 6 to his Mother, and the Mother shall have 6 Crownes for ever 4 to her Daughter. When I apply it to the Golden Rule in three examples, as followeth.

Where the first number is the Addition of those three numbers 9, 6, 4: and the third is one of them severally: the second is the totall of the goods in that Testament; and then

by the woorkes of the Golden Rule, I find out the fourth number in every woork: that is for the Sonne 1705, for the Mother 1136, and for the Daughter 757, the which summes added together, doe make the summe of the whole goods, as may be seen by this example.

$$\begin{array}{r}
 19 \text{ } 3600 \\
 9 \text{ } 13600 \\
 16 \text{ } 13600 \\
 6 \text{ } 13600 \\
 19 \text{ } 3600 \\
 4 \text{ } 13600 \\
 1705 \\
 1136 \\
 757 \\
 \hline
 3600
 \end{array}$$

And this (mee thinketh) I doe perceiue, because in this case there is a necessary remedy devised against an urgent inconueni-
ence: therefore those learned men thought they might use the like liberty in that other question.

Matter: Doute good to good, but they had so good reason for them in the one, as they have in the other: As in another example of theirs, it may better appeare, as in this.

A man leaue unto his three sonne 7851 crowns to be parted in such sort, that the first Son should have $\frac{1}{2}$, the second Son $\frac{1}{3}$, and the third Sonne $\frac{1}{4}$, which is not possible: for $\frac{1}{2}$, and $\frac{1}{3}$, and $\frac{1}{4}$, doe make $\frac{13}{12}$, or $1\frac{1}{12}$, that is $1\frac{1}{12}$, so it is more then the whole, but reduce these Fractions into one denomination, the least that they will come to, and they will be

Another question of a Testament.

$$\begin{array}{r}
 26 \text{ or } 13 \\
 24 \quad 12
 \end{array}$$

be $3623 \frac{1}{2}$ and so may you part the goods into
such proportion as these three numerators be
together, that is, the first to have 6 for every 4 to
the second, and the second to have 4 as often as the
third hath 3, and so their portions will be for the
first, 3623 $\frac{1}{2}$, for the second 2415 $\frac{1}{2}$, and for the
third 1811 $\frac{1}{2}$, and these three partes added to-
gether, will make the totall summe of 7850
the whole goods, as you may easily
see in this example.

Another question is there pro-
poned thus.

Another
like questi-
on.

There are 450 crownes to be divided between
three men, so that the first man must have $\frac{1}{2}$ and
the second $\frac{1}{3}$ and the third man shall have
 $\frac{1}{6}$. Scholar. I marvel that any man would
be so overween, to propose that question as a
thing possible, for $\frac{1}{2} + \frac{1}{3} + \frac{1}{6}$ do make 1, that
is almost double the whole summe.



But I perceive it might be thus proposed:
that as often as the first man did receive 30
Crownes, so often the second man should re-
ceive 35, and the third man 27, for 30
is equall to 35, and so is 35
and 3 equall to 27, and so
is 27, and so working the
question the three figures
will appear in this form:
wherby the first mans por-
tion is found to be 200, the
second mans part is

| | | |
|-----|---|-----|
| 11 | Z | 450 |
| 50 | | 200 |
| 112 | Z | 450 |
| 35 | | 140 |
| 112 | Z | 450 |
| 27 | | 108 |

the common number, and the other greater than he: (for two greater, or two smaller, can not well be linked together) and the reason is this, that one greater and one smaller, may be so mixed, that they will make the mean, or common number very well: but two lesse can never make so many as the common number, being taken orderly: no more can two summes greater then the mean, ever make the mean in due order, as it shall appeare better to you hereafter. And as it is of necessity to linke every smaller (once at the least) with one greater, and every greater with one smaller, so it is at liberty to linke them oftner than once, and so may there be to one question, many solutions. When you have so linked them, then mark how much each of the lesser numbers is smaller then the meane or common number, & that difference set against the greater numbers, which be linked with those smaller, each with his match still on the right hand, and likewise the excesse of the greater numbers above the meane, you shall set before the lesser numbers, which bee combined with them. Then shall you (by addition) bring all these differences into one summe, which shall be the first number in the Golden Rule, & the second number shall be the whole masse that you will have all those particulars: the third summe shall be each difference by it selfe, and then by them shall be found the fourth number, declaring the just portion of every particular in that

that nature: As now by these Examples
will make it plaine.

There are four sorts of wine of severall prices, one of 6 pence a Gallon, another of 8 pence, the third of 10 pence, and the fourth of 15 pence the Gallon. Of all these wines would I have a mixture of 1000 Gallons of fifty Gallons, and so the price of each Gallon may be 9 pence. Now demand how much must be taken of every sort of wine to make 1000 Gallons of this mixture.

A question
of mixing
of wines.

Scholar. If it shall please your honor the first example, that I may touch the application of it to the rule, when I trust I shall be able, not only to doe the like, but also to see the reason in the order of the book.

Master, speak then this forme, and the placing of every kind of number in it.

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |
|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|-----|

The proof
of this
Rule.

Q Were you see I have set down the several

nothing A
which is
only 10

all prices, which be 4, 8, 11, 15, and have linked together 6 with 15, and 8 with 11. The common price 9. I have set on the left side, and the difference between it, and every particular price, I have set on the right hand, not against the summe (whose difference it is) but against the summe that is linked withall. So the difference of 15 above 9, is 6, which I have set, not against 15, but 6, that is linked with 15, and the difference between 6 and 9 (that is 3) I have set against 11; For likewise the difference between 8 and 9 is but 1, that I have set against 11, and the difference of 11 above 9 (which is 2) I have set against 8. Then adde I all those foure differences, and they make 12, which I set for the first number in the Golden Rule: the second number I make 50, which is the summe of Gallons that I should have, and the third summe is every particular difference. Now if you work by the Golden Rule; you shall finde the number of Gallons that shall be taken of each sort of Wine: For the better distinction whereof, I have set these letters, A, B, C, D both against the numbers, for which the words doe serve, and over the work also, which severally serve for each of them. And now (if you list to examine the truth of these workings) adde these foure summes together, and they will make 50, that is the totall which I

The proof
of this
Rule.

and the summe of 12 added to 50 will make 62

would be, as by this example you may easily perceive.

And (as to make the
Prices doe agree) do this: mul-
tiply the totall summe 50. by
the common price 9, & it will
make 450 : then keepe that

summe by it selfe, and aftertward multiplie
 ten several hundred of Gallons, by the price
 belonging to the same Gallons, and it shall
 doe agree with this which you have kept first;
 that is your 25; is well done, and there is 5 to
 the number of Gallons of 16 pence price, mul-
 tiply then 25, by 5, and it maketh 125, which
 you shall set downe. Then multiply 125 by 8,
 which is the price for the 125, and so
 number of Gallons; and it shall make 1000
 make 666; so againe multiply 666 by 11, both make 444. And lastly 444 by 12,
 of all, 12, multiplied by 5, maketh 600,
 both 600, and these added together maketh
 450; as in the Example annexed you may
 see, wherefore seeing it hath agreed with the for-
 mer sum of 50, multiplied by 9; I will gladly
 affirm this too; it to be good, and well done.

And now improve what you can do the like, I
propound the same question, and I desire you be
as strict either in the form of combining or linking the
summes.

The varia-
tion of
this questi-
on.

Schole: What shall I proue with your
 hour, & therefore I combine 8 with 15, and 8
 with 11, & then the sozm will be as 5 followeth

| | | | | | | | |
|---|----|---|----|----|----|---|----|
| $\left. \begin{array}{r} 6 \\ 8 \\ 11 \\ 15 \end{array} \right\}$ | 24 | A | 12 | 50 | 12 | Z | 50 |
| | 6 | B | 12 | 87 | 6 | Z | 69 |
| | 3 | C | 12 | 50 | 12 | Z | 50 |
| | 1 | D | 12 | 50 | 12 | Z | 50 |
| | 0 | E | 12 | 50 | 12 | Z | 50 |

Hereby amounteth the same summe in
 totall of the differences as did before: and yet
 now the differences be altered as the com-
 bination is changed, whereof I understand the
 reason by your former work. And therefore
 here appeareth no strange thing, but that now I
 have 8½ Gallons of 6 pence, and 25 gallons
 of 8 pence, and 12 gallons and ½ of 11 pence,
 and so consequently 4 gallons and ½ of 15 pence:
 so that multiplying 8½ by 6, it maketh 50, and then
 25 multiplied by 8, maketh 200, likewise 12½
 multiplied by 11 peeld 137½, and 4½ multiplied
 by 15 maketh 67½, which 4 summes added
 into one, will peeld in the totall 450, which
 agreeth with the multiplication of 50 (being the
 totall summe of gallons) by 9 the common or mean price.

Master. Seeing you conceive this work so
 well, I will propound another example unto
 you of more variety in the Alligations by com-
 binings, as thus:

A Merchant being minded to make a bargain for spices, in a mixt masse (that is to say) of Cloves, Nutmegs, Saffron, Pepper, Ginger, and Almonds: the Cloves being at 6 shillings, Saffron at 10 shillings, Pepper at 3 shillings, Ginger at 2 shillings, and Almonds at 1 shilling.

Now would he have of each sort some, to the value of 300 pound in the whole, and each pound one with another, to beare in price 5 shillings: Now much shall he have of each sort?

Scholar. That will I try thus.

First I set down those six severall prices, and at the left hand I set the common price 5 shillings. Then I linke them thus, 1 with 10, 2 with 6, and 3 with 8: as in the example following.

| | | | | |
|--|----|---|-----|-----|
| | | a | | b |
| | 18 | Z | 300 | 18 |
| | 5 | Z | 83½ | 3 |
| | | b | | e |
| | 3 | c | 18 | Z |
| | 3 | d | 1 | Z |
| | 2 | e | | f |
| | 4 | f | 18 | Z |
| | 18 | 3 | Z | 50 |
| | | | | 4 |
| | | | | Z |
| | | | | 69½ |

Master. I had minded to have combined them in more variety: but I am content to see your own work first, and then more varieties in combination may follow anon.

B b

Scholar.

maistep A
10

Scholar. Then to continue as I began, I
seeke the difference between 1 and 5, (which
is 4) and that I set against 10; then against
1 I set 5, which is the excelle of 10 above 5;
to I gather the difference between 2 and 5,
which is 3, and that I set against 6; because
it is combined with 2; and likewise the diffe-
rence of 6 above 5, (which is 1) I set against
2. Then take I the difference of 3 from 5,
which is 2, and that I set against 8; and be-
fore that 3, I set the difference of 8 above 5,
which is 3. Then gather I all these differen-
ces by Addition, and they make 18, which I
set for my first number in the Golden Rule,
and so appeareth by those works, that of Al-
monds I must take $83\frac{1}{3}$ pound of Ginger
 $16\frac{2}{3}$ pound, Pepper 50 pounds, of Cloves
50 pounds, of Narmegs $33\frac{1}{3}$ $83\frac{1}{3}$
pounds, and of Saffron $66\frac{2}{3}$ $33\frac{1}{3}$
pounds. 150

Then for trial hereof, I mul-
tiply every parcell by his seve-
ral price, as $83\frac{1}{3}$ which is the
summe of Almonds, I multiply
by one which is their price.

300
266
666
1500

Also for the summe of Ginger, I multiply
by 2, which is the price of it: and so each other
in his kinde, as this Table annexed doth re-
present, and then adding them all together I
finde the totall to bee 1500, which also will
amount by the multiplication of the grosse
masse of 300, by the common price 5, where-

And if appeareth well thoughte. Master. Now I will make the allegation to make your counting somewhat better: but because you shall not thinke your selfe pressed so much, I will also note the differences, as by this Example you may see, where I have

| | | A | D |
|-----|----|---|-----|
| 300 | 33 | Z | 300 |
| 37 | 4 | Z | 37 |
| | | B | E |
| 300 | 33 | Z | 300 |
| 63 | 7 | Z | 63 |
| | | C | F |
| 300 | 33 | Z | 300 |
| 45 | 9 | Z | 45 |

alligated 1 with 6 and 8, and therefore have I set against both their differences, that is 1 and 3: all the while, because 1 is combined with 8 and 10, I set before him their differences, 3 and 5. Against 3 I have set onely 5, which is the difference of 10, with whom 3 is combined onely: I likewise have onely alligate to 1, and therefore is the differences of 1 from 5, which is 4, onely set against it: 8 is linked with 1 & 2, and therefore hath set 4 against him, both their differences, 4 and 3: and 10 is joynd with 2 and 3, therefore hath he their differences, 3 and 2. And because of ease for you, in another columnne I have set the differences reduced into one number, for every severall sort,

and have also added them together, whereby appeareth that they make 33. And so consequently you see the works of the Golden Rule set forth. For the six Drugges I have added the letters A. B. C. &c. as before.

Note.

But I would not wish you to cleave still to these elementary aids, but accustom Memory to trust her self: so shall occasion of negligence best be avoided. And as for the proof try it at more leisure, because the time now is short, and you sufficiently instructed in that prooff: And there resteth divers things behinde yet, of which I would gladly give you some taste, before your departure.

Scholar. But if it may please you to let me see all the variations of this question, before you go from it, for me thinketh I could vary it two or thre wayes more yet.

Master. I am content to see you make two or three variations: but I should bee loath to stay to see all the variations, for it may be varied above 300 wayes, although many of them would not well serve to this purpose.

Scholar. I thought it impossible to make so many variations.

Note.

Master. Marvell not thereat, for some questions of this Rule, may be varied above 1000 wayes, but I would have you forget such fantasies till a time of more leisure. And now go forward with some variation of this question.

Scholar. For the first variation, I like the

the first number 1 with 8 and 10, and 2 I com-
bire with 9 and 10 : then joyne I 3 with 6, 8,
and 10, as in this forme.

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| <div> <div> 1
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And so doth there appeare the proportion
of weight for every kinde of Drugg in this
mixture. Now for the triall.

Master. Say say there : you shall not need
to make triall in one example so often, or if
you like to do it by your self, I am content. But
now set forth (for declaration that you con-
ceive the Rule) two or three examples of se-
verall Combinations, and then will we passe
to some other example, and so end this Rule.

Scholar. As it pleaseth you, so will I doe.
And these bee the varieties : in which, as the



combinations are severall, so doth it plainly appear, that the differences by which the proportion of each feberall kinde is taken, are all feberall. And yet I see in the three first of these five varieties, and in the one other before, the totall summe of the differences to be one, that is to say, 18, whereby I perceive that the variety of their mixture doth depend on the variety of their differences severall, and not of the variety of their totall summe,

Master. So is it. And seeing you conceive it so well, I will make an end of this Rule, onely exhibiting unto you one Question or two of the mixture of Metals, that by it you may devise others like, and exercise your selfe therein also, because the use of it serveth often in

in businesse of charge, not so much for Gold-
smiths, as of coyneage in Mints. First, I de-
mand of you this question; If a Mint-Master
have Gold of 22 Kareets, and some of 23 Ka-
reets, some of 24. Again, some 19, some 16, and
some of 18 Kareets, and would mix them, so that
hee might have 100 ounces of 20 Kareets: How
much must he take of each sort?

Scholar. To know that, I answer in order
thus:

| | | | | |
|----|----|-----|-----|-----|
| 15 | 20 | 100 | 20 | 100 |
| 16 | 3 | 10 | 5 | 25 |
| 18 | 4 | 20 | 100 | 20 |
| 22 | 5 | 3 | 15 | 4 |
| 23 | 4 | 20 | 100 | 20 |
| 24 | 2 | 10 | 100 | 20 |
| | 20 | 3 | 10 | 24 |

Master. You have wrought the question
well: but how chanced you made no doubt of
that new name Kareet?

Scholar. Because I thought it out of time
to demand such questions now, seeing you
make so much hast to end: and againe in this
case the proportion of the number is sufficient
for my purpose in this worke, trusting that
another time you will instruct mee as well of
this, as of sundry other things, which as I
have heard you talke of, so I have a great de-
sire to them.

Master. Your answer is reasonable, and
your request and trust (with Gods helpe)

I intend to satisfie. And now to goe forth
with this matter, let me see your examination
of this last worke.

Scholar. First for the one part
I adde together all the particular
summes, as they appeare in the
work, and they make 100, as here
by their Addition doth appeare.

And so it seemeth that the sums
are well gathered: but for the lar-
ther trall of them, I multiply

120 first 20 which is the common or
240 meane summe of the Karects by 100,
360 which is the sum of the whole Masse,
550 which I would have, and it maketh
460 2000. Then I multiply every par-
240 ticular summe by the Karects that it
— doth containe, as 10 by 15, and that
2000 maketh 150.



Likewise I multiply 15 by 16, and it yeeld-
eth 240: so 20 by 18, maketh 360. and 25
by 22, yeeldeth 550: likewise 20 by 23, bring-
eth forth 460: and last of all, 10 multiplied
by 24, yeeldeth 240: which summes all joined
together make 2000, that doth agree with the
like summe before, wherefore I may well say,
that the worke is good. And now (if it please
you) I would set forth some varieties of this
question to prove my self.

Master. Go so, let me see.

Scholar. Here be foure varieties.

And

| | | | | | |
|----|----|---|----|----|---|
| 15 | 34 | 7 | 15 | 23 | 5 |
| 16 | 3 | 2 | 16 | 3 | 7 |
| 18 | 2 | 2 | 18 | 4 | 4 |
| 20 | 5 | 3 | 20 | 5 | 5 |
| 22 | 4 | 2 | 22 | 5 | 4 |
| 23 | 5 | 5 | 23 | 4 | 2 |
| 24 | | | 24 | | |
| 28 | | | 36 | | |

| | | | | | | | | | | |
|----|----|---|----|---|----|----|----|---|---|---|
| 20 | 15 |  | 23 | 4 | 9 | 20 | 15 |  | 4 | 4 |
| | 16 | | 4 | 3 | 16 | | 4 | | 4 | |
| | 18 | | 3 | 3 | 18 | | 2 | | 3 | |
| | 22 | | 5 | 5 | 22 | | 2 | | 2 | |
| | 23 | | 5 | 7 | 23 | | 2 | | 2 | |
| | 24 | | 5 | 9 | 24 | | 5 | | 4 | |
| | | | 36 | | | | | | | |

And more yet could I make, but not like to the number that you speake of in the variation of the other question.

Master. What will I teach you at more les- sure, seeing it is a thing rather of pleasure then of any necessity.

But now for your exercise in this Rule, one o- ther question I will propose. A Mint-master hath six Ingots of silver, of sundry finenesse, some of foure ounces fine, and some of five ounces, some of six, and other of eight, some of 11, and other of 12, and his desire is to mixe 500 pounds weight, so that in the whole masse every pound weight should beare nine ounces of fine silver: How much shall he take (say you) of every sort of silver?

Scholar.

Scholar. To finde out that, I set the numbers thus in order.

And gathering the differences it will appear, that of the first sort there must bee

$43 \frac{11}{13}$ of the second line much: of the third sort $65 \frac{1}{13}$; and of the fourth sort as much: of the fifth sort $195 \frac{2}{13}$, and of the sixth sort $86 \frac{2}{13}$, which in the whole will make 500 pound weight, and in ounces after 9 ounces fine 4500, that is of the first sort $173 \frac{1}{13}$, and of the second sort $217 \frac{2}{13}$, of the third sort $391 \frac{7}{13}$, of the fourth sort $521 \frac{4}{13}$, of the fifth sort $2152 \frac{14}{13}$, and of the sixth sort, $1045 \frac{11}{13}$, which all together do make 4500 ounces, agreeable to the multiplication of 9 by 500.

Master. This is well done of you, therefore now make three or foure varieties, and so an end of this Rule.

Scholar. These foure varieties I set for example.

| | | | | | |
|----|-----|----|----|-----|-----|
| 4 | 3 | 3 | 4 | 23 | 5 |
| 5 | 3 | 3 | 5 | 2 | 2 |
| 6 | 3 | 3 | 6 | 2 | 2 |
| 8 | 3 | 2 | 8 | 2 | 2 |
| 11 | 1 | 1 | 11 | 543 | 113 |
| 21 | 543 | 12 | 12 | 5 | 5 |

Master.

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |

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Master. And by these it appeares, that you can find out more, with which I will not now trouble, save onely (to) to shew you an easie helpe drawing the lines of combination) I will set forth two varieties here.

| | | | | | |
|----|-----|----|----|------|----|
| 4 | 2 | 2 | 4 | 3 | 3 |
| 5 | 23 | 5 | 5 | 23 | 5 |
| 6 | 33 | 5 | 6 | 23 | 5 |
| 8 | 3 | 3 | 8 | 22 | 5 |
| 11 | 543 | 12 | 11 | 43 | 8 |
| 12 | 431 | 8 | 12 | 5421 | 12 |

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And this shall suffice now for the Rule of Alligation or mixture: for by these examples may you easily conjecture such other as do appertaine to it, as well for the one working; as for variety of drawing the lines of Combination.

Scholar. Sir, albeit it pleased you ere-while to put mee from my wishing at the many varieties that may fall in these Combinations, and

and termed them phantasies, yet my phantasie
gibeth mee, that the consideration of this
should in many other examples and cases of
importance be very needfull; and the know-
ledge of it most profitabie: Therefore ye may
well thinke, that at another time convenient I
will request you to aid me herein.

Master. Truth it is, that this consideration
may fall in practice as wel Politick as Philoso-
phicall, and sundry wayes in them be applied:
Therefore when time shall fall fit, for the dis-
cussing of this consideration, you shall not want
my helping hand.



The Rule of Falshood.

The occa-
sion of the
name.



Now will I briefly also teach you
some what of the Rule of False-
hood, which beareth his name,
not for that it teacheth any
fraud or falshood, but for that
by false numbers taken at all adventures, it teach-
eth how to finde those true numbers you seeke for.
Scholar. So might any other Rule be called,
the Rule of Falshood, for they worke by wrong
numbers, and by them finde out the right num-
bers: so doth the Rule of Allegation, the Rule
of Fellowship, and the Golden Rule partly.
Master. In the Golden Rule, the Rule of
Fellow-

Fellowship, and the Rule of Alligation, although the numbers that you worke by, be not the true numbers that you seek for, yet are they numbers in iust proportion, and are found by orderly worke, whereas in this Rule the numbers are not taken in any proportion, nor found by orderly worke, but taken at all adventures.

And therefore I sometimes being merry with my friends, and talking of such questions, to call unto them such children or idiots, as hapned to be in the place, and so take their answer, declaring that I would make them solve those questions, that seemed so doubtfull.

And indeed I did answer to the questions and worke the triall thereof also by those answers which they happened at all adventures to make: which numbers seeing they be taken as manifest false, therefore to this Rule called the Rule of false Positions, and to bytestness, the Rule of Falshood: which Rule for readynesse of remembrance, I have compassed in the few verses following, in forme of an obscure Riddle.

Ghesse at this work as hap doth lead,

By chance to truth you may proceed,

And first work by the question,

Although no truth therein be done.

Such falshood is so good a ground,

That truth by it will soon be found.

From

*From many take too many more,
 From too few take too few also,
 With too much joyne too few again,
 To too few adde too many plain,
 In crosse wise multiply contrary kinde,
 And all truth by falshood for to finde.*

The expo-
 sition of
 the Rule.

The sense of these Verses, and the summe
 of this Rule is this. When any question is proposed, happen what
 will, firste firste imagine a number as that, you
 list, which you shall name the *first position*, and
 put it in stead of the *maine number*, and then
 work with it as the *question* directs you, and if
 you have miste, then is the *first error* of that
 worke either too great or too little: that shall
 you note as hereafter shall be taught you, and
 you shall call it the *first error*.

Then begin againe, and take another num-
 ber, which shall be called the *second position*,
 and worke by the *question* as you have miste
 againe, note the excelsse or default as in it, and
 call that the *second error*. Then multiply
 crosse-wise the *first position* by the *second error*,
 and againe the *second position* by the *first error*,
 and note their totalls severally by the names of
totalls: Then marke whether the two errors
 were both alike, that is to say, both too much;
 or both too little: or whether they be unlike,
 that is, the one too much, and the other too
 little:

little : for if they bee like, then shall you subtract the one totall from the other, I meane the lesser from the greater, and the remainder shall be your Dividend : so must you abate the lesser error out of the greater, and the residue shall bee the Divisor. Now divide the Dividend by that divisor, and the quotient will shew you the true number that you seeke for. But, and if the errors be unlike, then must you adde both those for all (which you noted) together, and take that whole number for the dividend so that you adde both errors together, and that whole number shall be the Divisor, and the quotient of that Division shall give you the true number that the question seeketh for, and this is the whole Rule.

Scholar. This Rule seemeth to untie any other, that without some example I shall not easily understand it.

Master. Verily a good will : I propose halfe a score sundry questions and examples of variety for the better understanding of the worke hereof : and for the first, take this example.

A Mason was bound to build a wall in 40 dayes, and it was covenanted so with him, that every day that he wrought, he should have for his wages 2 shillings 1 penny, and every day that he wrought nor, he should be amerced 2 shillings six pence, so that when the wall was made, and the reckoning taken of the dayes that he wrought, and of the other that he wrought nor, the Mason had clearly but five shillings five pence for the worke. Now

A question
of Mason-
ry the first
example.


do

doe I demand how many dayes did hee worke of those 40, and how many did he not worke?

Scholar. I pray you expresse the order of the worke, that I may partly by imitation, and partly by comparing it with the Rule, be able again to do the like.

Master. This order shall you keepe in the work of this Rule: First take some number (as you list) at adventure: as for example, I say he played 12 dayes, and wrought 28 dayes. Now cast you the wages of every day, and see whether it will agree with the summe of 5 shillings 5 pence.

Scholar. The 28 dayes that he wrought after 25 pence the day, yeeldeth 700 pence: When 12 dayes that he wrought not, at 30 pence each day, doth amount to 360 pence, which if I abate out of 700 pence, thereresteth 340: but you say he had not so much.

Master. He had but 65 pence, and by this supposition he should have had 340: therefore is this summe too much, by 275, which summe I must set downe after this sort, as you see here, where first I have made a crosse (commonly called S. Andrews crosse) and at the over corner on the left hand I have set the first position 12: and at the other corner under it I have set 275, which is the first errour, with this figure , which betokeneth too much, as this line ———— plaine without a crosse line betokeneth too little.

On the right hand of the crosse I have left two like roomes for the second position and his error. Therefore to prosecute the worke, I suppose he played 16 dayes, and wrought 24.

Scholar. I was a while in doubt why you named the dayes of his working, seeing they be not set in the figure: and I doubted how you knew them, or else whether that you did suppose them at all adventures, as you did the dayes that he played: but now I gather, that seeing 40 dayes is the whole time limited, then the dayes that he played being supposed, the rest of 40 must needs be the dayes that he wrought; and therefore 28 followed 12 of necessity; and 24 followeth 16 also of necessity; but yet I scarce perceive why you set not in the figures as well 28 as 12, as well 16 as 24.

Master. It forceth not which of them I take, so that in the second position I take the numbers of the same nature that is here both of working dayes, or both of idle; but now examining you this second position.

Scholar. If he played 16 dayes, then abating 16 times 3 pence, the sum will be 480 pence, and for 24 dayes that he wrought, every day yielding 25 pence, the total is 600 pence; so that abating 480 out of 600, thereremeth 120; and as you say, it should be but 65: therefore it is too much by 55: that must be set on the right hand of the figure, at the neather part, and over it on the same side 16, which is the second position, thus.

NOTE

C c

And

12

16

X

27551

And as I gather by your words, it shal be all one if I did set 28 in stead of 12, and 24 in stead of 16, out of all the wayes of proportion. Master, So were it. But this shall you marke, that, of what nature soever the two positions bee, of the same nature shal be quotient. Therefore when the positions in this question are 12 and 16, which both being numbers of the playing dayes, the quotient shal declare the true number of playing dayes: whereas if the positions had been 28 and 24, which were supposed to bee the working dayes, then should the Quotient declare the true number of the working dayes, and not of playing dayes, as it will be now. And therefore to continue the work of this question, and to finde the true number of playing dayes, I must multiply crossewise the first position by 55, that is the second error, and the totall will bee 660. Then I multiply 275 and 6, and it yeeldeth 4400. Now because the errors are alike, that is to say, both too much, I must subtract 660 out of 4400, and so remaineth 3740, which is the dividend. Again, I must subtract the lesser error 55 out of 275, that is the greater error, and there will remaine 220, which will bee the divisor: then dividing 3740 by 220, the quotient shal bee 17. Wherby I say now constantly, that 17 is the exact number of dayes that the Mason played, and it shal followeth that he wrought 113 dayes, and this is the question answered.

on R

3 3

Now

The proof
of this rule

Now for the order of the whole of this worke, there
is enough to be said, but only this, no worke
with this number according to the question; and if
it agree, then appeareth the number to be as that
a man would have.

And here now seeing he wrought 23 dayes,
and must have for every day 25 pence, the
whole summe cometh to 575. Then againe,
seeing hee played 17 dayes, and must have 30
pence for every day, the whole summe of the
abatement will be 510. Therefore I subtrah
510 out of 575, and there will remaine 65,
which is the same as 5 shillings 5 pence, the cleere
wages of the Mason for his worke, according
to the question.

Scholar. Now I trust I understand the
worke and the rule so well, and the better by
this proof, that I can be able to doe the like:
And for a proof, I take the same question, all
save the last number, where I will suppose that
he had 10 shillings for his wages cleere. And
now to chesse at the number of the dayes hee
wrought, I suppose first that he wrought 20
dayes, then for 20. If he wrought 20 dayes, his
wages must be 500 d. then hee should have played other
20 dayes, for which must be abated 600 d. and
then hee leaveth 100 d. And so am I at a stay,
for it is not like to your former worke.

Master. You should have required of mee
some question, and not have taken a question of
your owne phantasying, untill you were more
expert in this Art, for so might you as well

happen to an impossible question, as an impos-
sible; but now to go forward, consider that this
number is too little by 220, seeing he should
gain by your supposition 120 pence, and in
this position he loses 100, these both make
220, which you shall see coming to the first er-
ror, with this sign $\frac{1}{2}$, before him 100 like,
as here it is to, and the result is 20
and both appear.

And now for the toll gate
to turn your life once a
day.

Scholar. As my errour hath misled my
folle, so it hath pleased me better under
standing.

Now therefore considering this position,
not to solve the question, I take another, sup-
posing cost be wrought 20 dayes. Even so,
his wages he must be allowed 750 pence, and
for the 20 dayes which he wrought not, he
must have 300 pence, and so remaineth still
450 pence, but it may be offered 120 pence,
therefore it is too much by 330, which I set
downe in the figure with the 20, and position
and his error, and the figure presently thus:
Now to this, I multiply the 20 by 20, and
that makes 400, and the 20 by 20, and
it will be 400.

36 by 240, and it will be
in 6600, and before it
shall subtract the one out of the other, there
will

will remembre nothing to bee the Dividend.

Master. In this you forget your selfe again; for in as much as the signes in the errors be unlike; therefore must you worke by Addition, adding together those two totalls to make the Dividend; and also adding the two errors to make the Divisor. And because you shall no more forget this part of that Rule, take this by rote remembrance.

Unlike require Addition.

And like desire Subtraction.

Scholar. You meane, that if the errors have like signes, then must the Dividend, and the Divisor be made by Subtraction, as is taught before: And if those signes bee unlike (as in this last example they bee) then must I by Addition gather the Dividend and the Divisor. Therefore must I adde 6600 to 6600, and it will bee 13200, which will be the Dividend. Then againe I adde 220 to 330, and it will be 550, which must be the Divisor: wherefore dividing 13200 by 550, the quotient will be 24, whereby I know that the Mason wrought 24 dayes, and then it followed, that he played 16 dayes.

Master. Examine your worke, whether it be agreeable to the question or no.

Scholar. For 24 dayes worke, the wages must be 600 pence, and for 16 dayes which the Mason wrought not, there must be abated 480 pence, and then remaineth cleare to the

Mason 120, and the question importeth to be answered: for it is evident that 24 is the true number of dayes that he wrought.

Master. Although you seeme now to understand this worke, yet to acquaint you with the better with the new Trade of this Rule, I thinke it good to propose to you 5 or 6 examples more before I make an end of the first lesson.

Scholar. Sir, I thanke you that you would consider my commodity and profit in knowledge, for undoubtedly it is practice and exercise that maketh men prompt and expert in every kinde of knowledge.

Master. You say well, so that they follow some certaine precepts to governe and rule their practice by, else may practice procure custome of error, and a repugnance to exactnesse of knowledge: namely, as long as the error is not plainly known to the vulgar sort. But to retorne to your work.

A question
of wares,
the second
example.

There is a servant that hath bought of Velvet and Damask for his master 40 yards, the Velvet at 20 shillings a yard, and the Damask at 12 shillings, and when hee cometh home, his Master demandeth of him, how much he hath bought of each sort: I cannot tell (saith hee) exactly: but this I know, that I paid for Damask 48 shillings more then I paid for Velvet: now must you ghesse how many yards there is of each sort.

Scholar. Although the ghesse seemeth difficult, yet I will prove what I can doe: for I remember your saying, that it soareth not how

bein said of false the ghesse bee, so it bee some-
what to the question, and not an answer of a
contrary matter.

Therefore first I imagine that he bought 20
yards of Damask, for which he should pay af-
ter the former price 240 shillings: then must
hee needs have of Velver other 20 yards, (to
make up the 40 yards) and that would cost 400
shillings. So that the totall of the price of the
Damask is lesse then the summe paid for Vel-
vet 160 shillings, and should bee more by 48.
Therefore the first errorr is 208, too little.
Then begin I againe, and suppose he bought
of Damask 30 yards, that cost 360 shillings,
then had he but 10 yards of Velver, which
cost 200 shillings: and now the price of the
Damask is greater then the price of the
Velvet by 160 shillings, and should bee but
48, therefore is the second errorr 112 too
much, which I set in forme of figures, as here
doth appeare. Then doe I
multiply in crosse wayes
208 by 30, and the summe
will be 6240. Also I mul-
ply 112 by 20, and there
will amount 2240. And in as much as the
signes of the errorrs be unlike, I know I must
worke by Addition, therefore adde I these
two totalls together, and they make 8480,
which is the Dividend: then adde I also the
two errorrs together, 208, and 112, and they
make 320, which is the Divisor: wherefore

$$\begin{array}{r}
 20 \quad 30 \\
 \times \quad \times \\
 \hline
 208 \quad 112
 \end{array}$$

dividing 3480 by 320, the quotient will be 10 1/2, which is the true summe of yards of Damask that he bought, and in velvet 13 yards 1/2, and that appeareth by examination, thus: 26 1/2 yards of Damask at 12 shillings the yard, maketh 318 shillings: then in Velvet he had but 13 yards and 1/2, and cost 270 shillings, at 20 shillings the yard. Now subtract 270 out of 318, and there will remaine 48, which is the number of shillings that the Damask did cost more then the Velvet.

Master. Now shall you have a question of another kinde.

A question
of debt,
the third
example.

There are three men that do owe money to me, and I have forgotten what the totall summe is, and what the particulars be.

Scholar. Why, then it is impossible to know the debt.

Master. Hence, you are too hasty, there is more helpe in it then yet you see. I have three severall notes, whereby it appeareth that I did conferre their debts together, and found the debt of the first and the second to amount to 47 pound, the debt of the first man and the third man did make 71 pound, and the second man his debt with the third, did rise to 88 pound. Now can you tell what every man did owe, and what was the whole summe?

Scholar. Nay, in good faith: but as I perceive that it must bee found by conjecture, so will I ghesse at it, supposing that the first man did owe 20 pound, and the second man 30, and the third ———,

Master.

Master. Nay stay there, you are too farre gone already: you may not suppose a febeall summe for every man; for it is enough to suppose one summe for the first man, and let the other follow the question imposseth. Wherefore sayd you let the first man his debt to bee 20 pound, the second man cannot owe 30 pound, for the declaration is, that their debts added together did make 47 pound, so must the second man his debt bee but 27 pound. Now the second debt with the third, must make 88: therefore subtract 27 out of 88, and there will remaine 61, as the third man his debt. Then saith the declaration, that the first and third mans debts do make 71: but by this supposition they make 81, that is 10 too much, which I must set for the first error. Now woike you the second position.

Scholar. I suppose the first mans debt to be 24 pound: then must the second mans debt (by your declaration) be but 23 pound, seeing both they make but 47 pound. And the second man his debt with the third, doe make 88 pound, and the second man oweth but 23: therefore the third man must owe 65 pound. Now the third mans debt with the first, should make by the declaration 71 pound, and they doe make 89 pound, that is 18 pound too much, and that is the second error, which I set downe with the first, and their positions in this forme, and then I doe multiply in crosse wayes 20 by 18, and it is 360.
And

And 10 by 34 maketh 340. 104. 15. 24.
 Also because the signes of the
 the xious be like, I must
 work by subtraction there
 104. 15. 24. I subtract 240 out of 360, and there re-
 steth 120, which is the Dividend: then I
 subtract 10 out of 18 by the same reason, and so
 is the Divisor 8, which is found 15 times in
 120: therefore I say that the first man did owe
 15 li. and then the second man must owe 32 li.
 for those two do make 47 li. and the third mans
 debt is 16: so much remaineth if I abate
 15 out of 71. or if I take 32 out of 88.

The
 fourth ex-
 ample.

Master. For the fourth example take this easie
 question for the variety in work. Two men having
 severall summes, which I know not, do thus talke
 together: the first saith to the second, if you give
 me 2 shillings of your money, then shall I have
 three times so much money as you. The second
 man answereth: It were more reason that our
 summes were made equal, and so will it be if you
 give mee 3 shillings of your money. Now geve
 what each of them had.

Note.

Scholar. I imagine that the first had 9 s.

Master. Consider evermore in your imagi-
 nation that you take a likely summe, as in this
 question, take such a summe, that having 2 ad-
 ded unto it, may bee divided into three parts
 even.

Scholar. Why? I remember your saying
 before, it soareth not how fondly soever I
 guessed.

Master.

Master. As for the possibility of the solution on, it is truly: but for easiness in thought, the aptest numbers are most convenient.

Scholar. I thought no lesse, and therefore I took 9 for an apt number to be parted into threes: but I perceiue I should haue considered the aptnesse of that partition after the addition of two unto it, and then 7 had been more meete.

Master. What is truth, and then should the second man his summe be 5: for although he hath not but the third part of 9, that is 3, yet you must remember that he lent the first man 2, and so had he 5.

Scholar. Then to go forward: if the second man had threes of the first man, then should hee haue 8 and the first man but 4; so hath he double to the first man, yet he said in the question they should haue equal: wherefore it appeareth that he hath 4 too much.

Wherefore I note that error with his supposition, & ghesse again that he hath 10 shillings: whereunto I adde 2 shillings borrowed of the second man, and then he hath 12: so the second man hath remaining but 4, whereunto if I adde the 2 that he lent to the first man, so had he 6 at the beginning.

When taking 10 from the first man, and giue to the second, then hath the first man but 7, and the second hath 9, which are not equal, but there are 2 too



many

many, wherefore I set downe both the positi-
ons with their errors, as before you set, and
multiply a crosse, so cometh there 40, and 14,
and because the signes bee like, I take 14 out
of 40, and so resteth 26 to be divided & there
likewise I take 2 out of 26, and there resteth
2, by which I divide 26, and the quotient
will be 13, which is the summe that the first
man had. And so appeareth that 2 being added
thereto, the summe will be 15, so hath the se-
cond man but 5, and before he had 7, there-
fore take 3 from the first, and put to his 7, and so
have each of them 10, and that is equal as the
question would.

The fifth
example:
a question
of Lambs.

Master. For the fifth example, take this questi-
on. One man said to another, I think you had this
year two thousand Lambs: so bad I said the o-
ther; but what with paying the tythe of them, and
then the severall losses, they are much abated:
for at one time I lost halfe as many as I have now
left, and at another time the third part of so ma-
ny, and the third time $\frac{1}{4}$ so many. Now guesse you
how many are left.

Scholar. Because here is mention made of
certaine parts, I must take a number that
may have all these parts, that is to say, 12, and
 $\frac{1}{4}$ which will be 24, both be it with the same
parts. Wherefore I take 24 to bee the
number that doth remaine, so hath he lost 6, 4,
and 3, that is 13, and the whole 23, but it should
be 2000.

Master. We are deceived yet. Till you have

A caution
to the
reader
of the
book.

And multiply in cross 12 24
ways 1775 by 24, where
of cometh 42600. Also I
multiply 1750 by 12, and
there cometh 21000. And

And now doth there come a question to my memory which was demanded of me, but I was not able to answer to it: and now methinketh I could solve it,

Scholar.

A question
of sheep
and tillage,
the sixth
example.

Scholar. There is supposed a Law made, that
(for furthering of tillage) every man that doth
keep sheep, shall for every ten sheep, ear and sow
one Acre of ground: and for his allowance in
sheep pasture, there is appointed for every foure
sheep one Acre of pasture. Now is there a rich
Sheep-master which hath 7000 Acres of ground,
and would gladly keep as many as hee might: by
that Statute I demand how many sheep shall he
keep?

Master. Answer to the question, your self.

Scholar. First, I suppose hee may keepe
500 sheepe, and for them hee shall have in
Pasture after the rate of foure sheepe to an
Acre, 125 Acres, and in Arable ground, 625
Acres, that is, 175 in all: but this error is
too little by 6825. Therefore I challenge in
that he may keepe 1000 sheepe, that is in pa-
sture 250 Acres, and in tillage 100 Acres,
which make 350, that is, too little by 650.
Both these errors with their positions, I set
downe as you see, and multiply them cross
6825 by 1000, and it maketh 6825000, also
I multiply 66650 by 500 and there cometh
33325000, which summe
I subtract out of the former, and there remai-
neth 3500000 for the Dividend: likewise I
subtract the lesser error out of the greater
and there resteth 175, by which I divide
3500000 (the Dividend aforesaid) and
the

the quotient will be 20000, so that by this Rule
that both 700 Acres of ground may keep
20000 sheep.

Master. You have done well, notwithstanding
say both this last question, and the next before
might be wrought without the second positi-
on by the Rule of Proportion, as this: When
in this question you found in the first error
that for 500 sheep there
might be 175 Acres; then 175 \times 500
might you reduce it to 7000 \times 2000
the Golden Rule, thus:

If 175 Acres will admit in allowance 500
sheep, then 7000 Will have 2000. And so by one
position, with the help of the Golden Rule, may you
answer this question.

And thus for the question of Lambs, when
you had found that 12 rains of 25, you might
have for the figure as followeth, and have
said:

12 \times 25 = 300
1800 \times 12 = 21600
864
If 25 do leave but 12,
what shall 1800 leave?
and it would appear to be
864.

Scholar. Sir, I thank you for this aid,
for it doth much shorten the worke of this
Rule.

Master. Yet againe, I will shew you an
other way to answer to this last question with-
out the Rule of false position, and that by
the Rule of Fellowship, for it appeareth in
the propounding of the question, that ten sheepe
must

Another
way of
working.

Another
way yet.

must be in pasture two Acres and $\frac{1}{2}$ and for
 them must there be eared but one Acre, so it
 followeth, that for 2 Acres eared, there must
 be 5 set to pasture: and if you put them both
 into one summe, they will make 7. Therefore
 look what proportion 7 being this totall, both
 beare to 5, and to 2, such proportion shall any
 totall in this question beare to the pasture
 ground, and the eared ground.

Scholar. This I ordeeth wondrous aptly.
 Therefore to probe it, I demand this by the
 former supposition: If a man have 300 Acres,
 how much shall he leave in pasture, and how
 much shall he turne to tillage? You say, that
 as 7 is to 5, so shall 300 be to the Acres of pa-
 sture: and as 7 is to 2, so is 300 to the Acres
 of tillage: whereof for both I have set exam-
 ples here following, where
 by appeareth that of Pa-
 sture, there shall bee 214 $\frac{2}{3}$ Acres, and of Tillage
 85 $\frac{1}{3}$, which both summes
 added together doe make 300.

Another
 question,
 the seventh
 example.

Master. Now take another Example: A man
 hath three silver Cups with a Cover, the Cover
 weigheth 18 ounces, the second cup weigheth even
 halfe the weight of the first and the third. Now if
 the cover be put to the first Cup, they weigh just as
 much as all the three Cups do weigh: and if the
 cover be joynted with the second cup, they weigh
 much as the second twice, and the third, and if the
 Cover

Cover be put to the Cup, they will make twice as much as the first and second Cup. Now try you what was the just weight of every Cup.

Scholar. I doe set the weight of the first Cup to be nine ounces, then inas much as these two (that is to say, the cover and the first Cup) do weigh the weight of the three Cups, I see that the three Cups must weigh 27 ounces, for so much is 18 and 9. Also because the first and the third do weigh double so much as the second, therefore it is the third part of that weight, that is 9, and then would it follow, that the third Cup also should weigh 9 ounces; but then the question saith, that the Cover being joynd to the second Cup, they weigh as much as the second twice, and the third once, that should bee 27, and so it doth; that being joynd with the third Cup, they should weigh twice as much as the first and the second, that should bee 36, and they weigh but 27, so is that error 9 too little. Then begin I againe, and say, that the first Cup doth weigh twelve ounces which I joyne with the Cover, and they make thirty ounces: then seeing the second is of that weight; it must needs weigh ten ounces, and the third must weigh 8 ounces, seeing the first and the third must weigh 20 ounces. Now put I the Cover to the second Cup, and they weigh 28 ounces, which should be even so: then joyne I the Cover with the third Cup, and so should it weigh twice the first, and the second, that is 44 ounces, and they

do

weigh

weight but 26, that is 18 too
 little : those errors with
 their positions I set downe,
 and multiply in crosse-wayes
 9 by 12, whereof cometh
 108 : Also 9 by 18, and that yeeldeth 162 :
 and in as much as the signes bee like, I abate
 the lesser out of the greater, and there doth re-
 maine 54. When doe I also abate the lesser er-
 rour from the greater, and so remaineth 9, by
 which I divide 54, and the quotient is 6,
 which I take 10; the true weight of the first
 Cup, which being ioyned with the Cover, must
 weigh as much as the thre Cups, so doe they
 weigh but 24 ounces. When seeing the second
 Cup is the thirde part of that weight, 10; the
 other two Cups (you say) must weigh double
 his weight, the weight of the second Cup is 8
 ounces, and so the weight of the thirde Cup
 must be ten ounces. Now put the Cover to
 the second Cup, and it will make 28 ounces :
 that must be the weight of the second twice,
 and the thirde once, that is, twice 8, and once
 10, and so is it. Again, put the Cover to the
 thirde Cup of 10 ounces, and they must weigh
 twice as much as the first, and the second, that
 is, 28, and so is all agreeable.

Master. When answer to this Question.

A question
 of water :
 the eight
 example.

There is a Cisterne with foure Cocks, contain-
 ing 72 barrells of water : and if the greatest
 Cocke be opened, the water will avoide cleane in
 six houres ; at the second Cock it will ask eight
 houres :

hundred: as the third Cock is will avoid in no lesse then nine houres: and as the smallest it will require twelve houres: Now I demand in what space will it avoid, all the Cocks being set open?

Scholar: First, I imagine it will avoid in two houres.

Master: They must there avoid by the first Cock, of the water, that is 24 Barrels, and by the second Cock, that is 18, and by the third Cock, that is 16 Barrels, and by the smallest Cock, that is 12 Barrels, all which summes put together, do make 70, as by their Addition it doth appent, but it should be 72; therefore the error is too few.

Scholar: When will I begin again by your favour, because I thinke I understand the work, and put three houres for the due time: so shall there run out at the greatest Cock, that is 36 Barrels, and at the second hole, that is 27, and at the third Cock, that is 24, and at the smallest hole, that is 18 Barrels, which all together do make 105, and should be but 72, so is it too much by 33: therefore doe I set the errours in order of the signes with their positions, and worke by multiplication, in eache saying, two times 3 is 6, and two times 33 maketh 66, and because the signes are unlike,



I must adde these two totalls together, which make 72: also I adde the two errors, and they make 35, by which I diuise 72, and the Quotient riseth $\frac{2}{3}$, whereby I see that all the Cocks being set open, the water will aboide in two houres, and $\frac{2}{3}$ of an houre.

Master. This exercise maketh you to grow expert in the Rule. Therefore I will inuade you somewhat more with a question or two.

A question
of part-
ners.

The ninth
example.

There were two men that had been partners, and had in account betweene them 300 Duckets; whereof the one should haue for his part 180, and the other 120: but in the parting of them, they fell at variance, so that each of them catched as many as he could: yet afterward being reconciled they agreed that he which had gotten most part of them, should lay downe $\frac{1}{4}$ of them againe, and he that had gotten least, should lay downe $\frac{1}{4}$ of those which he had taken, and then parting them into two equall parts, each man to haue halfe thereof, and so had they their just portions, as they ought: now I demand of you, what each of them had gotten by the scrambling?

Scholar. I suppose hee that had least, got 108 Duckets, then the other had 192: wherefore in laying downe againe of the 192, there was put downe $\frac{1}{4}$, that is, 144, and so hee had left but 48. Also of the 108 there was laid downe $\frac{1}{4}$, that is, 27, and so hee had left 81. When I put together 144 and 27, and it maketh 171, which I part into two parts euen, and so commeth 85 to be giuen to each of them, which

which summe put to 72 maketh 12, and for
new to 148, it maketh 238: and now I doubt
both I shall go forward.

Master. You need not to take but one of Now.
them, which you list, the greater or the smal-
ler, for all cometh to one purpose: and so
may you compare it that you take to any of the
other summes, remembryng that you make
comparison to the same in the second worke
as for example of the first part. If you com-
pare 138 with the lesser summe one, that is
120, so is it 18 too much; and if you compare
it with the greater summe, then is it 42 too
little. Again, if you compare 162 to the grea-
ter summe, the error will be 18, as it was in
the other: but it will have a contrary signe:
and if you compare it with the lesser summe,
it will be 42 too much: so that the error both
wayes is either 18, or 42: and as for the signes
it little so ceth, for in them is nothing consi-
dered here, but likenesse and unlikenesse, which
in this case doth neither further or hinder:
But now go on with the worke.

Scholar. If it be so, then am I out of my
greatest doubt. When I soune that 90 (which
I found as the halfe of the latter partition) was
to 48, which is left with the one man, and so
hath be 38, which (I may say) is 18 too ma-
ny, for the least should be but 120, that error
do I note, and then make a new position, sup-
posing the one man to have 204, and the other
to have 96: wherefore of the 204, there
must

must be laid downe 153, and so remaineth
with him 5. Also of the 96, there must be
laid downe 32, and so resteth with that
man 64. Now of the 153 and 32, I make one
summe, as 185, which I must divide into two
equall parts, and so each man shall have 92½,
whereunto if I adde their former portions re-
served, then the one shall have 156½, and the
other hath 143½. Wherefore take the lesser
summe now againe as I did before, that is,
143½, and finde that he hath too many by 23½
for he should have but 120, and so have I found
my two positions two errors, which I set down
as heretofore bee seene, each error under his po-
sition, and then by the Rule I doe multiply in
crosse wayes 108 by 23 which shal be 2484, and
there resteth 1438, which I note, then againe
I multiply 96 by 18, which shal be 1728, and
thereof abundanteth 18, which I note. Now
because the signes are both like, that
is, both too many, I must worke by Subtra-
ction, and so abating 1728 out of 2484, there
will rest for the Dividend 756: then for the
Divisor I subtract 18 out of 234, and there re-
maineth 216, by which I divide 756, and the
quotient will be 3½, which is the just por-
tion of him that had the least summe. And if I
doe subtract it out of 300, being the totall
summe, then will there remaine 150, as the
portion that the other did get.

Master.

Master. For the prooſe of this worke, you may chuse whether you will examine thoſe numbers according to the formes of the queſtions, or elſe worke by other two poſitions, for to finde the ſecond numbers: and if thoſe poſitions bring the ſame numbers that did amount by the two firſt poſitions, then both each worke confirme other.

Note,

Scholar. By your patience, I will probe both wayes, not onely to ſeeke their agreement, but alſo to accuſtome my mind to thoſe worke, for I perceiue it is exerciſe that muſt bee the chiefe engraver of theſe Rules in my memory.

Master. You conſider it well: then go to.

Scholar. Firſt, I will by two other poſitions, try to finde the portion of him which had moſt.

Master. Although you may doe it with any poſitions, yet to ſee the agreement of your worke the better, take the ſame poſitions that you did before; comparing them now to the greater, as you did before unto the leſſer.

Scholar. When I ſuppoſe that he that had moſt, had 192, ſo had the other 108. Now if I take $\frac{1}{2}$ out of 192, that will be 144, and there will reſt to that man but 48. And from the ſecond which had 108, if I take $\frac{1}{3}$, that is 36, there will remaine to him 72: then joining 144 with 36, it will make 180, the halfe whereof being 90. If I adde to each of thoſe

two mens portions remaining with them, the one shall have 138, and the other 162, of which two I take the greater (that is 162) & see it to be 18 too few; for it should be 180, that error I note under this position. Then for the second position, I take (as I did before) 204 for the one, and so resteth 96 for the other: then take I $\frac{1}{2}$ of 204, and it will bee 153, and there resteth to him 51. Also of the 96 I take $\frac{1}{3}$, that is 32, and there remaineth to him 64; now put I that 32, to 153, and it yeeldeth 185: which being parted in equall values, maketh $92\frac{1}{2}$ to be added to each mans remainder, and so the one hath 143 $\frac{1}{2}$, and the other 156 $\frac{1}{2}$: wherefore I take the greatest summe, and it is 23 $\frac{1}{2}$ too little, that do I note also, and set both these errors under their positions, as in this Example following doth appeare.

And then multiplying 102 by 23 $\frac{1}{2}$, there doth arise 4512.

Again, I multiply 204 102 204
by 18, and it maketh 3672,
which I do subtract out of
4512, because the signes 18 23 $\frac{1}{2}$
be like, and there resteth
840 for the dividend, then subtracting 18 out
of 23 $\frac{1}{2}$ there will remaine 5 $\frac{1}{2}$, which I must
take for the Divisor. And so dividing 840 by
3 $\frac{1}{2}$ the quotient will be 152 $\frac{1}{2}$, whereby I have
found an agreeable summe to that which I
found by the former positions, for him that had
most

most which I doe subtract out of 300, that is the totall, there will rest 147 $\frac{1}{2}$, which was the portion of him that had the least part.

Master. So by others positions, you see that one doth confirme the work of the other. Now examine those two numbers by the forme of the question and so shall you probe your work good also.

Scholar. If that hee which gat most, had 152 $\frac{2}{3}$, then must he lay downe $\frac{1}{3}$ of this sum. What is 114 $\frac{2}{3}$, and so shall remaine with him but onely 38 $\frac{1}{3}$. The other which had least, that is 147 $\frac{1}{2}$, must put downe of his sum $\frac{1}{2}$, that is 49 $\frac{1}{2}$, and so doth there remaine with him yet 98 $\frac{1}{2}$. When do I add together 114 $\frac{2}{3}$, and 49 $\frac{1}{2}$ and it will make 163 $\frac{1}{6}$, which I must part into equall parts, and that will be 81 $\frac{1}{6}$, to be given to each of them: putting 81 $\frac{1}{6}$ unto 38 $\frac{1}{3}$, there doth amount 120 $\frac{1}{2}$, which is the true portion of him that should have the lesser sum: and adding 81 $\frac{1}{6}$, 98 $\frac{1}{2}$, the totall will be 180, the true portion of the other. And so is the work by this proof also tried to be good. And this I mark by the way, that in their scambling, hee got most (as it chanceth often) that ought to have had least by just partition.

Master. Let your study be to learn truth and just Art of Proportion, and to distribute and part according therunto, as often as occasion shall bee ministered. And here would I make an end of this Rule, save that I remember one pleasant question, which I cannot over-
 passe,

parte, which I will declare somewhat largely because you shall as well understand some reason in the pleasant invention, as apt proceeding in the witty working thereof.

The tenth
example of
gold and
silver.

Hiero King of the Syracusans in Sicilia, had caused to be made a Crown of Gold of a wonderfull weight; to bee offered for his good success in wars: in making whereof the Goldsmith fraudulently tooke out a certaine portion of Gold, and put in Silver for it, so that there was nothing abated of the full weight, although there was much of the value diminished.

Which thing at length being uttered (as no child can alwayes be hid) the King was sore moved: and being desirous to try the truth without breaking of the Crown, proponed the doubt to Archimedes, unto whose wit nothing seemed impossible, which although presently he could not answer unto, yet he had good hope to devise some policy for that invention, and so musing thereon, as he chanced to enter into a Bath full of water to wash him, he observed, that as his body entered into the Bath, the water did runne over the Tub, whereby his ready wit, of such small effects conjecturing greater workes, conceived by and by a reason of solution to the Kings question, and therefore rejoycing exceedingly, more then if he had gotten the Crowne it selfe, forgot that he was naked, and so ranne home crying, as he ranne, *Eureka, Eureka*. I have found, I have found: And thereupon caused two masse pieces,

Archimedes
discovered

pieces, one of gold, and another of silver, to
bee prepared, of the same weight that the said
Crowne was at: and considering that gold
is heavier of nature then silver, and there-
fore gold of like weight with silver, must
needs occupy lesse room, because it is more
compact and sound in substance, hee was as-
ured that putting the masse of gold into a ves-
sell bym full of water, there would not so
much water runne out as when hee should put
in the silver masse of the like weight. And here-
fore hee tried both, and noted not onely the
quantities of the water at each time, but also
the difference or excelle of the one above the
other, whereby he learned what proportion
in quantity is betwixt gold and silver of
equall weight. And then putting the Crowne
it self into the vessell of water bym full (as
before) marked, how much water did run out
then, and comparing it with the water that
ranne out when the gold was put in, noted
how much it did exceed that: and likewise com-
paring it to the water that ranne out of the
silver, marked how much it was lesse then
that, and by those proportions, found out the
just quantity of gold that was taken out of
the Crowne, and how much silver was put
in stead of it: but seeing Virginius to which be-
teth this History, doth not declare the particu-
lar woordes of this trial, it shall bee no incon-
venience to suppose an example for declarati-
ons sake, wherein although the true and just

posse

pro-

Proportion be not expressed, yet the forme of trial shall be truly set forth. And for an example, I suppose the weight of the Crowne to be 8 pound, and so of each the other two Masses. And when the Masse of Gold was put into the water, I imagine, that there ranne out two pound of water: and when the masse of silver was put in, I suppose there ranne out three pound. Again when the Crowne was put in there ran out two pound $\frac{1}{2}$. Now to know what quantity of silver was in the Crowne, work by the Rule of false position, and imagine that there was two pound of silver, then must there be six pound of gold; then say thus by the Rule of Proportion: If eight pound of gold doe expell two pound of water, what shall six pound expell? and it will be 1 pound $\frac{1}{2}$. Again, for the silver, If eight pound of silver expell three pound $\frac{1}{2}$ of water, what shall two pound of silver put out? it will be $\frac{1}{2}$; now adde those two weights of water together, and they will make two pound $\frac{1}{2}$, and it should be by the supposition two pound $\frac{1}{2}$, so is it too much by $\frac{1}{2}$.

Scholar. Now doe I understand the worke as I thinke, therefore I pray you let me worke the rest of the question. And because this first supposition did erre, I note that position and his error, and take a new position, esteeming the silver to bee but one pound, so must there bee in gold seven pound. Then say I; If eight pound of gold doe yeeld two pound

pound of water, what shall seven pound. yeld:
and it will be 1 pound $\frac{2}{3}$. Again, if 8 pound
of silver expell $\frac{3}{4}$ pound of water, what shall
1 pound expell? and it will be $\frac{1}{12}$. Now must
I adde these two summes together, and they
make two pound $\frac{2}{3}$, and they should make 2
pound $\frac{1}{4}$, so is it too little by $\frac{1}{12}$. Therefore
I set the positions, with their errors in order,
as here followeth: And then I multiply in
crosse wayes 2 by $\frac{1}{12}$, and it maketh $\frac{1}{6}$: Like-
wise 1 multiplied by $\frac{2}{3}$ ma-
keth $\frac{2}{3}$. And because the
signes be unlike, I must
adde these two summes which
make $\frac{5}{6}$: and that is the
dividend

Againe, I must adde $\frac{1}{12}$ to $\frac{2}{3}$, and it will be
 $\frac{9}{12}$, that is the Divisor. Now I shall divide $\frac{5}{6}$
by $\frac{9}{12}$, and the quotient will be $\frac{10}{9}$, that is, $1\frac{1}{9}$:
whereby I know that there was put 1 pound
and $\frac{1}{9}$ of silver into the Crowne, and so much
gold taken out for it.

Master. Prove it now by examination, ac-
cording to the question.

Scholar. If there were 1 pound $\frac{1}{9}$ of silver,
then was there of gold 6 pound $\frac{8}{9}$. Now say
I by the Rule of Proportion:
if 8 pound of gold expell two 8
pound of water, what shall 6 $\frac{8}{9}$
pound $\frac{8}{9}$ expell?

It

It will be 1 pound. **Againe,**
Z If 8 pound of silver expell three
 pound of water, what shall 1
 expell? It will be $\frac{3}{8}$. Nowe more adde to-
 gether 1 pound; and $\frac{3}{8}$, and they will make
 2 pound $\frac{3}{8}$, that is, 2 pound $\frac{3}{8}$, according to
 supposition of the question: whereby I per-
 ceive the worke to be well done. And I can-
 not but much rejoyce at this excellent inventi-
 on, so my desire is kindled vehemently to be
 perfectly instructed in every part thereof, and
 namely in this point, whether the proporti-
 on between water and gold be such, that for 8
 pound of gold put into a vessell full of water,
 there shall runne out two pound of water, and
 soz as much silver, whether 3 pound of wa-
 ter would abold.

Master. I perceive your meaning, and con-
 fecture your imagination to be thus, that if you
 knew the exact proportion between gold and
 silver, and water, both in their weight and
 quantities, then could you easily finde out the
 mixtures of them, which thing I have reser-
 ved soz another worke that intreateth of such
 matters especially. And at this time you must
 consider that you learne Arithmetick, which
 intreateth of the manner to solve doubtful
 questions touching number, without regard
 what matter is signified by that number: as
 were it necessary in Arithmetick, to teach all
 Arts, seeing in it may be moved questions of
 all Arts.

But seeing you are so desirous to know these things, I will tell you in such a sort, that you shall practise your Art in finding it, and propound it in forme of a question. Gold beareth a greater proportion to water, then silver doth, and their two proportions be in proportion together, as 48 to 25. But to helpe you somewhat in this Riddle, you shall note that the proportion of Quick-silver unto water, is the just middle number proportionall in ProgreSSION Geometricall, between the proportion of gold and silver unto water.

A question
of the pro-
portion of
of gold,
silver, and
quicksilver
unto water.

And this proportion is $\frac{25}{48}$. Now if you will know the just numbers of these three Proportions, then must you finde out three numbers in ProgreSSION Geometricall, whereof the middlemost must be $\frac{25}{48}$, and the first must be unto the last, as 25 to 48. And thus I will leave you to finde those numbers, when you bee at leisure.

Scholar. Yet Sir, I thanke you heartily for thus much, for now I see the possibilitie to finde them out. Howbest, because this question seemeth strange, if it might please you to instruct me somewhat in the order of working for it, I should the more easily finde the true working.

Master. You desire too much if you will studie for nothing: Wherefore to occasion you to study the better, I will leave this doubt wholly to your own search: But as touching the generallity of the Rule, Archimedes needed not to take two masses of Gold,
and

and Silver equall in weight with the Crowne, for the proportion might as well be found in any other weight, yea, although the Masse of Gold were of one weight, and the Masse of Silver of another. As for example: If the Crowne were of 18 pound weight, as I did suppose, and I have not so much other fine Gold, but onely one pound, and trying that by water, and finding that it doth expell but of an ounce of water, yet then by it I may inferre, that 8 pound of Gold would expell 6 ounces of water. And likewise of silver, whereof if I had but two pound, and find that it doth expell three ounces of water, then might I affirme that 8 pound would expell 12 ounces, that is, one pound weight: and so is it good as if the three Masses were all of one weight. And thus for this time I will make an end of this other part of Arithmetick.

Scholar. Although I cannot sufficiently thank you for this, yet your promise made me to looke for the Art of Extraction of Roots, whereof hitherto I have learned nothing.

Master. I will not breake my promise, but intend (God willing) to performe it within this three or foure moneths, if I perceiue this my pains to be well taken in the meane season. And you shall not repent the tarrying for it: for it shall be increased by the tarrying: And in the meane time you shall take this Addition, not for the second Part of Arithmetick which I promised, but for an
aug.

augmentation of the first part, unto which I
would have annexed the extraction of Roots
square and cubick, namely, for examples of
the Statute of Assise of Wood, but that in the
second part I must write of divers other
Roots, and thought it best to reserve those
Rules also with their Examples unto the
same second Part.

Scholar. Sir, although I cannot recom-
pence your goodnesse, yet I shall alwayes doe
mine endeavour to occasion you not to repent
your benefit on me thus employed.

Master. That recompence is sufficient for
your part,

FINIS.

E c

your name, in 1840
 M. J. Thompson is the first of
 your name on the map
 mine entered in 1840 not in 1841
 place your name in 1841 and not
 school, it is all right I cannot recall
 made from 1841

21417

3

THE
THIRD PART,

OR,

Additions to this Booke,
Entreateth

Of brief Rules, called Rules of Practice,
of rare, pleasant and commodious effect,
abridged into a briefer Method,
then hitherto hath been
published.

With divers other necessary Rules, Tables,
and Questions, not onely profitable for
Merchants, but also for Gentlemen, and
all other Occupiers whatsoever, as
by the contents of this Book
may appeare.

Set forth by JOHN MELLIS
Schoolemaster.

L O N D O N,

Printed by M. F. for John Harrison, 1648.

THE
THIRD PART

Additions to the

Of brief Rules, called Rules of Practice
of law, plain and convenient
abridged into a brief Method,
then hitherto hath been
published.

With divers other necessary Rules, Tables
and Questions, not only profitable for
the use of the Law, but also for the
all other that are concerned in the
by the contents of this Book
may appear.

Set forth by JOHN MELLIS
Schoolmaster.

LONDON

Printed by A. L. for John Mellis 1648.

The first Chapter of this Addition,
 entreateth of brief Rules, called Rules of
Practice, with divers necessary questions, profit-
 able not onely for Merchants, but also for
 all other Occupiers whatsoever.

The working of Multiplication
 in practice, is no other thing
 then a certain manner of mul-
 tiplying of one kinde by ano-
 ther: whereupon is brought
 forth the product of the pro-
 poned number, which is accomplished by the
 means of Division, in taking the *half*, the *third*,
 the *fourth*, the *fifth*, or such other parts of the
 summe which is to be multiplied.

And for the better understanding of such con-
 versions, you shall understand that in the manner
 and use of these Rules of practice, you ought first
 to know the even or aliquot parts of a shilling,
 which in this Table following doth appear.

| | |
|---|---------------|
| 6 | 1 |
| 4 | $\frac{1}{2}$ |
| 3 | $\frac{1}{3}$ |
| 2 | $\frac{1}{4}$ |
| 1 | $\frac{1}{5}$ |

pence is the of a shilling.

Wherein as you see according to the order

of these Rules of Practice : At six pence the yard of any thing, you must take $\frac{1}{2}$ of your number which is to be multiplied, and the product that cometh thereof shall be shillings, if any unite do remain, it is 6 pence.

For 4 d. take the $\frac{1}{3}$ of the number that is to be multiplied, and the product also produceth shillings, if any unites doe remain, each one shall be worth in value 4 pence. The like is to be understood of the other 3, &c.

III
I Example

At 6 d. the yard, what

379 yards?
189 s. — 8 d.

II
At 4 d. the yard, what

104 yards?
34 s. — 8 d.

III
At 3 d. the yard, what

5014 yards?
1353 s. — 6 d.

IV
At 2 d. the yard, what

532 yards?
88 s. — 8 d.

V
At 1 d. the yard, what

409 yards?
34 s. — 1 d.

Here you may see in the first example, that 379 yards at 6 d. the yard, are worth 189 s. 6 d. in taking the $\frac{1}{2}$ of 379. And in the second example the 104 yards at 4 d. the yard, are worth 34 s. 8 d. in taking the $\frac{1}{3}$ of 104: Likewise in the third example, 5014 yards at 3 d.

the

the yard, bringeth forth 1253 s. 6. d. in taking
the $\frac{3}{4}$ of 5014. As also in the fourth example
at 2 d. the yard, maketh 88 s. 8 d. And lastly;
in the fifth example, 409 yards at 1 d. the yard,
amounteth to 34 s. 1 d. in taking the $\frac{3}{4}$ of 409.
and so is to be done also of all other questions
the like, when the number of the pence is any
of the even or aliquot parts of 12 pence.

Item, to bring the products of these shillings, and all other the like into pounds, is very easy in dividing of it in your minde by 20, for it is to be understood that as often as 20 is found in that product, so many pounds doth it contain: which with facility to perform, always strike off the figure towards your right hand, with a right down dash of your pen, for the 0 that appertaineth to the 20. And then begin at the left hand, in taking the half of the rest. And if that at the last any unite do remain, the same shall be joyned with the figure that is cut off, which shall represent the odde shillings, contained in that work.

As for example, in your third question at 3 d,
the yard, which amounteth to 1253 s. 6 d. the
product whereof maketh

| | |
|----|------|
| | 1253 |
| 68 | — |
| 13 | — |
| 6 | — |

may see, is easily performed by this example.

Also for the working of one penny the yard,
it is something harsh and hard to take the $\frac{1}{3}$
of some products: therefore to ease that hard
work, you shall first bring your delivered

summe into *groats*, by taking $\frac{1}{2}$ part of the product, and if any unites remain of that $\frac{1}{2}$ part, as sometimes there may, they are pence, and must be signified with a line from the *groats* with their title of *pence*; and because that 60 *groats* maketh a pound or 20 shillings, strike off the first figure toward your right hand, for the 0 that appertaineth to 60 (as you did even now for the 0 that belongeth to 20.) Then in taking the $\frac{1}{2}$ of that product, if there do remain any unites, the same shall you joyn with the figure that you cut off, esteeming them as *groats*, which keep in your minde, and by taking the $\frac{1}{2}$ part of them, you shall turn them into *shillings*, and so have you done: As for example, by a question or two hereafter proponed, shall more plainly by the work appear.

At 1 d. the yard, what 54368 yards.

| | | |
|------|-----|----------------|
| 1359 | 2 | <i>groats.</i> |
| 5 | 226 | 10 s. 8 d. |

Here in taking the $\frac{1}{2}$ part of 1359, in coming to the last work, the $\frac{1}{2}$ part of 39 being taken, the remainder is 3, which joyned with the 2 that was cut off, maketh 32 *groats*, which converted into *shillings*, by taking the $\frac{1}{2}$ part, maketh as appeareth 10 s. 8 d. Many other wayes there are, but none more apt for a young learner to understand then this: wherefore this one way well impressed in memory, is better then 20 wayes doubtfully understood.

At

At 1 penny the yard, what 45 33 yards?

1133 great 1 d.

At 1 penny the yard, what 64 68 yards?

1619 2 great 1 d.

269—17--4 d.

Now followeth also to be understood, that if 2 Rule.

the number of pence be not an aliquot part of 12, you must reduce them into some aliquot part of 12: and after the aforesaid manner, you shall make of them two or three products, as need shall require, and add them together into one sum. And here for thy furtherance appeareth a note of the order of their parts, as they are to be taken.



Here in the first note of this Table, at 5 d. you shall first take for 3 d. the $\frac{2}{3}$ of the number that is to be multiplied, and likewise for 2 d. the $\frac{1}{2}$ of the same number, adding together both the products: But if you will work by 4 and 1, you must for 4 d. first take the $\frac{1}{2}$ of the number that is to be multiplied: and for 1 d. take the $\frac{1}{4}$ of the whole summe, or rather, which is more better, for 1 penny you may take the $\frac{1}{4}$ of the product which did come of the 4 pence:

pence: because that 1 d. is the $\frac{1}{4}$ of 4 pence. The totall summes of these two numbers shall be the solution to the question. And in like manner is to be done of all others, as by these examples following shall appear.

I

At 5 d the yard, what

748 yards?

3 d

187 — 0 d

2 d

124 — 8 d

shillings

311 — 8 d

Otherwise,

At 5 pence the yard, what

758 yards?

4 d

252 — 8 d

1 d

63 — 2 d

shillings

315 — 10 d

II

At 7 d the Ell, what

563 Ells?

4 d

187 — 8 d

3 d

140 — 9 d

shillings

328 — 5 d

III

At 8 d the pound, what

112 pound?

4 d

37 — 4 d

4 d

37 — 4 d

shillings

74 — 8 d

Otherwise,

At 8 pence the pound, what

112 pounds?

6 d

56 — 0 d

2 d

18 — 8 d

shillings

74 — 8 d

IV

IV
At 9 pence the Ell, what 356 Ells?
178 — 0
189 — 0
shillings 267 — 0 d
At 10 pence the piece, what 795 pieces?
397 — 6
265 — 0
shillings 662 — 6

VI
At 11 pence the pound, what 7576 pounds?
3788 — 0
2525 — 4
631 — 4
shillings 6944 — 8 d

Pounds 347 — 4 s — 8 d

Here, in this first example, where it is demanded (at 5 d. the yard) what will 758 cost?

First, for 3 d. I take the $\frac{1}{2}$ of 758, and thereof commeth 189 s. 6 d. Then for 2 d. I take the $\frac{1}{3}$ of the same 758, which amounteth to 126 s. 4 d. these two sums added together, do make 315 shillings 10 pence; and so much are the 758 yards worth at 5 d. the yard.

1 Item, for the same again: First, for 4 d. I take the $\frac{1}{2}$ of 758, and thereof commeth 252 s. 8 d. then for 1 penny I take the $\frac{1}{4}$ of the same 758, that is to say, of 252 s. 8 d. and it yeeldeth me 63 s. 2 d. which both added together maketh 315 s. 10 d. as before.

2 Item,

2 *Item*, for 7 d. there is taken the $\frac{1}{2}$ and the $\frac{1}{4}$ of the whole sum which is to be multiplied, and adde them together, that is to say; first, for 4 d. there is taken $\frac{1}{2}$ of 563; which comes to 187 s. 8 d. as appeareth by the work, and for 3 d. there is taken the $\frac{1}{4}$ of the whole summe, which amounteth to 140 s. 9 d. Both which products added together, do make 328 s. 5 d. and so much comes 564 Ells to; at 7 d. the Ell.

3 *Item*, for the first 8 d. there is taken for 4 d. the $\frac{1}{2}$ of the whole summe, and another $\frac{1}{2}$ for the other 4 d. which added together, as in the example doth evidently appear, amounteth to 74 s. 8 d.

Again, for the second work of 112 li. there is taken first the $\frac{1}{2}$ of the whole summe for 6 d. which comes to 56 s. then for that 2 d. you have to take $\frac{1}{4}$ of the whole summe, or if you will, the $\frac{1}{4}$ of the product that came of 6 d. either of which maketh 18 s. 8 d. These two summes being added together, do make 74 s. 8 d. as in the third example appeareth.

4 *Item*, for 9 d. there is taken for 6 d. the $\frac{1}{2}$ of the whole summe, and the $\frac{1}{4}$ of the whole summe for 3 d. or otherwise for the 3 d. you may take the $\frac{1}{4}$ of the product that came of 6 d. because 3 d. is the $\frac{1}{2}$ of 6 d. which added together, as plainly appeareth in the fourth example, amounteth to 167 s. 8 d.

5 *Item*, for 10 d. first there is taken for 6 d. the $\frac{1}{2}$ of the whole summe, which amounteth to 397 s. 6 d. Then for 4 d. there is found 265 s. both

both which added together, make 66 s. Shillings 6 d. appeareth in the first example, it may also be wrought, as appeareth by the second note in the Table, by 4 d. twice taken, and the $\frac{1}{2}$ of the product of 4 d. or else by the $\frac{1}{2}$ of the whole summe, &c.

Item, for 1 s. d. there is first taken the $\frac{1}{2}$ for 6 d. then the $\frac{1}{2}$ of the whole summe for 4 d. Lastly, the $\frac{1}{2}$ of the last product for 1 d. All which 3 summes added together, maketh in shillings 60 s. 8 d. and in pounds 3 l. 4 s. 8 d.

Item, likewise by the same reason, when you will multiply (by shillings) any number that is under 20 s. you shall have in the product pounds, if you know the even or aliquot parts of 20 which are here in this little Table set down to sight.

Item, $\frac{1}{2}$ is the $\frac{1}{2}$ of one pound.

So that for 10 s. which is the $\frac{1}{2}$ of a pound, you may take the $\frac{1}{2}$ of the number which is to be multiplied, and you shall have in your product pounds: if an unite do remain, it shall be worth 10 shillings.

Likewise for 5 s. you must take the $\frac{1}{4}$ of the number which is to be multiplied, and if there do remain any unites, they shall be fourth parts of a pound, every unite being in value five shillings.

For 4 s. take the $\frac{1}{3}$ of the number which

2 1/2
10
6
10
09

Don

is to be multiplied, and if there doe remain any *unites*, they shall be fift parts of a pound, each *unite* being in value 4 shillings.

For 1 shilling you must take the $\frac{1}{2}$ of the number to be multiplied, wherefore to take the $\frac{1}{2}$ of any number, you must cut off the last figure of the same number (which is nearest your right hand) from all the other figures with a small right down line or dash with a pen, and so have you done: for all the other figures which do remain toward your left hand from the same figure that you do separate, shall be the said $\frac{1}{2}$ of a pound; and that figure so separated towards your right hand, shall be so many pieces of 2 s. the piece, the which figure you must double to make thereof the true number of shillings, as by the example shall appear.

Finally, for 1 shilling verdet *small work*, for it is so many shillings as be proponed in the summe, which to bring into pounds hath been already taught in the first Rule.

Example.

At 10 s. the piece, what

li.

8543 pieces

At 5 s. the Ell, what

li.

3371 10s

At 4 s. the yard, what

li.

4373 Ells

At 2 s. the pound weight, what

li.

1093 5s

7839 yards

1567 16s

752 14s

At 3 s. the piece, what sum of 100 s. will buy 100 pieces?

3 s. the piece, 100 s. will buy 33 1/3 pieces.

100 s. will buy 33 1/3 pieces.

100 s. will buy 33 1/3 pieces.

Next followeth in order to be understood 4 Rule.

That if the number of shillings be not found

even or aliquot parts of 20, you must then convert

the same number of shillings into the aliquot

parts of 20; and thereof make two or three pro-

ducts as need shall require: which done, add them

together, and bring them into pounds: And here

for thy further use I have set down a note of the

order of their parts, as they are to be taken.

For 10 s. the piece, 100 s. will buy 10 pieces.

For 12 s. the piece, 100 s. will buy 8 1/3 pieces.

For 15 s. the piece, 100 s. will buy 6 2/3 pieces.

For 20 s. the piece, 100 s. will buy 5 pieces.

For 25 s. the piece, 100 s. will buy 4 pieces.

For 30 s. the piece, 100 s. will buy 3 1/3 pieces.

For 40 s. the piece, 100 s. will buy 2 1/2 pieces.

For 50 s. the piece, 100 s. will buy 2 pieces.

For 60 s. the piece, 100 s. will buy 1 2/3 pieces.

For 70 s. the piece, 100 s. will buy 1 1/3 pieces.

For 80 s. the piece, 100 s. will buy 1 1/4 pieces.

For 100 s. the piece, 100 s. will buy 1 piece.

For 120 s. the piece, 100 s. will buy 5/6 pieces.

For 150 s. the piece, 100 s. will buy 2/3 pieces.

For 200 s. the piece, 100 s. will buy 1/2 pieces.

For 300 s. the piece, 100 s. will buy 1/3 pieces.

For 400 s. the piece, 100 s. will buy 1/4 pieces.

For 500 s. the piece, 100 s. will buy 1/5 pieces.

For 600 s. the piece, 100 s. will buy 1/6 pieces.

For 700 s. the piece, 100 s. will buy 1/7 pieces.

For 800 s. the piece, 100 s. will buy 1/8 pieces.

For 900 s. the piece, 100 s. will buy 1/9 pieces.

Rules of Practice

number that is to be multiplied: then for 2 s. take the $\frac{1}{2}$ of the product that came of 4 s. and adde them together.

Or else as appeareth also in the Table, for 5 s. you may take the $\frac{1}{4}$ and the $\frac{1}{2}$ part of the product that came of 5 shillings, and adde them together.

Item, for 7 s. first for 5 s. take $\frac{1}{4}$ of the product that is to be multiplied, then for 2 s. take the $\frac{1}{2}$ of the number that is to be multiplied, and adde them together, &c.

Item, for 8 s. according to reason, and the intent of the Table, for the first 4 s. take the $\frac{1}{4}$ of the product, and the same number again for the other 4 s. and adde them together.

Item, for 9 s. first for 5 s. take the $\frac{1}{4}$; then for four shillings take the $\frac{1}{2}$ and adde them together.

Or likewise, as you see by the intent of the Table, work twice for 4 shillings, as was taught even now for 8 s. and then take the $\frac{1}{4}$ of the last product for the 1 shilling: but 5 and 4 is the shorter.

Item, for 11 s. first dispatch 10 shillings; for which you must take the $\frac{1}{4}$ of the product, then lastly, for 1 shilling take the $\frac{1}{11}$ part of the summe produced of the $\frac{1}{4}$ of the product, and adde them together.

Item, for 12 s. where I will end with the first part of my Table. First take the $\frac{1}{4}$ for ten shillings: and then for 2 shillings, take the $\frac{1}{3}$ of the sum that came of ten shillings, take and adde

adde them together, or else if you please for 2 shillings, you may take the $\frac{1}{4}$ of the whole given number.

To write more of the manner of taking the true parts, I omit. The desirous practitioners will (no doubt) conceive it. Also the *Table* is some aid to help the unperfect, whereupon by and by I will set down three or four of these notes in *Examples*, and the rest I will leave to thine own industry and practice, to labour upon.

This is the order most commonly used in practice, when the number of shillings is not an *aliquot* part of a pound. But (*loving Reader*) after I have touched the even or *aliquot* parts of a pound that falleth out in pence and shillings, I will deliver two new Rules that shall drown this common order quite and clean: wherein shall be comprehended in one line, or working both of even and odde parts of shillings under 20, without regard whether it be an *aliquot*, or not an *aliquot* part; which two Rules (when they come in place) I commit to thy friendly judgement in working.

Now follow the examples upon the notes before said.

At 6 shillings the yard, what

3215 yards?

4 shillings

643

2 shillings

321—10

li.

964—10s.

Ff

Other-

Otherwise by Multiplication of 6.

| | |
|------------------------------|-------------|
| 6 shillings | 19290 |
| 11 | 964 |
| At 7 shillings the Ell, what | 4563 Ells? |
| 5 shillings | 1140 |
| 2 shillings | 456 |
| 11 | 1597 |
| | 1 shilling. |

Otherwise by Multiplication of 7.

| | |
|----|-------|
| 7s | 4563 |
| | 31941 |
| | 1597 |
| | 1 |

| | |
|-------------------------|--------------|
| At 8 s. the piece, what | 7563 pieces? |
| 4 s | 1512 |
| 4 s | 1512 |
| pounds | 3025 |
| | 4 s. |

Otherwise by Multiplication.

| | |
|--------------------------|-------------|
| 8s | 7563 |
| | 60304 |
| pounds | 3025 |
| At 13 s. the piece, what | 401 pieces? |
| 10 s | 200 |
| 2 s | 40 |
| 1 s | 20 |
| pounds | 260 |
| | 13 |

Other

Otherwise by Multiplication

$$\begin{array}{r} 401 \\ 1203 \\ \hline 401 \\ 5213 \\ \hline 260 \end{array}$$

 Pounds 13 s.

These and such like questions of compound numbers, which I have here in this fourth rule for orders sake set down, for that it hath been hitherto a common course of work, I account but superfluous. For in the eight and ninth Rules of this my simple Addition shall appear, that the given price of any even or odd number of shillings, either under or above 20 shall be wrought at one or two workings as the most, how difficult soever the question be.

Item, there resteth yet a kinde of practice, both 3 Rule.

to bring pence into pounds at the first working, whereupon you must understand that 240 pence maketh one pound, or 20s. In consideration whereof I cut off the last figure or 0, and there remaineth but 24 (of which 24) 8 d. is the $\frac{1}{3}$ part thereof, 4 d. is the $\frac{1}{2}$ part, and 2 pence is the $\frac{1}{4}$ part thereof.

To reduce pence into pounds at one operation.

Whereupon if it were demanded what 1486 yards or pounds of any thing cometh to, at 8 pence the yard, in pricking or cutting off the first figure towards your right hand, for

the 0 that appertaineth to 240. There is remaining of the said summe 148, whereout I taking the $\frac{1}{2}$ part, and it commeth to 49 li. and there resteth 1, which I put to the 6, that I prick or cut off, and it maketh 16 pieces of 8 pence, which I double to make into groats, and they make 32, whereof the $\frac{1}{2}$ part maketh 16 s, and there remaineth 8 s. which is 8 d, whereby it followeth, that the 1489 yards at 8 pence the yard maketh 49 li. 10 s. 8 d. as by the example shall appear.

Item, for 6 d. take $\frac{1}{2}$ part of the number from the prickt figure; and if any unites remain, they are so many six pences, whereof taking the $\frac{1}{2}$ they are shillings, if there do remain yet one, it is in value six pence.

Item, for 4 d. take the $\frac{1}{2}$ part of the number from the prickt figure; If any unites do remain, they are so many groats, which to convert into shillings, take the $\frac{1}{2}$ part. And if any yet remain, they are thirds of shillings, each one in value being worth 4 pence.

Item, for 3 pence, take the $\frac{1}{2}$ part from the prickt figure, if any unites remain, they are so many pieces of 3 pence, whereof in taking the $\frac{1}{2}$ part, maketh shillings: if any thing yet remain, they are the fourth parts of shillings, each one being in value 3 pence.

Item, for 2 pence, as appeareth also by the Table, take the $\frac{1}{2}$ part of the number from the prickt figure: if any thing remain, they are so many pieces of 2 pence, which by taking the

the 1 part, you shall cut into shillings, and if any unites remain, they are so many first parts of shillings, or pence, or two pence, whether you will.

If one cost 8 pence, what maketh pounds $49-10-8d.$

If one cost 6 pence, what maketh pounds $196-12-6d.$

At 4 pence the yard, what maketh pounds $145-12-0d.$

If one cost 3 pence, what maketh pounds $123-8-6d.$

At 2 d. the Ell, what maketh pounds $65-15-8d.$

But if your number of pence be not an aliquot or even part of 24, then must you bring them into the aliquot parts of 24. and make thereof diverse products which must be added together, as by the question hereafter following shall appear. 6 Rule.

Item, for 5 d. first take for 3 d. then for 2 d. and adde them together, according to the instruction of the second Rule: or else first take for 4 d. then 1 d.

Item, for 7 d. first take for 4 d. then for 3 d. and adde them together.

Item, for 9 d. first take for 8 d. then for 3 d. and adde them together.

Item, for 10 d. first take for 6 d. then for 4 d. and adde them together.

Item, for 11 d. first take for 8 d. then for 3 d. and adde them together: as by these Examples.

Examples.
 1 If one yard cost 5 d. what
 4 pence
 1 peny
 maketh pounds

Otherwise
 1 — 5 — 7596
 3 pence
 2 pence
 maketh pounds

2 If one cost 7 d. what
 4 pence
 3 pence
 maketh pounds

Otherwise
 1 — 7 — 981
 6 pence
 1 peny
 maketh pounds

3 If one cost 9 d. what
 6 pence
 3 pence
 maketh pounds

Other

Otherwise.

| | | |
|---------------|----|-------|
| 1 | 9 | 98/7? |
| 6 pence | 24 | 13 6 |
| 3 pence | 12 | 16 9 |
| maketh pounds | 37 | 00 03 |

4 If one cost 10 pence, what 98/7?

| | | |
|---------------|----|------|
| 6 pence | 24 | 13 6 |
| 4 pence | 16 | 9 0 |
| maketh pounds | 41 | 2 6 |

5 If one cost 11 pence, what 98/7?

| | | |
|---------------|----|------|
| 8 pence | 32 | 18 0 |
| 3 pence | 12 | 6 9 |
| maketh pounds | 45 | 6 9 |

But if you have any shillings and pence to be multiplied together, then are you to take for the shillings according to the instruction of the third Rule; and for the pence according to the first Rule before mentioned: unlesse you can spie the advantage thereof, and thereby help your self; as appeareth in this second example, where first I work for 6 d. which is to be rebated out of the given number, and I have 719 li. 11 s. my desire.

At 19 s. 9 d. the yard, what 738 yards?

| | | |
|--------|--------|---------------|
| | 738 | Otherwise by |
| 10 s. | 369—0 | Rebating. |
| 5 s. | 184—10 | 738 |
| 4 s. | 147—12 | 6 d. 18—9 s. |
| 6 d. | 18—9 | 11—7—19—11 s. |
| pounds | 719— | 11 s. |

The like again is done by rebating, as by these two examples appeareth.

At 18 s. the Ell, what 418 Ells?

| | | |
|------------------------|-----------|--------|
| 2 s. | 418 | 16 |
| pounds | 376 | —4 s. |
| At 16 s. the Ell, what | 517 Ells? | |
| 4 s. | 129 | 8 |
| pounds | 413 | —12 s. |

7 Rule.

And now I will touch a little the even part of a pound, that falleth out in pence and shillings, whereof for those parts you shall take such like part out of the given number that is to be multiplied, as the price of that given number beareth in proportion to a pound, which also for their better aid is here set down,

1 s. 8. d.

2
3
6

is the part of a pound.

Item,

Item, first for 1 shilling 8 pence take the $\frac{1}{12}$ part of the given number, and if any thing do remain, they are twelve parts of a pound, each one being in value 1 shilling 8 pence.

Item, for 2 shillings 6 pence, take the $\frac{1}{6}$ part of the number that is to be multiplied; and if any thing do remain, they are eight parts of a pound, each one being in value 2 shillings six pence.

Item, for 3 shillings 4 pence, as appeareth by the Table, you must take the $\frac{1}{3}$ part of the given number, and if any thing do remain, they are 6 parts of a pound, each one being in value 3 shillings 4 pence.

Item, for 6 shillings 8 pence take the $\frac{1}{3}$ part of the number that is to be multiplied: And if any unites doe remain, they are thirds of a pound, every one being worth 6 shillings 8 pence.

Other infinite numbers there are, that may be reduced by abbreviation into the proportionate parts of a pound, as 16 shillings 8 pence maketh $\frac{1}{3}$: which 16 shillings 8 pence is easily reduced into groats, by multiplying 16 by 3; and thereto adde 2, which maketh 50 groats.

Then set 60 the groats of a pound under 50: cutting off the the two Ciphers as is here performed.

And then have you brought 16 shillings 8 pence into the knowne parts of a pound, which maketh

$$\begin{array}{r} 16-8 \\ 3 \\ \hline 510 \\ 610 \end{array}$$

But

But yet gentle Reader, for thy further instruction, I have herunto annexed in a *Table*, how pence and shillings bear proportion to a pound, which I commit to thy friendly benevolence; it will be some aid unto the ungrounded Practitioner: but I count him the best Workman that can presently reduce his given price into the known and proportionate parts of a pound.

Here follow four Examples upon the
**A Table of the Aliquot parts of a
 pound, or 20 shillings.**

At 1 s. 8. d. the yard, what 388 yds?

| Shillings | Pence | Farthings | Shillings | Pence | Farthings |
|-----------|-------|-----------|-----------|-------|-----------|
| 1 | 0 | 0 | 1 | 0 | 0 |
| 2 | 0 | 0 | 2 | 0 | 0 |
| 3 | 0 | 0 | 3 | 0 | 0 |
| 4 | 0 | 0 | 4 | 0 | 0 |
| 5 | 0 | 0 | 5 | 0 | 0 |
| 6 | 0 | 0 | 6 | 0 | 0 |
| 7 | 0 | 0 | 7 | 0 | 0 |
| 8 | 0 | 0 | 8 | 0 | 0 |
| 9 | 0 | 0 | 9 | 0 | 0 |
| 10 | 0 | 0 | 10 | 0 | 0 |
| 11 | 0 | 0 | 11 | 0 | 0 |
| 12 | 0 | 0 | 12 | 0 | 0 |
| 13 | 0 | 0 | 13 | 0 | 0 |
| 14 | 0 | 0 | 14 | 0 | 0 |
| 15 | 0 | 0 | 15 | 0 | 0 |
| 16 | 0 | 0 | 16 | 0 | 0 |
| 17 | 0 | 0 | 17 | 0 | 0 |
| 18 | 0 | 0 | 18 | 0 | 0 |
| 19 | 0 | 0 | 19 | 0 | 0 |
| 20 | 0 | 0 | 20 | 0 | 0 |

Here follow four examples upon the

10 year, North delivered.

15 willid 05 10 15009

At 1 s. 8 d. the yard, what 3884 yards?

maketh pounds 323 — 136 40

At 2 s. 6 d. the yard, what 4563 yards?

maketh pounds 570 — 7 — 6 d.

At 6 s. 8 d. the Ell, what 7562 Ells?

maketh pounds 2520 — 13 — 4 d.

Now by custome you are able to work by all sorts of summes being delivered in shillings and pence, as one shilling one peny, two shillings two pence, three shillings three pence, and so of all other: wishing you to have some consideration of your questions, when they are set down, for there are many subtille abbreviations, and great advantages to be gotten, and easily to be perceived.

As of 3 s. — 8 d. of 2 s. and 1 s. 8 d.

Of 4 s. — 2 d. of 3 s. — 4 d. 8

10 d. which 10 d. is $\frac{1}{4}$ of 3 s. — 4 d.

Of 5 s. — 8 d. of 4 s. 1 s. — 8 d.

Of 5 s. 10 d. of 5 s. and 10 d. which 10 d. is $\frac{1}{2}$ of 5 s.

And by this mean when you have taken one product, you may oftentimes upon the same take

take another more briefly then upon the sum which is to be multiplied, &c.

NOW (Gentle Reader) that you have seen the 8 Rule, verue of the even or aliquot parts of a pound in shillings alone, and also in the aliquot parts of shillings and pence according to my promise hereafter followeth a brieft and easier method for any even number of shillings, either under or above 20, then ever yet hath been published; Norwich standing M. Humphrey Baker, whose travell is worthy commendation, and whom for knowledge sake I reverence, hath in some part touched this first part, though not in this method. The work of the Rule both pleasant, ready, and brief, as by the variety of the examples delivered thereupon shall appear. And first I will set forth a question, thereby the better to expresse or teach you the order thereof: which is this.

If one cost 6 s. what 8574?

6 8574

maketh pounds

2572 — 4 s.

To the understanding of this example, after you have set down your given number in form of the Rule of 3, with a line drawn under it, you shall presently set a prick under your first figure 4. toward your right hand drawing from the prick, as heretofore hath been practised, a little short line, thereto set down the

Mr. John Mellis his first Rule.

the shillings upon, which done multiply the first figure 4 by 6, the value of your price, (which here you see standeth in sight above the line) it maketh 24, which is one pound four shillings. The one pound keep to carry to the next place, and the four shillings set down at the end of the prescribed line towards your right hand. Thus have you done now with 6 above the line, and now with 4 in the first place (for the prick under 4 doth signify that 4 hath done his office.) Then set on a new line for a general Rule take but the 1 of the given price, which here is 3, which 3 is the number that shall now continue the rest of the multiplication, and end the work, thereupon I multiply 3 into 7, standing in the second place it maketh 21, and with the one pound I kept it 23; set down 3, and keep 2 in mind, working according to the Rule of multiplication, delivering the tenths in minde in their due place, which done, the product from the prick to your left hand representeth the pounds, and the other at the end of the shilling, as appeareth by the examples.

Note a general rule.

If one yard cost 2 s. what
If one yard cost 4 s. what
If one yard cost 6 s. what
If one yard cost 8 s. what
If one yard cost 10 s. what
If one yard cost 12 s. what
If one yard cost 14 s. what
If one yard cost 16 s. what
If one yard cost 18 s. what
If one yard cost 20 s. what
If one yard cost 22 s. what
If one yard cost 24 s. what
If one yard cost 26 s. what
If one yard cost 28 s. what
If one yard cost 30 s. what
If one yard cost 32 s. what
If one yard cost 34 s. what
If one yard cost 36 s. what
If one yard cost 38 s. what
If one yard cost 40 s. what
If one yard cost 42 s. what
If one yard cost 44 s. what
If one yard cost 46 s. what
If one yard cost 48 s. what
If one yard cost 50 s. what
If one yard cost 52 s. what
If one yard cost 54 s. what
If one yard cost 56 s. what
If one yard cost 58 s. what
If one yard cost 60 s. what
If one yard cost 62 s. what
If one yard cost 64 s. what
If one yard cost 66 s. what
If one yard cost 68 s. what
If one yard cost 70 s. what
If one yard cost 72 s. what
If one yard cost 74 s. what
If one yard cost 76 s. what
If one yard cost 78 s. what
If one yard cost 80 s. what
If one yard cost 82 s. what
If one yard cost 84 s. what
If one yard cost 86 s. what
If one yard cost 88 s. what
If one yard cost 90 s. what
If one yard cost 92 s. what
If one yard cost 94 s. what
If one yard cost 96 s. what
If one yard cost 98 s. what
If one yard cost 100 s. what

If one piece cost 6 s. what 9537?

$\begin{array}{r} 1 \quad 6 \\ 9537 \\ \hline 2861 \end{array}$ — 2 s.

If one piece cost 8 s. what 7509?

$\begin{array}{r} 1 \quad 8 \\ 7509 \\ \hline 300 \end{array}$ — 12 s.

If one cost 12 s. what 5794?

$\begin{array}{r} 1 \quad 12 \\ 5794 \\ \hline 3476 \end{array}$ — 8 s.

If one cost 14 s. what 3705?

$\begin{array}{r} 1 \quad 14 \\ 3705 \\ \hline 2593 \end{array}$ — 10 s.

If one cost 18 s. what 5703?

$\begin{array}{r} 1 \quad 18 \\ 5703 \\ \hline 5132 \end{array}$ — 14 s.

If one cost 22 s. what 953?

$\begin{array}{r} 1 \quad 22 \\ 953 \\ \hline 1048 \end{array}$ — 6 s.

Let these suffice (gentle Reader) for an entrance into even numbers. And now I will shew the like rule for any odde or uneven part of a pound.

TO help you to the understanding of these other Questions that hereafter follow: where in my first Example the given number is 6487

at 3 s. the yard: I multiply 3 above the line into 7, it maketh 21. The one shilling is set down, and the 1 pound I keep. Now am I to take the 2 of three, which because it is an odde number I cannot.

Mr. John
Mellis his
second
Rule.

Therefore I shall keep and continue my multiplication by three still, and work by the $\frac{1}{2}$ of the rest of the given figures or number, to wit, 648. And first the $\frac{1}{2}$ of 8 which is 4 multiplied into 3, maketh 12, there to joyn the 1 li. in minde it maketh 13. set down 3, keep one. Then again multiply by two the $\frac{1}{2}$ of four it maketh six, and with one in minde it maketh 7. Then lastly, take the $\frac{1}{2}$ of six, which is 3. saying, 3 times 3 is 9, which 9 set down, and so is the question answered, as appeareth by the practice, and examples following.

At 3 s. the yard, what 648?

| | | | |
|---------------|---|------|--------|
| 1072 | 3 | 6487 | 1 |
| | | | |
| maketh pounds | | 973 | — 1 s. |

If one yard cost 5 s. what 4269?

| | | | |
|---------------|---|------|--------|
| 1 | 5 | 4269 | 1 |
| | | | |
| maketh pounds | | 167 | — 5 s. |

At 7 s. the Ell, what 6489?

| | | | |
|---------------|---|------|--------|
| 1 | 7 | 6489 | 1 |
| | | | |
| maketh pounds | | 2271 | — 3 s. |

If one Ell cost 9 s. what 2807?

| | | | |
|---------------|---|------|--------|
| 1 | 9 | 2807 | 1 |
| | | | |
| maketh pounds | | 1363 | — 3 s. |

If

the sum of \$25.00
the first place, as was suggested for the
working of the building in my first Rule of
makeher pounds 45.44 A31

If one piece cost 13 s. what 4829?

4629

maketh pounds

3008

17 S.

2 But now note (gentle Reader) when the given price falleth upon an odde number, as 3, 5, 7, 11, 13, &c. then it is to be presupposed, that the given summe to be multiplied, must be a summe made of even numbers, 2, 4, 6, 8, 10, &c. else cannot that question be wrought at one line or working.

¶ Providing alwayes that it may bear an odde figure in the first place towards your right hand, as appeareth in these six examples, which last were wrought, and such like, &c. which may bear an odde number for the price, and be done at one line or working very well.

But if the given price be an odde number, and the summe to be multiplied, odde numbers also: then can it not be done at one working, but requireth the aid of two workings, for odde with odde will not agree, which notwithstanding to bring to passe, take this for a generall Rule. First, work for the even number contained in that question, or given price, according as you have learned, and then afterwards for the one odde shilling, take the 1 of

A general Rule. How

the summe given to be multiplied; omitting
the first price place, as was taught for the
working of one shilling in my first Rule of
Practice, and adde those two together, and you
shall have your desire.

Examples,

At 3s. the yard, what 7539 yards maketh pounds

At 7s. the Ell, what 7539 maketh pounds

At 13s. the yard, what 7534 maketh pounds

At 13s. the Ell, what 7534 maketh pounds

At 13s. the yard, what 7534 maketh pounds

At 13s. the Ell, what 7534 maketh pounds

Ninth this
well.

And thus have I abridged these two rules
taught being any number of shillings, whether
ver they be, into pounds, with a briefer Method
than ever yet hath been published, which I com-
mend unto thy friendly censure and judgement
in the use and practice thereof.

If one cost 6s. 5d. what

$$\begin{array}{r} 1231? \\ 369 \overline{) 650} \\ 10 \overline{) 10} \\ 5 \overline{) 2} \end{array}$$

maketh pounds

At 14s. 2d. what

$$\begin{array}{r} 2825? \\ 1977 \overline{) 142} \\ 23 \overline{) 10} \end{array}$$

maketh pounds

At 16s. 4d. what

$$\begin{array}{r} 2531? \\ 2024 \overline{) 16} \\ 24 \overline{) 3} \end{array}$$

maketh pounds

At 3s. the Pistol, what

maketh pounds

$$\begin{array}{r} 8324? \\ 1248 \overline{) 155} \end{array}$$

At 7s. the Crown, what

$$\begin{array}{r} 6529? \\ 2285 \overline{) 35} \end{array}$$

At 9s. the price, what

maketh pounds

$$\begin{array}{r} 6567? \\ 2955 \overline{) 35} \end{array}$$

These three last questions may seem something harder, yet they are easie enough, if you mark them well: If I should explaine them, then are they too easie. Therefore I leave them to what the minds of the desirous.

10 Rule.

Item, when any one of the summes, which is to be multiplied, is composed of many denominations, and the given number but of one figure alone; then shall you multiply all the denominations of the other summe by the same one figure, beginning first with that summe which is least in value toward your right hand, and bring the product of those pence into shillings, and the product of the shillings into pounds, as by this example appeareth.

At 3 li. 7 s. 4 d. a yard, what are 9 worth?
maketh pounds 30—6 s.—0 d.

11 Rule.

But if in any of the summes that are to be multiplied, there be a broken number, first work for the whole according to the instructions that you have learned, and then take such part of the given price, as that broken number beareth in proportion to the price, as in the examples following. After you have wrought for 3 s. and for 6 d. then are you to take the $\frac{1}{2}$ of 3 s. 6 d. for the $\frac{1}{2}$ yard, and adde that to the summe. So adding all the 3 products together, which make 43 li. 2 s. 9 d. the just price of 245 $\frac{1}{2}$ Ells, and thus must you doe of all other.

At 3 s. 6 d. the Ell, what 245 $\frac{1}{2}$?

3 s. 6 d. $\frac{1}{2}$

maketh

43-2-9

At

At 16 s. 4 d. the piece what 12 pieces

16 s.

4 d.

maketh pounds

$$\begin{array}{r} 11 \text{ --- } 4 \\ 0 \text{ --- } 4 \text{ --- } 8 \\ 12 \text{ --- } 3 \\ 12 \text{ --- } 0 \text{ --- } 11 \end{array}$$

If one piece cost 4 li. 3 s. 6 d. what 12 pieces

4 li.

3 s.

6 d.

maketh pounds

$$\begin{array}{r} 48 \text{ --- } \\ 1 \text{ --- } 16 \text{ --- } \\ 6 \text{ --- } 6 \\ 6 \\ 50 \text{ --- } 2 \text{ --- } 7 \end{array}$$

The prooffe.

If 12 pieces cost 50 li. 2 s. 6 d. what one piece maketh pounds

$$4 \text{ --- } 3 \text{ --- } 6 \frac{1}{2}$$

Item, touching the manner how to understand the order of this question, and others the like, first seek how many times 12 is contained in 50, which is 4 times, and so resteth 2 pound, which 2 pound converted into shillings, and joyned with the other 2 shillings, maketh 42 shillings: wherein is found 12, three times, resteth 6 shillings: which turned into pence, putting thereto the 6 pence in the first place, it maketh 78, wherein 12 is found 6 times, resteth 6 pence: which containeth 12, but $\frac{1}{2}$ a time, put that $\frac{1}{2}$ to the 6 pence, and then the solution is 4 li. 3 s. 6 d. as appeareth by the practice thereof.

G g 3

Item,

13 Rule.

Item, the like is to be done of any thing that is bought or sold after five score to the hundred, or the Quintall, As for example.

If 100 pound cost 27 li. 13 s. 4d. what one pound?

27li. — 136. — 4d.

20

S. 5/53

12

110



d.64 | o

100.0f3

Maketh 5s. 6 $\frac{1}{2}$ d.

I have wrought this at length for the aid of the young learner, because he should understand how all the Multiplication is set down.

But to work it more neatly, it is by a little understanding ended thus.

27 li. — 13s. — 4d.

20

5553

12

d6/40

1700

Maketh ss. 6th

Item, to the understanding of this and such like questions, the right downe line is all the guide, which is pulled down close by 10 as you see in the example, where 27 pound 13 shillings is reduced all into shillings and maketh 553 shillings.

The γ towards the left hand being separated
with the hanging or right down line, is the just

254877-

number of shillings that answereth to the hundred
of pence, i. 53 shillings, is multiplied by 12, to
reduce them to pence, putting so the 4d. it yet
deth for the multiplication of the first figure, ma
1104 the one beyond the line is written the left
hand, & penny towards the right of the price, then
53 also multiplied by 12 yet deth 53 & thus he g
behind the line towards the left hand, and also 5
pence more towards the price, which is 104 and 5
add together under the line, it maketh 109. It is
there found now, as appeareth by the titles of shil
lings and pence, shillings 6 pence.

Finally, I come now on this side the line towards
the right hand, and under 12 I find first 10, and
then 3, which added together make 13, under
which 10 pence must pay the 100, and it maketh
13 which abbreviated, cometh to 13. So the just
price of one pound after 5 years to the hundred,
maketh 5 s. 6 d. One example more, and so I
will leave this rule.

If 100 cost 10¹/₂ d. what

| | | | |
|----|---|----|-------|
| 6d | 0 | 01 | 0874? |
| 4d | 0 | 0 | 104 |
| 2d | 2 | 2 | 126 |
| 2d | 8 | 11 | 150 |

| | | | |
|---------|---|----------------|-----|
| li. | 4 | 4 ² | |
| | | 20 | |
| Ma- | | — | |
| kerb f. | 8 | 45 | |
| | | 12 | |
| | | 45 | 91 |
| d. | 5 | 100 | 100 |

G g 4

parts of a penny,
Also

Also the like may be done of the other
weights here in England (which is 112 for
every hundred weight) in case you know the
aliquot parts of a hundred weight, which are
these, 56 li. 28 li. 14 li. and 7 li. For 56 li. is
the 2 of 112 li. 28 li. is the 4 of 112 li. 14 li. is
the 8 and 7 li. is 16 part. 1 to 112 li. is 1 to 112

Therefore for 56 li. take the 2 of the summe
of the money that 112 li. weight is worth.

For 28 li. take the 4 of the summe of money
that 112 li. weight is worth.

For 14 li. take the 8 of the summe that 112
li. is worth.

And for 7 li. take the 16 of the summe of money
that 112 li. is worth.

As for example, if 112 li. 10 s. the hundred
pounds weight, that is to say, the 112 li. which
shall 3 quarters and 7 pound cost 2 s. 10 d. 6 gr.

| | | | |
|--------------|--------|-------|-------|
| I.C. | 17 li. | 19 s. | 3 d. |
| 2 quarters | 8 | 19 | 6 |
| 1 quarter | 4 | 9 | 9 |
| 7 pounds | 1 | 2 | 5 1/2 |
| Maked pounds | 14 | 11 | 8 1/2 |

| | | |
|----|---|----|
| 27 | 44 | 11 |
| 2 | 88 | |
| 2 | 176 | |
| 2 | 352 | |
| 2 | 704 | |
| 2 | 1408 | |
| 2 | 2816 | |
| 2 | 5632 | |
| 2 | 11264 | |
| 2 | 22528 | |
| 2 | 45056 | |
| 2 | 90112 | |
| 2 | 180224 | |
| 2 | 360448 | |
| 2 | 720896 | |
| 2 | 1441792 | |
| 2 | 2883584 | |
| 2 | 5767168 | |
| 2 | 11534336 | |
| 2 | 23068672 | |
| 2 | 46137344 | |
| 2 | 92274688 | |
| 2 | 184549376 | |
| 2 | 369098752 | |
| 2 | 738197504 | |
| 2 | 1476395008 | |
| 2 | 2952790016 | |
| 2 | 5905580032 | |
| 2 | 11811160064 | |
| 2 | 23622320128 | |
| 2 | 47244640256 | |
| 2 | 94489280512 | |
| 2 | 188978561024 | |
| 2 | 377957122048 | |
| 2 | 755914244096 | |
| 2 | 1511828488192 | |
| 2 | 3023656976384 | |
| 2 | 6047313952768 | |
| 2 | 12094627905536 | |
| 2 | 24189255811072 | |
| 2 | 48378511622144 | |
| 2 | 96757023244288 | |
| 2 | 193514046488576 | |
| 2 | 387028092977152 | |
| 2 | 774056185954304 | |
| 2 | 1548112371908608 | |
| 2 | 3096224743817216 | |
| 2 | 6192449487634432 | |
| 2 | 12384898975268864 | |
| 2 | 24769797950537728 | |
| 2 | 49539595901075456 | |
| 2 | 99079191802150912 | |
| 2 | 198158383604301824 | |
| 2 | 396316767208603648 | |
| 2 | 792633534417207296 | |
| 2 | 1585267068834414592 | |
| 2 | 3170534137668829184 | |
| 2 | 6341068275337658368 | |
| 2 | 12682136550675316736 | |
| 2 | 25364273101350633472 | |
| 2 | 50728546202701266944 | |
| 2 | 101457092405402533888 | |
| 2 | 202914184810805067776 | |
| 2 | 405828369621610135552 | |
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| 2 | 1623313478486440542208 | |
| 2 | 3246626956972881084416 | |
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| 2 | 831136500985057557610496 | |
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| 2 | 3324546003940230230441984 | |
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| 2 | 6808670216069591511945183232 | |
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| 2 | 18534963333666064832209572896261711109620189043938756993669398528 | |
| 2 | 370699266673321296644191457925234222192403780878751539013042176 | |
| 2 | 741398533346642593288382915850468444384807561757503078026084352 | |
| 2 | 1482797066693285186576765831700936888769615123515006156052168704 | |
| 2 | 2965594133386570373153531663401873777539230247030012312104337408 | |
| 2 | 5931188266773140746307063326803747555078460494060024624208674816 | |
| 2 | 11862376533546281492614126653607495110156920988120049248417349632 | |
| 2 | 23724753067092562985228253307214990220313841976240098496834699264 | |
| 2 | 474 | |

The second Chapter. In the which of the
Reduction of divers measures to
others value by Rules of
Practice.

Now will I shew a few examples of
Practice, in reducing of measures,
as Ells, Yards, Braces, Pawns of
Genoe, &c. Much more would I
have written, but that I feare the
Booke will rise to too great a Volume.

18 Rule.

Item, how many yards of
London are there in 864 Ells of
Amsterdame?

$$\begin{array}{r} 864 \\ 432 \\ 216 \\ \hline 216 \end{array} \quad \begin{array}{r} 864 \\ 216 \\ \hline 648 \end{array}$$


maketh 948 yards of London.

Item, in these and such like questions of Flemish
measure, to be brought into yards Eng-
lish, first take the $\frac{1}{2}$ of the given number, as ap-
peareth in the first example, towards your left
hand; then take half of the product, or the $\frac{1}{4}$ of
the given number, and add those two products to-
gether, as they shall be yards English; as by the
example you may perceive.

The

The second example toward your right hand
is yet briefer then the first, whose work is this:
Take the $\frac{1}{2}$ of the delivered number, and that
product subtrah all out of the given number, and
the rest sheweth your desire. Of these two wayes
use which you thinke best.

The proof.

In 648 yards London, 
How many Ells of Antwerpe?
648
maketh 863 Ells of Antwerpe.

15 Rule.

Item, for the understanding of this worke, first
take the $\frac{1}{4}$ part of the yards of London, which
found, adde that $\frac{3}{4}$ part and the yards together, as
appeareth by the practice, and the product sheweth
the Ells of Antwerpe.

Item, in 20 yards of London,
How many ells of Antwerpe?
maketh 426 Ells
320 yards Proof.

426 Ells
320 yards

Other Reductions

16 Rule.

Item, you shall understand, that forasmuch as
six Braces of Millain, make five Ells of Ant-
werpe, whetsoever according to the Rules of
Practice, you may reduce the one into the other,
by the like reasons aforesaid, in taking the $\frac{1}{2}$ part
and

Rules of Practice

and then subtract the same, to make Ells of Ant-
werpe. And again, by the contrary, taking the
part with adding the given number, to make the
Ells to Braces. As for example,

In 876 Braces, how many Ells of Antwerpe?
876 The contrary.

146

Ells 730 Flemmish.

46 Braces.

816 Braces.

Ells 730 Antwerpe.

182½

Yards 547½ English.

Thus appeareth, that 876 Braces by Practice
make 730 Ells Flemmish, which Ells Flemmish
reduce into English yards.

So again upon the same first position of Bra-
ces, I would know how many yards English
they make.

After the rate that 100 Braces are
worth 82½ yards.

876 Braces.

438

109½

I answer, 547½ yards.

Item, to the understanding of this Worke, and
such like, first take the ½ of the given Braces,
and after take the ¼ of that halfe, or the ¼ of the
given number, and adde them together, and the
products are also yards English.

Item,

Item, three Ells of Rochell make 5 Ells at Lisbon. So likewise three Ells at Lions make 5 Ells at Antwerp.

To work these and such like, double the Ells of Lions, and the Ells of Rochell, and from their products subtract the $\frac{1}{2}$ and the rest shall be the Ells of Antwerp or the Ells of Lisbon. 878

Example.

In 63 Ells of Lions, In 108 Ells of Rochell, how many Ells of Antwerp? of Lisbon?

63

63

128

110

200

231

Ans. 105 Ells of Antwerp. Ans. 166 Ells of Lisbon.

Touching the proof or return of these and such like questions, for a general Rule, you shall first take the $\frac{1}{2}$ of the given number: and adde that $\frac{1}{2}$ and the given number together, and the $\frac{1}{2}$ of that product shall be your desire.

Example.

In 105 Ells of Antwerp, In 166 Ells of Lisbon, how many Ells of Lions? of Rochell?

105
166

Ans. 63 Ells of Lions.

Ans. 100 of Rochell.

Qu.

Questions of Factorage and Interest

briefe and truly resolved by the

Rule of Practice with

an Time.

I Question.

A T 5 shillings per Centum, what comes

Answer. Note

that 3 s. is the fourth of 20 s. I take the $\frac{1}{4}$ part of 8860 li. 15 s. 4d. which makes 2215 li. 3s. 10d.

Now the Root is 100, which you should divide by, so cutting the two last figures away of the pounds, is 22 li.

then multiply 15 li. by 20 s. so adde the 3 unto it, you shall have 303 s. cut away the two last figures, there resteth 3 s. Lastly, there remaines 3 s. which I multiply by 12. to bring into pence, and so I finde 0 d. and $\frac{3}{4}$ remaining, which being abbreviated, makes $\frac{3}{4}$ parts of a peny, so I finde that there is gained 22 li. 3s. 0d. $\frac{3}{4}$ parts of a peny.

2 Quest.

2. *Quest.* At ten s. 1448 li. 16s. 8d.

per centum, what comes unto?

Answer. Note that ten s. is the $\frac{1}{2}$ of 20s. I take the $\frac{1}{2}$ of 1448 li. 10s. 8d. which makes 724 li. 8s. 4d. cut off the two last figures, & there resteth 7 li. then multiply the 24 li. by 20s. and add the 8s. and it maketh 488s. cut the two last figures off, and there resteth 4s. then multiply 88s. by 12d. and take in 4d. and there resteth 1069d. cut off the two last figures, and there resteth ten d. and which is of a peny, so the whole sum is 7 li. 4s. 10d. which is the answer to the question.

3. *Quest.* At 15 s. 1008 li. 12s. *per centum*, what comes

Answer. Note that 15 s. is $\frac{3}{4}$ and $\frac{1}{4}$ of 20s. take the $\frac{3}{4}$ of 1008 li. 12s. there resteth 504 li. 6s. then take the $\frac{1}{4}$ add the together, the totall will bee 756 li. 9s. cut off the two last figures, resteth 7 li. then multiply by 20s. and take in your 6s. it maketh 1129s. cut off the two last figures, there resteth 11s. then multiply by 12d.

there

there commeth 348d. cut off the last two figures, there remain 34 and 8, which being abbreviated maketh 3 parts of a penny, so shall you finde 7 li. 12s. 3d. which is the answer to the question.

4 Quest. At 1 li. per centum, what comes

Answer. Cut away the two last figures, and multiply by 20, and 12, and take in your shillings and pence. And you shall finde 8 li. 13s. 8d. as doth appear by this work.

5 Quest. At 2 li. per centum, what comes

Answer. Multiply the whole summe by 2 li. thus, then cut off the two last figures of your pounds, as you did before, and you shall finde 112 li. then multiply by 20 and by 12, taking in your shillings and pence and you shall finde 112l. 3s. 4d. which is either for Factor or Broker, &c.

6 Quest.

454 Questions of Fellowship

6 Question. At 3 lb. per centum, what comes

Answer. Multiply the summe by 3. thus; then cut off the two last figures, and you shall find 24 s. then multiply by 20, and by 12, taking your shillings and pence, and you shall finde 0 s. 6 d. $\frac{2}{3}$ parts of a peny, which is something above a half peny.

7 Question. At foure per centum, what comes

Answer. Multiply by 4 li. thus, cut off the two last figures. Multiply by 20, and by 12, taking in your shillings and pence, and you shall find 11 li. 19 s. 0 d. $\frac{2}{3}$ parts of a peny, which is something above a farthing.

8 Question. At 5 lb. per centum, what comes

Answer. Multiply the summe by 5. thus; then cut off the two last figures of your summe, and you shall find 11 li. 19 s. 0 d. $\frac{2}{3}$ parts of a peny, which is something above a farthing.

9 Question. At 6 lb. per centum, what comes

Answer. Multiply the summe by 6. thus; then cut off the two last figures of your summe, and you shall find 11 li. 19 s. 0 d. $\frac{2}{3}$ parts of a peny, which is something above a farthing.

Questions of Factoridge. 455

8 *Quest.* At 5 li. $\frac{1}{2}$ per centum, what comes 3658 li. 16 s. 8 d.

Answer. Multiply by unto? 5
5 li. thus, then take the $\frac{1}{2}$ of the whole summe, and place the figures even, then take the $\frac{1}{2}$ of that $\frac{1}{2}$, & adde all three sums together, cut off the two last figures, then multiply by 20 & by 12, taking in your shillings and pence, & you shall find 21017 s. 7 d. $\frac{2}{3}$ parts of a peny, which is the answer to the question.

$$\begin{array}{r} 18294 \quad 03 \quad 14 \\ 18294 \quad 08 \quad 14 \\ 9147 \quad 14 \quad 22 \\ \hline 21017 \quad 05 \quad 18 \\ 20 \\ \hline 420340 \\ 112 \\ \hline 130 \\ 66 \\ \hline 7190 \\ 100 \end{array}$$

9 *Quest.* At 6 li. $\frac{1}{2}$ per centum, what comes 5684 li. 12 s. 6 d.

Answer. Multiply by unto? 6
6 li. and then take $\frac{1}{2}$ of the whole summe, adde them both together, then multiply by 20, & by 12, taking in your odde shillings & pence, and you shall finde 369 li. 10 s. 10 d. $\frac{2}{3}$ parts of a peny, which is the answer to your question.

$$\begin{array}{r} 34107 \quad 15 \quad 0 \\ 2842 \quad 06 \quad 3 \\ \hline 369 \quad 50 \quad 01 \quad 3 \\ 20 \\ \hline 7380 \\ 05 \\ 01 \\ \hline 15 \quad 3 \\ 100 \quad 20 \end{array}$$

456 Questions of Exchange.

10. *Quest.* At 7 li. $\frac{1}{2}$ per centum, what comes 3868 li. 13 s. 4 d. unto?

Answer. Multiply 3868 by 7, then take the 1934.0678, adde them together, 1934.0678, cut off the two last figures, then multiply by 20, you shall finde 290 li. 3 s. the answer to the question.

11. *Quest.* At 8 li. per centum, what comes 2560 li. 17 s. 6 d. unto?

Answer. Multiply 2560 by 8, li. cut off the two last figures, multiply by 20, and by 12, and you shall finde 204 li. 17 s. 5 d. 5 parts of a peny.

Questions of Interest with Time

wrought by Practice.

8 20

Answer. Multiply by

~~0 21 12 08 28 04 12 01~~

~~0 21 12 08 28 04 12 01~~

~~0 21 12 08 28 04 12 01~~

Question.

A T 6 per Centum

what comes un-
to for 1 month

268 li. 16 s. 8 d.

28 13 00 0

28 13 00 0

li. 234. 08. 4

20

f. 688

142

180

388

d. 106 0 12

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

100 15

Answer. Multiply by
6 li. there commeth
2813 li. 00 s. 0 d. then
take for 1 month the $\frac{1}{12}$
of the Totall, and you
shall find 234 li. 8 s. 4
d. of the two last fi-
gures of the pounds,
Multiply by 20 and by
12, taking in your odde
mony, and you shall
finde 2 li. 6 s. 10 d. 2 parts of a peny, which is
the answer to the question.

Hh 2

2 *Quest.*

2 *Quest.* At 7 li. $\frac{1}{2}$ per centum, what comes unto for 3 months.

Answer. Multiply by 7 li. then take $\frac{1}{2}$, adde them two together, then for your two months take the $\frac{1}{2}$ of the Totall, multiply by 20 and 12, taking in your odde shillings and pence, and you shall find 47 l. 10 s. 1 d. $\frac{2}{3}$ parts of a peny, which is the answer to the question.

3 *Question.* At 8 li. per centum, what comes unto for 3 months.

Answer. Multiply by 8 li. then for your 3 months take $\frac{1}{2}$ of the Totall, multiply by 20, and by 12, adding in your odde shillings and pence, and you shall finde 197 li. 5 s. 11 d. $\frac{1}{3}$ parts of a peny, your demand.

3800 li. 12 s. 8 d.

28604 08 8

1900 06 4

28504 15 0

47 50 15 10

120

10 15

12

30

16

1 10 10

10 10

10 10

9864 li. 16 s. 11 d.

7898 16 8

107 29 12 8

120

92

12

192

93

11 12 6 3

100 50 25

4 Quest. At 6 li. per centum, what comes unto for 4 months.

Answer. Multiply by 6 l. then take $\frac{1}{2}$ adde both together, then for your 4 months take $\frac{1}{2}$ part of the whole, cut away your two last figures, multiply by 20, and by 12; adde in your odde shillings & pence, and you shall finde 131 li. 14 s. 10 d. $\frac{1}{2}$ parts of a peny your demand.

3648 18 9
 3940 06 6
 39524 04 1
 131 14 10
 14 9 12
 184
 91
 1094 47
 100 50

5 Question. At 8 per centum, what comes unto for 5 months.

Answer. Multiply by 8 li. then for 5 months take $\frac{1}{2}$ of the Totall, cut off the two last figures of your pounds, Multiply by 20 and by 12, add in your odde shillings and pence, and you shall finde 100 li. 13 s. 4d. your demand.

3020 li. 00 s. 00 d.
 24160 00 00
 6040 00 00
 24026 13 4
 100 66 13
 100 00 00
 13 33
 12 00
 70
 33
 4 00

6 Question. At 8 per centum, what comes unto for 6 months.

Answer. Multiply by 8 li. then for your 6 months take the 100 of the Total, cut off the two last figures of your pounds. Multiply by 12, taking in your odd shillings and pence, & you shall find 322 li. 8 s. 5 d. 1/2 parts of a penny, your desire.

7 Quest. At 8 li. per centum, what comes unto for 4 months,

Answer. Multiply by 8 li. then for your 7 months take 1/4 and 1/2 of the Total, cut off the two last figures of your pounds, then multiply by 20 and 12, taking in your odd money, and you shall finde 275 li. 2 s. 1 d. 1/3 your desire.

8060 li. 12 s. 0 d.

64484. 16 s.

322 li. 8 s. 5 d.

20

848

12

96

48

3763819

1005025

1005025

1005025

1005025

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1005025

1005025

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1005025

1005025

1005025

1005025

1005025

1005025

8. Question. At 8 $\frac{1}{2}$ per centum, what comes unto for 8 months.

Answer. Multiply by 8 li. then for 8 months take $\frac{1}{2}$ of the totall cut off the two last figures of your pounds, then multiply by 20, and by 12 adde in your odde money, and you shall finde 116 li. 5 s. 9 d. your desire.

3680 ll. 08 s. 03 d.
29443. 04 0
9814. 08 0
9814. 08 0
116128
20
576
12
912 128 0
100 50 25

9. Quest. At 8 li. per centum, what comes unto for 9 months.

Answer. Multiply by 8 li. then for your 9 months take $\frac{1}{2}$ and $\frac{1}{2}$ of the whole summe, cut off the two last figures of the pounds, then multiply by 20, and by 12: taking in your odde shillings and pence, and you shall finde 221 li. 1 s. 11 d. $\frac{1}{2}$, which is something above a farthing.

29479. 12 0
14739. 16 9
7369 18 0
221 09 14 0
20
1 94
12
188
94
11 28 14 1
100 50 25

10 *Quest.* At 6 $\frac{1}{2}$ per centum, what comes unto for 10 months.

Answer. Multiply by 6 li. then take the $\frac{1}{2}$ and $\frac{1}{4}$ of 100 li. add all 3 summes together, then for the 10 months take $\frac{1}{2}$ and $\frac{1}{4}$ of the Totall, adde them together, cut off the two last figures of the pounds, multiply by 20, and 12, adding in your shillings and pence, cutting off the last figures of your shillings & pence, you shall find 5 li. 12 s. 6 pence your desire.

100 li. 0 s. 0 d.
 6000
 3000
 1500
 750
 375
 187 10 0
 225 00 0
 562 10 0
 89 10 0
 1250
 12
 100
 50
 600

Questions of Interest.

463

11 *Quest.* At 8 li. 886 li. 16 s. 0 d.

per centum, what comes unto for 11 months.

Answer. Multiply by 8 li. then for 11 months take 0 and 7 from the Total, adde all three summes together, cut off the two last figures of your pounds. Multiply by 20 and by 12 adding in of your shillings and pence, cutting off the two last figures of your shillings and pence and you shall finde 65 li. 0 s. 7 d. 11 parts of a peny, your desire.

12 *Quest.* At 8 li.

per centum, what comes unto for 12 months.

Answer. Multiply by 8 li. cut off the two last figures of the pounds, Multiply by 20, and by 12 adding in your shillings and pence, cut off the two last figures of your shillings, and the two last of your pence, and you shall finde 726 li. 8 s. 11 d. 12 parts of a peny, your desire.

F I N I S.

The

The third Chapter teacheth of the Order
and work of the Rule of three in broken
numbers after the Trade of Merchants
digesting something from Master
Records, which is comprehen-
ded in three Rules.

NOW, that I have somewhat intreated
of the Rules of Practice, I will give
a few instructions, after my simple or-
der, for the working of the Rule of three in bro-
ken numbers wherein I shall need to say the
lesse, because I hope the studious learner, that
hath travelled any thing in the Grounds of Arts,
is not unfurnished of knowledge capable to under-
stand me.

But before I deliver any instructions for
broken numbers, I will propound a question
which shall be wrought three sundry wayes,
thereby to shew, as it were, three degrees of
Comparison: how farre the Rule of three in
broken, for more speed of work, differeth
from the whole, which I rather set down for
a view, that the studious herein may be more
desirous to attain broken, leaving any more
to discourse in Dialogue form, but onely to
give instructions where need is: and in the
rest to put forth the questions with their an-
swers.

The Golden Rule of 3.

461

Here the product is found according to the rule of three, and thus
My first question is thus

If one yard cost 6 s. 8 d. what are 789 worth at that rate?

The first way.
 Now let you have seen the three former parts of the Rule of three, whose products had been found d. and s. and lastly li. I will deliver three more in order following:
 Here the product of the summe are pence, according to the nature of the middle numbers.

numbers or fractions.
 1 The first four shall be under questions of Fraction containing in the second place.
 2 The second four shall be under questions containing in the second of third place.
 3 The third four of Questions in all three places.
 I answer 263 li.

The second way.
 Upon the first Rule for a Fraction containing in the second place.
 1 6 s. 789
 3 15780 s.

Here the product of the summe are s. according to the nature of the middle number.

The third way.
 In setting down the question to be found the work I turn four pence into the part of a shilling, which is 4; and then the question standeth thus:
 Here

466 .The Golden Rule of 3

Here the product is pounds, according to the title of the second number.

Now 8 s. 2 d. 8 fl. 8 b. 8 n. 11
 889 163
 332

shd edT
 .yew

Now that you have seen the three former vertues of the Rule of three, whose products have first brought forth d. next s. and lastly li. I will deliver three notes in order following : and with them a dozen questions that shall shew the work of the Rule of three in broken numbers or Fractions.

Note these three well.

- 1 The first foure shall be sundry questions of a Fraction comming in the second place,
- 2 The second foure shall be of two Fractions comming in the second or third place.
- 3 The third foure of Fractions in all three places.

shd edT
 .yew

Notes upon the first Rule for a Fraction comming in the second place.

1 Rule.

The first variety.

My first Question is this.
 If one yard cost me 3 s. 4 d. what are 756 worth at that price ?

In setting down the question to perform the work, I turn four pence into the part of a mil-ling, which is $\frac{1}{4}$; and then the question standeth thus :

shd edT
 .yew

1 — 63 $\frac{1}{4}$ — 756 To

To the ready working of this question, and all such other like: my first note is this, which take for a generall Rule; that when any one Fraction shall come, either in the second or third place, that the Denominator of that Fraction or Fractions, must alwayes be brought unto the Number, or Numerator of the first place; and thereby multiply the one into the other.

A generall Rule.

And this benefit is always gotten by the virtue of bringing the Denominator of the second Number Fractions unto the first place: For the Fraction in the middle number, is now released; and the product that cometh of the multiplication, is of the nature and like denomination of the whole number in the second place which here are shillings.

Note this.

Whereupon now to work the Question, I bring 3, the Denominator of the Fraction in the second place, unto my first Number 1, with a line set under thus 1, and the 3 under it thus, 1 over 3, saying once 3, is 3, my Divisor; that done, reduce 3, saying 3 times 3 is 9, and the other 1 over 3, make 10; my second number in the Rule of three, by which 10 I doe multiply my last number 756, as appeareth by the work thereof, and it yeeldeth 7560 shillings my Dividend.

The 1st Rule of three.

Then dividing 7560 by 3, my Divisor, it yeeldeth an quotient 2520 shillings, which maketh 126 pounds, as appeareth here most plainly, both by the example and the work.

At

And Answ^r 4d, the vant, what 755 p^{rs} 755 p^{rs} 755 p^{rs}

the price now into the proportion 3 to 4, which is the proportion of the price now to the price then.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

the price then is the price now, which is the price then.

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the price now is the price then, which is the price then.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

The second variety.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

the price then is the price now, which is the price then.

the price now is the price then, which is the price then.

of this my first Rule or note, is converted into the rule of my second number, which here are pounds. Now followeth the division performed in my Division 6, to make an end of this question,

28

758 (126 which makes 126 li. as before,

666

And thus much for the variety in working that question.

And now followeth another.

My second Question.

If one yard of Cotton cost 8½d. what 859?

1 ——— 8½ ——— 859

Notes upon my second Rule for two

Fractions coming in the

cond and third place.

2577

2577

My first Question

If one Ell cost 13s. 4d. what 1221

1221

1221

1221 (1221) 1221

1221 (1221) 1221

1221 (1221) 1221

This Question was also wrought like the first,

and brought forth the same answer.

as before was taught in the first Rule.

My

My

bring 3 the Denominator of the second Fraction unto your first number 1, setting a line under it thus, $\frac{1}{3}$, Saying once 3 is 3, that done, bring 8 the Denominator of the third Fraction, setting it under 3, and multiply them together, saying, 3 times 8 maketh 24, which 24 is your Divisor. (Now have you done with the Denominator 8) therefore you shall put a line under, thus, $\frac{1}{3}$. And the like line also under 8, setting or pulling down under them their own Numerators, that is, 2 under 3, and also 1 under 8, as appeareth in the example, which Numerators for a generall rule evermore to be pulled down of custome in sight, to multiply the one by the other, according to the tenour of the Rule of Three. Then I multiply the one by the other, saying, once 2 is two, which signifieth 2 li. being of the nature and like denomination of the middle number, which 2 li. is, to be reduced into shillings, otherwise it cannot be divided by my first number 24.

Then dividing 40 by 24, the quotient bringeth forth $1\frac{2}{3}$. So much is $\frac{2}{3}$ of an Ell worth after that rate. Otherwise although 2 pound could not be divided by 24, yet it might have been abbreviated to $\frac{1}{12}$ of a pound: which is worth 1 s. 8 d. as before.

If

sight, to be the two numbers, that of duty ought to be multiplied together; which done, I bring 1, being the lesser figure under 7, multiplying them together, it maketh 14, which are of the nature of the middle number: that is to wit, pounds, which 14 cannot aptly be divided among 24: therefore are reduced into shillings, as is plainly to be seen in the example: then 280 shillings parted among 24 yeeldeth for his portion 11 s. 8 d. your desire, and the just price of 1 of an £11. Otherwise 14, though it could not be divided by 24, might by *addition* or *division* in broken numbers have been divided or abbreviated to $\frac{7}{12}$, which in effect being reduced to his known parts, maketh 11 s. 8 d. as before. But my good will and meaning is to aid young beginners: therefore have I reduced the 14 pound into shillings, which is the easier way.

Now followeth the Example.

$$\begin{array}{r}
 280 \text{ s. } 11 \text{ s. } 8 \text{ d.} \\
 \underline{24} \quad \underline{14} \quad \underline{2} \\
 11 \text{ s. } 8 \text{ d.}
 \end{array}$$

280 s. I answer, 11 s. 8 d.

The Golden Rule of 3.

The third Example.
-If one yard cost me 2s. 6d. what 24s. 6d. worth of yards?

Answer. First put 6 d. into the parts of a Gallie, and then the question standeth thus:

vided among 24; therefore are reduced into

Item, to the ready understanding of this, and all such like, according as before hath been declared, bring the *Denominators* of the second and third *Fractions* unto the first place, multiplying them the one into the other, all which make 8 for the common *Divisor*. Then next reduce your second number $\frac{3}{2}$, saying, two times 2 is 4, and 1 is 5; as was taught in the example aforesaid. Lastly, reduce your third number $345 \frac{1}{4}$ all into fourths, and they make 1381, which 1381 is to be multiplied by 5, according to the tenor of the *Rule of three*: which done, maketh 6905 s. and divided by 8, your *Divisor* yeeldeth in *Quotient* 862 $\frac{1}{2}$ s. which maketh in pounds 43 li. 3 s. 1 $\frac{1}{2}$ and so much are the $345 \frac{1}{4}$ yards worth at that price.

The same question wrought again by two shillings 6 pence, is now converted into the parts of a pound; and standeth thus :

$$1 - \frac{1}{2} - \frac{1}{4} - \frac{1}{8} - \frac{1}{16} - \frac{1}{32} - \frac{1}{64} - \frac{1}{128} - \frac{1}{256} - \frac{1}{512} - \frac{1}{1024} - \frac{1}{2048} - \frac{1}{4096} - \frac{1}{8192} - \frac{1}{16384} - \frac{1}{32768} - \frac{1}{65536} - \frac{1}{131072} - \frac{1}{262144} - \frac{1}{524288} - \frac{1}{1048576} - \frac{1}{2097152} - \frac{1}{4194304} - \frac{1}{8388608} - \frac{1}{16777216} - \frac{1}{33554432} - \frac{1}{67108864} - \frac{1}{134217728} - \frac{1}{268435456} - \frac{1}{536870912} - \frac{1}{1073741824} - \frac{1}{2147483648} - \frac{1}{4294967296} - \frac{1}{8589934592} - \frac{1}{17179869184} - \frac{1}{34359738368} - \frac{1}{68719476736} - \frac{1}{137438953472} - \frac{1}{274877906944} - \frac{1}{549755813888} - \frac{1}{1099511627776} - \frac{1}{2199023255552} - \frac{1}{4398046511104} - \frac{1}{8796093022208} - \frac{1}{17592186044416} - \frac{1}{35184372088832} - \frac{1}{70368744177664} - \frac{1}{140737488355328} - \frac{1}{281474976710656} - \frac{1}{562949953421312} - \frac{1}{1125899906842624} - \frac{1}{2251799813685248} - \frac{1}{4503599627370496} - \frac{1}{9007199254740992} - \frac{1}{18014398509481984} - \frac{1}{36028797018963968} - \frac{1}{72057594037927936} - \frac{1}{144115188075855872} - \frac{1}{288230376151711744} - \frac{1}{576460752303423488} - \frac{1}{1152921504606846976} - \frac{1}{2305843009213693952} - \frac{1}{4611686018427387904} - \frac{1}{9223372036854775808} - \frac{1}{18446744073709551616} - \frac{1}{36893488147419103232} - \frac{1}{73786976294838206464} - \frac{1}{147573952589676412928} - \frac{1}{295147905179352825856} - \frac{1}{590295810358705651712} - \frac{1}{1180591620717411303424} - \frac{1}{2361183241434822606848} - \frac{1}{4722366482869645213696} - \frac{1}{9444732965739290427392} - \frac{1}{18889465931478580854784} - \frac{1}{37778931862957161709568} - \frac{1}{75557863725914323419136} - \frac{1}{151115727451828646838272} - \frac{1}{302231454903657293676544} - \frac{1}{604462909807314587353088} - \frac{1}{1208925819614629174706176} - \frac{1}{2417851639229258349412352} - \frac{1}{4835703278458516698824704} - \frac{1}{9671406556917033397649408} - \frac{1}{19342813113834066795298816} - \frac{1}{38685626227668133590597632} - \frac{1}{77371252455336267181195264} - \frac{1}{154742504910672534362390528} - \frac{1}{309485009821345068724781056} - \frac{1}{618970019642690137449562112} - \frac{1}{1237940039285380274899124224} - \frac{1}{2475880078570760549798248448} - \frac{1}{4951760157141521099596496896} - \frac{1}{9903520314283042199192993792} - \frac{1}{19807040628566084398385987584} - \frac{1}{39614081257132168796771975168} - \frac{1}{79228162514264337593543950336} - \frac{1}{158456325028528675187087900672} - \frac{1}{316912650057057350374175801344} - \frac{1}{633825300114114700748351602688} - \frac{1}{1267650600228229401496703205376} - \frac{1}{2535301200456458802993406410752} - \frac{1}{5070602400912917605986812821504} - \frac{1}{10141204801825835211973625643008} - \frac{1}{20282409603651670423947251286016} - \frac{1}{40564819207303340847894502572032} - \frac{1}{81129638414606681695789005144064} - \frac{1}{162259276829213363391578010288128} - \frac{1}{324518553658426726783156020576256} - \frac{1}{649037107316853453566312041152512} - \frac{1}{1298074214633706907132624082305024} - \frac{1}{2596148429267413814265248164610048} - \frac{1}{5192296858534827628530496329220096} - \frac{1}{10384593717069655257060992658440192} - \frac{1}{20769187434139310514121985316880384} - \frac{1}{41538374868278621028243970633760768} - \frac{1}{83076749736557242056487941267521536} - \frac{1}{166153499473114484112975882535043072} - \frac{1}{332306998946228968225951765070086144} - \frac{1}{664613997892457936451903530140172288} - \frac{1}{1329227995784915872903807060280344576} - \frac{1}{2658455991569831745807614120560689152} - \frac{1}{5316911983139663491615228241121378304} - \frac{1}{10633823966279326983230456482242756608} - \frac{1}{21267647932558653966460912964485513216} - \frac{1}{42535295865117307932921825928971026432} - \frac{1}{85070591730234615865843651857942052864} - \frac{1}{170141183460469231731687303715884105728} - \frac{1}{340282366920938463463374607431768211456} - \frac{1}{680564733841876926926749214863536422912} - \frac{1}{1361129467683753853853498429727072845824} - \frac{1}{2722258935367507707706996859454145691648} - \frac{1}{5444517870735015415413993718908291383296} - \frac{1}{10889035741470030830827987437816582766592} - \frac{1}{21778071482940061661655974875633165533184} - \frac{1}{43556142965880123323311949751266331066368} - \frac{1}{87112285931760246646623899502532662132736} - \frac{1}{174224571863520493293247799005065324265472} - \frac{1}{348449143727040986586495598010130648530944} - \frac{1}{696898287454081973172991196020261297061888} - \frac{1}{1393796574908163946345982392040522594123776} - \frac{1}{2787593149816327892691964784081045188247552} - \frac{1}{55751862996$$

Items, After I have brought here my second and

and third Denominator unto my first place, and found 32 to be my Divisor, having thus finished my first place with all things unto him belonging (which is meant of bringing and multiplying the Denominators of the second and third Fractions into him) I then goe in hand to see what is to be done in my second place, where presently of custome I pull down my Numerator under 8, being the figure in sight that shall multiply my third number.

Then lastly, I reduce $345\frac{1}{2}$ all into fourths as afore was practised, which maketh 1381, the which 1381, I am to multiply by 1 my second number, they are nothing increased, but by the Metamorphosis of my work they are now 1381 pound, being of the nature of the middle number, as I have often shewed you, which divided by 32 my Divisor yeeldeth 43 pound, and $\frac{1}{2}$ which $\frac{1}{2}$ of a pound reduced into known numbers, make 3 shillings 1 d, as before.

Example.

$$1 \frac{1}{2} \text{ --- } 345\frac{1}{2} \text{ --- } 108$$

$$32 \overline{) 1381} \quad \begin{array}{r} 43 \\ 128 \\ \hline 101 \end{array} \quad \begin{array}{r} 5 \\ 160 \\ \hline 41 \end{array}$$

NOW follow foure other questions, which are in all three places broken numbers: or whole and broken together.

11 3

Item,

Item, First for the finding out of your *Divisor*, you shall take this for a most certain, and generall rule: That you must multiply the *Numerator* of the first number in the question, by the *Denominator* of the second: And that *Product* again by the *Denominator* of the third: And the totall thereof shall be your *Divisor*.

Secondly, for a generall rule to find out your *Dividend*, multiply the *Denominator* of the first number by the *Numerator* of the second, and the whole thereof by the *Numerator* of the third. And the totall thereof shall evermore be your *Dividend*.

Now for an example, I propound this question, thereby to make my meaning more plain, and to shew you, as I have done in the rest, the manner and order of the work,

If $\frac{3}{4}$ of any Weight or measure cost $\frac{3}{4}$ of a pound, or 20s. What are $\frac{1}{2}$ of the like Weight or measure worth after that rate?

Example.

$$\frac{3}{4} \text{ --- } \frac{3}{4} \text{ --- } \frac{1}{2}$$

Item, For the more plainer understanding thereof, and all other the like, in broken Numbers: First, you shall pull down two, the *Numerator* of the first Number or Fraction, with a line under, thus, $3 \frac{1}{2}$: that done, according as you have learned before, bring 6, the *Denominator* of the second Fraction, and set it under

under two, multiplying the one into the others which maketh 16. Then lastly, bring 8, the *Denominator* of the third *Fraction*, and set it under 16, multiplying that 16 by 8, which amounteth to 96, or else for more brieft, multiply 6 by 8, saying 6 times 8, makes 48, which 48 set under 2, and multiply the one into the other, it maketh 96, as before. And this 96 is the first *number* in the *Rule of three*. That shall alwayes for a most generall Rule be your *Divisor*.

Secondly, to work for your *Dividend*, you shall, (as it hath been sufficiently declared before) pull downe 5, the *Numerator* of your second *Fraction*, and set it under 6, with a line under, thus 6.

That done (as you know) you are to pull down 3, the *Numerator* of the third *Fraction*, and set it under 8, with a line under it, thus 8, multiplying the one into the other, according to the tenour of the *Rule of three*; which maketh 19. Then according to my note, forget not to bring the *Denominator* of the first *Fraction*, which is 3, under 15, and multiply them together, which maketh 45, which 45 is your *Dividend*, and are of the nature of *Denomination* of the middle *number*, as I have taught you before: And therefore are 44 li. which aptly cannot be divided by 96. Therefore you shall reduce the 45 li. into s. as you see performed in the Example, which amounteth to 900s. which divided by 96 your *Di-*

viser, it yeeldeth 9 s. and $\frac{1}{2}$ of a shilling which in lesser termes is $\frac{1}{2}$: which $\frac{1}{2}$ in money maketh $4\frac{1}{2}$ d. and so much will the aforesaid $\frac{1}{2}$ cost, as by the work following shall appear.

The Example.

| | | | |
|----|-----|-----|--|
| 2 | 35 | 8 | |
| 3 | 6 | 8 | |
| 2 | 5 | 3 | |
| 6 | 5 | 13 | |
| 12 | 15 | 96 | |
| 8 | 3 | 900 | |
| 96 | 45 | 96 | |
| | 20 | | |
| | 900 | | |

Otherwise though 45 could not be divided by 96, yet by Division in broken numbers it might have been abbreviated to $\frac{1}{2}$ of a pound, which reduced into known parts, will make 9 s. $4\frac{1}{2}$ d. as before.

Now my second example shall be the proof of this question.

If $\frac{1}{2}$ yards cost $\frac{1}{2}$ of a pound, or 20 shillings; what shall $\frac{1}{2}$ cost?

Answer. Work as was taught you before, and you shall have your desire.

Here

into 1000, which is the first fraction. Then multiply the second fraction by the first, and pull down under 4, of the number 1000, ready to multiply this number by 288, which is performed as the first number 288 is reduced into halves. Then lastly, I multiply that by 4, the

Here as appeareth by the work, the multiplication being ended, 240 is to be divided by 288, which to some perchance may seem hard, yet notwithstanding is the work good. Therefore abbreviate 240 by 288, as you see here is practised: and the end of your abbreviation shall come to $\frac{5}{6}$ your desire.

$$\begin{array}{r} \text{Otherwise, } 240 \overline{) 12060305} \\ 288 \overline{) 14472306} \\ 888 \end{array}$$

$$\begin{array}{r} \text{Otherwise, } 240 \overline{) 405} \\ 288 \overline{) 486} \end{array}$$

The third Question.

If 2 Ells cost 13 s. 4d. what 156 $\frac{1}{2}$ Ells?

Answer. To work this question the shortest way: reduce 13 s. 4d. into the parts of a pound, which is $\frac{53}{16}$.

Then as you did afore, after you have set down the question, the Numerator of the first Fraction 3 is pulled down under 4, and Denominators of the other two fractions multiplied into

The Golden Rule of 3.

into him, which maketh 18, your *Divisor*:

Then the *Numerators* of the second *fraction* is pulled down, under 3 of custome now in sight, ready to multiply my third number, by which is performed as soon as the last numbers 156 $\frac{1}{2}$ is reduced into halves.

Then lastly, I multiply that product by 4, the *Denominator* of the *fraction*: it yeeldeth 1504, which I divide by 18, and my quotient is 139 $\frac{1}{2}$ kind of a pound remaining, which is worth 2 s. 2 d. And so much will 156 $\frac{1}{2}$ Ells cost, as by the work following doth appeare.

$$\begin{array}{r}
 4 \quad 3 \quad 313 \quad 47 \\
 3 \quad 2 \quad 2762 \quad \text{li.} \\
 \hline
 6 \quad 826 \quad 2304 \quad (139 \frac{1}{2}) \\
 18 \quad 4 \quad 2888 \\
 \hline
 2504 \quad 22
 \end{array}$$

The fourth question.

If 2 $\frac{1}{2}$ Ells cost 1 $\frac{1}{2}$ pounds, what cometh 29 $\frac{1}{2}$ Ells to?

Item, to the workmanship of this question, first reduce your second number in saying three times 1 is 3, and 2 is 9. Then bring the multiplication of the *Denominators* of the second and third *fractions*, which maketh 12: and multiply that 2 by 3 your first *Numerator*, and it maketh 6, which is your *Divisor*.

Then the *Reduction* of the second number, which

which is 5, multiplied by 117 the product of the last number, reduction, make 585, which 585 yet resteth to be multiplied by 2, the denominator of the Fraction in the first place, yeeldeth 1170, which divided by your Divisor 60 yeeldeth 19 pound, 10 s. as appeareth by the work thereof.

Thus having now touched the 12 questions whereof I first pretended, which with diligence and oft Practice, I trust are sufficient to aid the desirous unto the working of any broken numbers, I will now treat of divers necessary Rules incident unto traffick, as hereafter followeth.

The fourth Chapter treateth of losse and gain in the Trade of Merchandise.



If one yard cost 6 s — 8 d. and the same is sold again for 8 s — 6 d. the question is, what is gained in 100 pounds laying out on such commodities?

Answer. The Rule of three direct, applied two manner of wayes to doe the same: The one is to say, If 6 s give 8 s, what giveth 100? Multiply and divide, and look what your quotient bringeth forth above your laying out, is the neat gaines and relation

to your question: If you follow the work, your solution will bring forth 127 li. — 10 s. which is 27 li. 10 s. more then your principall, and so much is gained in the 100 pounds laying out.

Item, to work it the other way, which I take the nearest, seek the difference betwixt the just price and the other price, which is one shilling ten pence, then say by the rule of three, If 6 s. gain 1 s. what shall 100 pound gain? Multiply and divide, and you shall find 27 li. 10 s. and so much is gained in 100 li. laying out.

You may use which of these two wayes you think good.

The proof.

If a yard of clothe be delivered for 8 s. 6 d. whereupon was gained a tenth part of 27 li. 10 s. in 100 pounds laying out: The question is, what the yard cost at the first hand?

Answer. Put your gain 27 li. 10 s. to 100 pounds, all maketh 127 li. 10 s. Then say, If 127 li. 10 s. give but a 100 pounds, what giveth 8 s. 6 d. Work, and you shall find 6 s. 8 d. the true solution to your question.

Yet another Example or Proof upon the first Question.

If one yard cost 6 s. 8 d. the question is, at what price the same is to be sold again, for to gain

Losse and Gain.

483

gain 27 li. 10 s. in 100 pounds laying out 7

Answer. Say by the Rule of three, if 100 li.

gain 27 li. 10 s. what giueth 63 s. Multiply
and diuide, and you shall finde 8 s. 6 d. your true
solution.

If one Ell cost 7 s. 8 d. and be sold again for
8 s. 6 d. The question is, What is gained in 20
pounds laying out in such commodities.

Answer. Seek the difference betwixt the just
price, and the other price which is ten pence, and
then apply the Rule of three, as before is taught,
saying, If 7 s. give 3 shillings; what giueth 20
li. Multiply and diuide, and you shall find 2 li.
3 s. and so much is gained in 20 li. laying out.

The proof, also by an example of losse.

A Merchant hath bought Holland cloth, at 8
s. 6 d. the Ell, which promiseth not to his
expectation, whereupon he is content to lose 2 li. 3
s. in 20 pounds laying out. The question is, what
price ought to be made of the Cloth, abating this
losse?

Answer. Doe as before in Gains hath been
taught, putting 2 li. 3 s. to your 20 pound,
all together, maketh 22 li. 3 s. Then say by
the Rule of three, If 22 li. 3 s. give but 20 l.
what shall come of 8 s. work, and you shall
finde 7 s. 8 d. the just price that the Ell ought
to be sold for after the rate of this losse.

Thus

Thus it appeareth evidently, as in company the Rule is applicable as well to gain as losse.

If 20 $\frac{1}{2}$ yards cost 36 li. 10 s. how shall I sell the same again $\frac{1}{3}$ of the principall, or to make of 3, 4. Which is all one?

Answer. By the Rule of three, if 3 doe give 4, what will 36 $\frac{1}{2}$ give? Multiply and divide, and you shall find 48 $\frac{1}{2}$ li. Then say again, if 20 $\frac{1}{2}$ yards do give 48 $\frac{1}{2}$ pounds, as well principall as gain, what will one yard be worth at that price? Multiply and divide, and you shall find 2 li. 10 s.

If one Ell of Cloth cost me 8 s. 8 d. and afterwards I sell 10 $\frac{1}{2}$ Ells thereof for 5 li. 13 s. 4 d. I would know, whether I win or lose: and how much upon the 100 pounds of money.

Answer. See first at 8 s. 8 d. the Ell, what 10 $\frac{1}{2}$ Ells comes to, and you shall finde 4 li. 11 s. and I sold the same for 5 li. 13 s. 4 d. so that I did gain upon the 10 $\frac{1}{2}$ Ells 22 shillings 4 d. Then if you would know how much is gained in 100 pounds, I say by the Rule of three, if 4 li. 11 s. did gain 22 s. 4 d. what will 100 pounds gain? Multiply and divide, and you shall find 24 li. 10 s. 10 d. and so much is gained in the 100 pound of money.

If 12 $\frac{1}{2}$ yards cost me 11 pound five shillings, and I sell the yard again for 16 shillings, the question is whether I do win or lose, and how much in or upon the pound of money?

Ans-

Answer. Look what the 100 yards come to at 6s. the yard, and you shall find ten pound. But they cost 11 pound 5 shilling. So there is lost upon the whole 1 pound 5s. Then to know how much is lost in the pound, say by the *Rule of three*, if 11 $\frac{1}{2}$ pound do lose 1 $\frac{1}{2}$ pound, what will 1 pound lose? Multiply and divide, and you shall find 2s. 3d. $\frac{1}{2}$ and so much is lost in the pound of money.

Ques. If I sell the 100 weight of any commodity for 4 pound, whereupon I doe lose after ten pound in the 100 pound, I demand how much I shall lose or gain in the 100 lb. if in case I shall sell the same for 4 pound ten shillings.

Answer. Say, if 90 pound yeeld 100, how much will 4 give? Multiply and divide, and you shall finde 4 $\frac{1}{2}$. Then say again, if 4 $\frac{1}{2}$ give me 4 $\frac{1}{2}$, what will 100 come to? Multiply and divide, and you shall find 101 pound $\frac{1}{2}$ which is more then 100 pound by 1 pound 5 shillings: and so much is gained in the 100 pound.

A Merchant hath sold Currants for the sum of 430 pound, and he hath gained therein after ten pound in the 100 pound. The question is to know how much he gained in all.

Answer. Say by the *Rule of three*. If 100 pound doe gaine ten pound, what will 430 pound gaine? Multiply and divide, and you shall find 43, and so much hath he gained in all.

Questions: 26. I

Of some yarde worth 8 li. 6 s. 8 d. for how much shall
10 yards be sold again after 8 li. 6 s. 8 d. in the
100 pounds? *Answer.* First, adde 8 li. 6 s. 8 d. to 100.

Then say, if 100 li. do give 108 $\frac{1}{2}$ s. for principall
and gain, what will 28 $\frac{1}{2}$ s. principall yeeld?
Multiply and divide, and you shall find 30 $\frac{1}{2}$ s.
Then say, again, by the *Rule of three*, if 1 yarde
do give 30 $\frac{1}{2}$ s. (which is as well the principall
as the gain) what shall ten yarde give? Multi-
ply and divide, and you shall find 45 li. 8 s. 9 d.
And for the same price, shall the ten yarde be
sold, for to gain after the rate of 8 li. 6 s. 8 d.
upon the 100.

A branch or proof out of this Question.

A Merchant hath sold clothes for 15 li. 8 s. 9 d.
and he hath gained in the whole the summe of
1 li. 3 s. 9 d. The question is, to know how
much he hath gained in the 100 pound?

Answer. To know this, first rebate the gains
from the price, and there will remain 14 li. 5
s. 9 d. Then say by the *Rule of three direct*, if
14 li. $\frac{1}{2}$ give me 1 li. 3 s. 9 d. what will 100 li.
give? Multiply and divide, and you shall find
8 li. 6 s. 8 d. the effect desired, the proof is ap-
parent in the question before.

Yet

Yet another branch or prooffe of the
first Question.

If 100 yds be delivered for 15 li. 8 s. 3 d.
whereupon was gained after the rate of 18 li. 6 s.
8 d. upon the 100 pound, the question is, what the
yard did cost at the first hand?

Answer. First, say by the Rule of Three, if 100
with principall and gain yeeld 15 li. 8 s. 3 d. shil-
lings, what shall 100 yeeld? Multiply and divide,
and you shall finde 30 1/2 s. Then say again by the
Rule of Three, if 108 of principall and gain give
but 100, what shall 30 1/2 s. of principall and
gain yeeld? Work, and you shall finde 21 1/2 s.
And so much did the yard cost at the first penny.

If our yard cost 36 s. how much shall 12 yards
be sold for, to gain after the rate of 22 li. in the
100?

Answer. First, say, If 100 give 120 li. prin-
cipall and gain, what will 36 s. give? Multiply
and divide, and you shall finde 39 1/2 s. Then say
again by the Rule of Three, If our yard of prin-
cipall and gain yeeld 39 1/2 shillings, what shall
12 yards gain? Multiply and divide, and you
shall finde 23 li. 15 1/2 s. which 1/2 s. in known
number, is 2 1/2 d. And for the same price shall
the 12 yards be sold, to gain after the rate of
10 in the 100.

The Proof.

If 12 yards be sold for 23 li. 15 1/2 d. where-

upon is gained after 10 li. in the 100. The question is, What the yard cost at the first penny? 15 Y

Answer. First say, If 23 li. 15 s. what one yard? Multiply and divide, and you shall find 30 s. Then say again by the Rule of Three, If 10 pounds give me a 100, what shall 30 s. give? Work, and you shall find 36 s. the just price of the yard at the first hand.

Item, When one Merchant selleth wares to another, and he giveth to the buyer 10 li. 6 s. 8 d. upon the score, or 20 li. The question is, How much shall the buyer give upon the 100 li. after that rate? And you shall find the gain yeeld And so much did the yard cost at the first penny.

Answer. First add 1 li. 6 s. 8 d. unto 20 li. and they are 21 s. Then say, If 20 pound give 21 s., what shall 100 give? Multiply and divide, and you shall find 105 s. 8 d. the buyer getteth after the rate of 6 s. li. upon the 100 li.

Gentle Reader, Other necessary questions appertaining to Loss and Gain, you shall have in the eighth Chapter of this Treatise.

And for the same price shall the 100 be sold, to gain after the rate of 10 s. li.

The Proof.

If 100 be sold for 105 s. 8 d. where-
upon

The fift Chapter entreateth of Losse and Gain upontime, wrought by the double Rule of Three, or by the Rule composed: which is contained In four speciall selected branches, or questions of diuers formes, each one of them springing from the first question, and each one of them also being a proof to other, &c.

Question. One yard cost me 2 s. 8 d. ready money, and after I sell the same again for 2 s. 10 d. to be paid for it at the end of three months: the question is, what I gain upon the same in 12 months.

Answer. First say, if 10 gain, what shall 100 li. gain? Multiply and divide, and you shall find $6\frac{1}{2}$ li. Then say again, by the Rule of three, if three months gain 64 pound, what shall 12 months gain? Work, and you shall find 25 li. and so much shall I gain in 12 months after that rate.

Now, You may also work it all at one working by the first part of the Rule of three composed, saying, if 2 $\frac{1}{2}$ d. in three months do gain $\frac{1}{2}$ of a shilling (which is 1 d.) what will 100 li. gain in 12 months? Which for thy further encouragement, the work of this one example I

have here put down, to verifie that I affirme in
the first part of this *Gravice*, that this
Rule, and so all others, more rejoyceth in *Bro-*
ken then in *Whole*.

The first Chapter concerning the Rule of
Single, and by the Rule of Double
s. moneths li. mo.
2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12.
- 8. 11. 14. 17. 20. 23. 26. 29. 32. 35. 38. 41.
- 44. 47. 50. 53. 56. 59. 62. 65. 68. 71. 74. 77. 80.
- 83. 86. 89. 92. 95. 98. 101. 104. 107. 110. 113. 116. 119. 122. 125. 128. 131. 134. 137. 140. 143. 146. 149. 152. 155. 158. 161. 164. 167. 170. 173. 176. 179. 182. 185. 188. 191. 194. 197. 200. 203. 206. 209. 212. 215. 218. 221. 224. 227. 230. 233. 236. 239. 242. 245. 248. 251. 254. 257. 260. 263. 266. 269. 272. 275. 278. 281. 284. 287. 290. 293. 296. 299. 302. 305. 308. 311. 314. 317. 320. 323. 326. 329. 332. 335. 338. 341. 344. 347. 350. 353. 356. 359. 362. 365. 368. 371. 374. 377. 380. 383. 386. 389. 392. 395. 398. 401. 404. 407. 410. 413. 416. 419. 422. 425. 428. 431. 434. 437. 440. 443. 446. 449. 452. 455. 458. 461. 464. 467. 470. 473. 476. 479. 482. 485. 488. 491. 494. 497. 500. 503. 506. 509. 512. 515. 518. 521. 524. 527. 530. 533. 536. 539. 542. 545. 548. 551. 554. 557. 560. 563. 566. 569. 572. 575. 578. 581. 584. 587. 590. 593. 596. 599. 602. 605. 608. 611. 614. 617. 620. 623. 626. 629. 632. 635. 638. 641. 644. 647. 650. 653. 656. 659. 662. 665. 668. 671. 674. 677. 680. 683. 686. 689. 692. 695. 698. 701. 704. 707. 710. 713. 716. 719. 722. 725. 728. 731. 734. 737. 740. 743. 746. 749. 752. 755. 758. 761. 764. 767. 770. 773. 776. 779. 782. 785. 788. 791. 794. 797. 800. 803. 806. 809. 812. 815. 818. 821. 824. 827. 830. 833. 836. 839. 842. 845. 848. 851. 854. 857. 860. 863. 866. 869. 872. 875. 878. 881. 884. 887. 890. 893. 896. 899. 902. 905. 908. 911. 914. 917. 920. 923. 926. 929. 932. 935. 938. 941. 944. 947. 950. 953. 956. 959. 962. 965. 968. 971. 974. 977. 980. 983. 986. 989. 992. 995. 998. 1001. 1004. 1007. 1010. 1013. 1016. 1019. 1022. 1025. 1028. 1031. 1034. 1037. 1040. 1043. 1046. 1049. 1052. 1055. 1058. 1061. 1064. 1067. 1070. 1073. 1076. 1079. 1082. 1085. 1088. 1091. 1094. 1097. 1100. 1103. 1106. 1109. 1112. 1115. 1118. 1121. 1124. 1127. 1130. 1133. 1136. 1139. 1142. 1145. 1148. 1151. 1154. 1157. 1160. 1163. 1166. 1169. 1172. 1175. 1178. 1181. 1184. 1187. 1190. 1193. 1196. 1199. 1202. 1205. 1208. 1211. 1214. 1217. 1220. 1223. 1226. 1229. 1232. 1235. 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3728. 3731. 3734. 3737. 3740. 3743. 3746. 3749. 3752. 3755. 3758. 3761. 3764. 3767. 3770. 3773. 3776. 3779. 3782. 3785. 3788. 3791. 3794. 3797. 3800. 3803. 3806. 3809. 3812. 3815. 3818. 3821. 3824. 3827. 3830. 3833. 3836. 3839. 3842. 3845. 3848. 3851. 3854. 3857. 3860. 3863. 3866. 3869. 3872. 3875. 3878. 3881. 3884. 3887. 3890. 3893. 3896. 3899. 3902. 3905. 3908. 3911. 3914. 3917. 3920. 3923. 3926. 3929. 3932. 3935. 3938. 3941. 3944. 3947. 3950. 3953. 3956. 3959. 3962. 3965. 3968. 3971. 3974. 3977. 3980. 3983. 3986. 3989. 3992. 3995. 3998. 4001. 4004. 4007. 4010. 4013. 4016. 4019. 4022. 4025. 4028. 4031. 4034. 4037. 4040. 4043. 4046. 4049. 4052. 4055. 4058. 4061. 4064. 4067. 4070. 4073. 4076. 4079. 4082. 4085. 4088. 4091. 4094. 4097. 4100. 4103. 4106. 4109. 4112. 4115. 4118. 4121. 4124. 4127. 4130. 4133. 4136. 4139. 4142. 4145. 4148. 4151. 4154. 4157. 4160. 4163. 4166. 4169. 4172. 4175. 4178. 4181. 4184. 4187. 4190. 4193. 4196. 4199. 4202. 4205. 4208. 4211. 4214. 4217. 4220. 4223. 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4724. 4727. 4730. 4733. 4736. 4739. 4742. 4745. 4748. 4751. 4754. 4757. 4760. 4763. 4766. 4769. 4772. 4775. 4778. 4781. 4784. 4787. 4790. 4793. 4796. 4799. 4802. 4805. 4808. 4811. 4814. 4817. 4820. 4823. 4826. 4829. 4832. 4835. 4838. 4841. 4844. 4847. 4850. 4853. 4856. 4859. 4862. 4865. 4868. 4871. 4874. 4877. 4880. 4883. 4886. 4889. 4892. 4895. 4898. 4901. 4904. 4907. 4910. 4913. 4916. 4919. 4922. 4925. 4928. 4931. 4934. 4937. 4940. 4943. 4946. 4949. 4952. 4955. 4958. 4961. 4964. 4967. 4970. 4973. 4976. 4979. 4982. 4985. 4988. 4991. 4994. 4997. 5000. 5003. 5006. 5009. 5012. 5015. 5018. 5021. 5024. 5027. 5030. 5033. 5036. 5039. 5042. 5045. 5048. 5051. 5054. 5057. 5060. 5063. 5066. 5069. 5072. 5075. 5078. 5081. 5084. 5087. 5090. 5093. 5096. 5099. 5102. 5105. 5108. 5111. 5114. 5117. 5120. 5123. 5126. 5129. 5132. 5135. 5138. 5141. 5144. 5147. 5150. 5153. 5156. 5159. 5162. 5165. 5168. 5171. 5174. 5177. 5180. 5183. 5186. 5189. 5192. 5195. 5198. 5201. 5204. 5207. 5210. 5213. 5216. 5219. 5222. 5225. 5228. 5231. 5234. 5237. 5240. 5243. 5246. 5249. 5252. 5255. 5258. 5261. 5264. 5267. 5270. 5273. 5276. 5279. 5282. 5285. 5288. 5291. 5294. 5297. 5300. 5303. 5306. 5309. 5312. 5315. 5318. 5321. 5324. 5327. 5330. 5333. 5336. 5339. 5342. 5345. 5348. 5351. 5354. 5357. 5360. 5363. 5366. 5369. 5372. 5375. 5378. 5381. 5384. 5387. 5390. 5393. 5396. 5399. 5402. 5405. 5408. 5411. 5414. 5417. 5420. 5423. 5426. 5429. 5432. 5435. 5438. 5441. 5444. 5447. 5450. 5453. 5456. 5459. 5462. 5465. 5468. 5471. 5474. 5477. 5480. 5483. 5486. 5489. 5492. 5495. 5498. 5501. 5504. 5507. 5510. 5513. 5516. 5519. 5522. 5525. 5528. 5531. 5534. 5537. 5540. 5543. 5546. 5549. 5552. 5555. 5558. 5561. 5564. 5567. 5570. 5573. 5576. 5579. 5582. 5585. 5588. 5591. 5594. 5597. 5600. 5603. 5606. 5609. 5612. 5615. 5618. 5621. 5624. 5627. 5630. 5633. 5636. 5639. 5642. 5645. 5648. 5651. 5654. 5657. 5660. 5663. 5666. 5669. 5672. 5675. 5678. 5681. 5684. 5687. 5690. 5693. 5696. 5699. 5702. 5705. 5708. 5711. 5714. 5717. 5720. 5723. 5726. 5729. 5732. 5735. 5738. 5741. 5744. 5747. 5750. 5753. 5756. 5759. 5762. 5765. 5768. 5771. 5774. 5777. 5780. 5783. 5786. 5789. 5792. 5795. 5798. 5801. 5804. 5807. 5810. 5813. 5816. 5819. 5822. 5825. 5828. 5831. 5834. 5837. 5840. 5843. 5846. 5849. 5852. 5855. 5858. 5861. 5864. 5867. 5870. 5873. 5876. 5879. 5882. 5885. 5888. 5891. 5894. 5897. 5900. 5903. 5906. 5909. 5912. 5915. 5918. 5921. 5924. 5927. 5930. 5933. 5936. 5939. 5942. 5945. 5948. 5951. 5954. 5957. 5960. 5963. 5966. 5969. 5972. 5975. 5978. 5981. 5984. 5987. 5990. 5993. 5996. 5999. 6002. 6005. 6008. 6011. 6014. 6017. 6020. 6023. 6026. 6029. 6032. 6035. 6038. 6041. 6044. 6047. 6050. 6053. 6056. 6059. 6062. 6065. 6068. 6071. 6074. 6077. 6080. 6083. 6086. 6089. 6092. 6095. 6098. 6101. 6104. 6107. 6110. 6113. 6116. 6119. 6122. 6125. 6128. 6131. 6134. 6137. 6140. 6143. 6146. 6149. 6152. 6155. 6158. 6161. 6164. 6167. 6170. 6173. 6176. 6179. 6182. 6185. 6188. 6191. 6194. 6197. 6200. 6203. 6206. 6209. 6212. 6215. 6218. 6221. 6224. 6227. 6230. 6233. 6236. 6239. 62

of 25 pound upon the 100 pound in 12 moneths?
Answer. First say, if 25 gain 1, what shall
 100 pound gain? Multiply and divide, and you
 shall finde 65 pound. Then say again for the
 second work, if 25 pound be come of 12 mo-
 neths, what shall come of 65? A Work, and you
 shall finde three moneths, the just terme of
 time that the Cloth ought to be delivered at
 22 s. 10 d. to gain 25 pound upon the 100 li-
 in 12 moneths.

If one yard of steele 2 s. 8 d. ready money, for
 what price shall I sell the same again to be paid at
 the end of three moneths, so that I may gain after
 the rate of 25 pound in the 100 pound for 12
 moneths?

Answer. First say, if 12 gain 25 li, what shall
 3 moneths gain? Multiply and divide, and you
 shall finde 6 s. 11 d. Then say for the second
 work, if 100 li give 106 s. what giveth
 3 s. 11 d.? Work, and you shall finde 2 s. 10 d.
 and for that price must the yard be sold to gain
 after 25 pound in the 100 pound for twelve
 moneths.

Many other of these questions I might here
 have delivered, but for feare the Book would
 rise to too thick a volume, and so to make the
 price so much the dearer, whereby it might
 not be so portable to my Countreymen as I
 wish it. But these 4 I have of purpose framed
 in this order, having relation one to another;
 assuring you, that what question soever may
 be proposed within the compasse of this Rule

you shall finde by one of these, to make a solution. And moreover, divers others are yet to be delivered, where the Creditor giveth divers dayes of payment, which can never be well wrought, nor yet understood, unless you can first find by Art the just times that all those payments, how different soever they be, ought to be paid at once: whereupon first I think good here to give some instructions unto such a Rule, for it is the onely aid for the finishing of such questions as hereafter shall follow.

The sixth Chapter increaseth of Rules of payment, which is a right necessary Rule, and one of the chiefeft handmaids that attendeth upon buying and selling, &c.

Example.



Admerchant hath owe a summe of money, whereof the $\frac{1}{4}$ is to be paid at six moneths; and the $\frac{1}{4}$ at eight moneths, and the rest at a year. If he would pay all as one payment, the question is, what time ought to be given for it. Answer. I have omitted the quantity of the summe, for you shall understand the Rule is appli-

appliable, and yeeldeth true solution fo what
 summe soever shall be proposed. But now for
 order sake in teaching, I doe imagine the sum
 to be 60 pounds, whereupon the matter of this
 work is to multiply the proportionate part
 of the money by the time, as in company. Then
 20 being the first payment, and the 4 of 60,
 which I multiplied in broken numbers by 6,
 his time of payment maketh 4 months, which in
 whole numbers, at 40 pounds, by 2 Moneths,
 appeareth by the example in the operation, ma-
 keth two moneths, next by 4 Moneths,
 30 which is the 1 multi-
 plied by his term 8, by 2 Moneths,
 yeelds 4 moneths, then
 the rest which is 10 li.
 must needs be abbreviated into the proportion
 it beareth to 60, which is 1, which I multi-
 plied by his time 2 moneths, produceth ma-
 keth two moneths. All which added together,
 as appeareth in the operation, maketh eight
 moneths, which is the just time that all those
 payments ought to be paid as once.

A Marchant hath 800 li. to pay, the 1 third
 ready money, the 1 at 6 moneths, the 1 at 1
 moneth, and the rest at a year. The question is
 if he would pay all at one payment, what time
 ought to be given him?

Answer

Answer. The ready money here is never multiplied, then multiplied by two months as you did before, make it, then by 4, produce 2 months, as appeareth here in the operation. But now for the rest of the money you cannot multiply it until you have sought what proportion it beareth to 800 pounds. Therefore you must subtract the ready money, the 4 and 1 out of the principall. The rest will be 65; 11, which you must look what part it beareth to the principall, which you shall finde to be $\frac{1}{4}$, the same you must also multiply by his time 10 months, and it yeeldeth one month, so all make 3 months, as appeareth in the operation.

A Merchant is to pay 1200 li. in three termes that is to wit, 400 li. in two weeks, and 600 li. at four monthes, lastly, 200 li. in five monthes. The question is, in what time they ought to be paid.

Answer. Proportionate the parts, and you shall finde that 400 is $\frac{1}{3}$ part, and for 600 you shall finde $\frac{1}{2}$, and likewise 200 is the $\frac{1}{3}$ part, which multiply by their times as before, and you shall have 3 weeks, more eight weeks, and lastly 3 weeks, which together maketh 13 weeks, or three monthes, your desire.

A Merchant is to pay 600 pound in three termes, whereof 100 pound is paid present, more

300 pound in ready dayes, and the rest in 12 moneths, reckoning thirte dayes to a moneth, The question is, what time ought these payments to be paid at once?

Answer. Work and you shall finde two moneths.

The seventh Chapter intreateth of buying and selling in the Trade of Merchandize, wherein is taken part ready money, and divers dayes of payment given for the rest, and what is woane or lost in the 100 pound forbearance for 12 moneths more or lesse, according to the quantity of money, or proportion of time, &c.

A Merchant hath bought satins which cost eight shillings the yard ready money: and he selleth the same again to another man for 10s. the yard, but he giveth two dayes for the payment, that is to say, three moneths for the one half, and sixe moneths for the other halfe. The question is to know how much the seller doth gain upon the 100 li. in 12 moneths after that rate.

Answer. Seek first by the Rules of payment, at what time those two payments ought to be paid at once, and you shall finde foure moneths,

moneths, at which time the second Merchant ought to have paid the whole entire payment. And therefore say by the first part of the Rule of three composed :

If 8 shillings in 4 moneths doe gaine 4 s. what will 100 li. gain in 12 moneths?

Multiply and divide, and you shall finde 75 pounds, as appeareth in the example, and so much doth the first Merchant gain upon the 100 pounds in 12 moneths.

A Merchant hath sold 50 Clothes, at 9 $\frac{1}{2}$ li. the piece, to be paid the one $\frac{1}{3}$ at foure moneths, the $\frac{1}{3}$ at five moneths, and the $\frac{1}{3}$ at seven moneths, and the sellers minde is to take no more but after eight pounds in the 100 for 12 moneths. The question is now, what the first Merchant gaineth in the sale of these Clothes after that rate.

Answer. First look what the 50 Clothes come to at that price, and you shall finde 475 pounds. Then secondly, according to your direction in the Rules of payment, seek at what time all the payments are to be performed, at once. And you shall finde 4 $\frac{1}{2}$ moneths. Then thirdly say, by the first part of the Rule of three composed

composed. If 100 li. in 12 moneths gain 8 li. what will 475 li. gain in 45 moneths. Work and you shall finde 15 li. and $\frac{1}{2}$ of a pound, which is the neat gains that the first Merchant hath after the rate afore said.

A Merchant hath bought Holland at 7 s. 3 d. the Ell ready money, and he selleth the same at gain for 8 s. 4 d. the Ell, to be paid in part in ready money, whereof part at 2 moneths, and the rest at 4 moneths. The question is how to know how much the first Merchant doth gain upon the 100 pounds in 12 moneths after that rate. I bid to be Answer. According to the direction delivered you in the Rule of payment, the ready money is not to be multiplied. Then working for the other two payments to finde out the true proportion at what time they ought to be paid at once, you shall finde first at two moneths $\frac{2}{3}$ of a moneth. And the rest of the moneth which is $\frac{1}{3}$ multiplied by his term 4 moneths, yeeldeth $\frac{4}{3}$ moneths, both which added together make $2\frac{2}{3}$ moneths, the just time that both the payments ought to be performed at once. And therefore say by the first part of the rule of three composed, if 74 s. in $2\frac{2}{3}$ moneths do gain $\frac{1}{2}$ of a pound, what shall 100 pounds gain in 12 moneths after that rate. Work, and you shall finde 28 $\frac{2}{3}$ pounds. And so much doth he gain upon 100 pounds in 12 moneths.

A Merchant hath bought 30 Clothes at 6 pounds the piece for ready money. Afterward he selleth nine of them for 7 pound the piece, for three moneths

moneths; and the other twenty he selleth for 180 pounds the piece, for 4 moneths terme. The question is now, what he garmeth upon 100 pounds in 12 moneths.

Answer. First finde the value of the thirty clothes, which amount to 180 pounds. Secondly, seek what the ten pieces come to at 7 pounds, and what the twenty pieces come to at 80 pounds; the one comes to 70, and the other to 160, both which together make 230, which is 50 pounds more then they cost. Thirdly, as I have taught you in the Rule of payment, proportionate the first and second prices unto the proportion they beare unto 230, the product of the two prices, and you shall finde 9 for the first, and 11 for the latter. Then fourthly, multiply those parts by their times, and you shall have 81 and 121 both which together maketh three whole moneths, and 1 of a moneth, which is the just time that both those payments ought to be paid at once. Then say by the first part of the Rule of three composed: If 180 pounds in 3 $\frac{1}{12}$ moneths do gain 50 pounds, what shall 100 gain in twelve moneths? Multiply and divide, and you shall finde 90 $\frac{1}{12}$ pound, and so much doth he gain upon 100 pounds in twelve moneths.

Now Merchants hath bought. Cloth upon which cost him 9 shillings the pound ready money. The question is now, at what price he ought to sell the cloth weight. To wit, 12 pounds to be paid the 1 in two moneths; and the residue at the end of three

three months, so that he may gain after the rate
of ten pounds upon 100 pounds for 12 months.

Answer. Seek first by the Rule of payment
at what term both the payments ought to be
paid at once, where the $\frac{2}{3}$ multiplied by his
term two moneths, maketh $\frac{4}{3}$ moneths, and
Likewise for the next payment, which is $\frac{1}{4}$ mul-
tiplied by his term three moneths maketh $\frac{3}{4}$
moneths, both which added together, maketh
 $2\frac{1}{4}$ moneths, which is the time, that both the
payments ought to be paid at once. Then say
by the Rule of three, if 12 moneths doe give
me ten pounds, what will $2\frac{1}{4}$ moneths give?
Multiply and divide, and you shall finde $4\frac{2}{3}$
pounds. Then say again by the Rule of three,
If one pound cost me 9s. what will 112 pounds
cost? Multiply and divide, and you shall finde
50 li. 8s. Then say once againe: If one pound
doe give 100 s. what will $4\frac{2}{3}$ pounds give?
Multiply and divide, and you shall finde y^e in
115. 13. 4. and for that price, ought I to sell
112 pound of Cinnamon to be paid at the two
severall payments aforefaide, to gain thereby
after the rate of ten pounds upon the hundred
pound in twelve moneths.

Briefe

Brief Rules for our hundred weight here

at London, which is after 112

pound for the 160

Item, **to know what multiplieth the pence that one pound is worth, is worth by 7, and divideth the product by 112, shall finde how many pence the money is a pound worth, both in weight, and in value, and so on in like manner.**

Example. **Let us take 112 pounds**

and to pence, the pound weight, what is 112

pounds weight worth done yet 112. 28

Answer. **Multiplie 112 by 7, and thereof com-**

meth 784, the which divideth by 112, and you shall

finde 7 pounds. And thus the 112 pounds is

worth 7 pounds. And thus the rate of 112 pence

the pound aforesaid is 7 pounds, and so on in like manner.

Answer. **Multiplie 6 by 15, and thereof com-**

meth 90, the which divide by 7, and you shall

finde 12 2/3 d. So much is one pound worth

when the 112 pounds did cost 6 pounds.

The

And for to much shall the 754 pound be sold

The eight Chapter intreateth of Tares and Allowances of Merchandize sold by

weight, and of losse and gains therein; &c.



T 16 pound the 100 Suttle,
what shall 89 pound Suttle
be worth, in giving 4
pound weight upon every
100 for Treat?

Answer. *Rule 4.* Unto
100, and you shall have 104.

Then say by the Rule of

Three, If 104 be worth 16 pounds, what are 89
pounds worth? Multiply and divide, and you
shall finde 137 lb. 13 s. 10 d. and so much shall
the 89 pound weight be worth.

Item, at 3 s. 4 d. the pound weight what shall
754 pound be worth, in giving 4 pounds
weight upon every hundred for Treat?

Answer. See first by the Rule of Three what
the 100 pound is worth, saying, If one cost
3 s. what 100? Multiply and divide, and you
shall finde 16 s. pounds. Then add 4 unto one
100, and they are 104. Then say again by the
Rule of Three, If 104 be sold for 16 s. pounds,
for how much shall 754 be sold for? Multiply
and divide, and you shall finde 120 lb. 18 s. 3 d.

And

And for so much shall the 754 $\frac{1}{2}$ pound be sold
for at 3s. 4d. the pound, in giving 4 upon
the 100.

Other necessary bills taken before for the
finding of Treasurers, casting up of what is sold
gar, &c. which for that it is a mystery to omit: if
any lack instructions that way, they shall finde me
ready to pleasure them.

Item, If 100 pounds be worth 36 $\frac{1}{2}$ s. d. what
shall 860 pounds be worth in rebating 4 pounds
upon every hundred for tare and cloffe?

Answer. Multiply 860 by 4, and thereof
cometh 3440, the which divide by 100, and
you shall have 34 $\frac{1}{2}$ pounds, abate 84 $\frac{1}{2}$ from
860, and there will remain 825 $\frac{1}{2}$ pounds.
Then say, by the Rule of three: If 100 pound
cost 36 $\frac{1}{2}$ s. what will 825 $\frac{1}{2}$ cost after that rate?
Multiply and divide, and you shall finde 30 li.
2s. 8 $\frac{1}{2}$ d. And so much shall the 860 cost in
rebating four pounds upon every hundred, for
tare and cloffe.

Item, whether doth he lose more that giveth 4
pounds upon the 100, or he that rebateth 4 pounds
upon the 100?

Answer. First note, that he that giveth 4
pounds on 100, giveth 40 s. for 100. And he
which rebateth 4 pounds upon the 100, giveth
the 100 for 96. Therefore say by the Rule of

three, if 104 be delivered for 100, for how much shall the 100 be delivered? Multiply and divide, and you shall finde $96\frac{2}{3}$, and he which rebatheth 4 in the 100, maketh but 96 pounds of 100, so that he loseth 4 pounds in the 100, and the other which giveth 4 pounds upon the 100 loseth but $3\frac{1}{3}$ pounds upon the 100. Thus you may see, that he which rebatheth 4 pounds in the 100, loseth more by $\frac{1}{3}$ pound in the 100 pounds, then the other which gave 4 pounds upon the 100, for tare and cloffe.

If 100 pounds of any thing cost me 23 s. 4d. the question is, how I shall sell the pound, to gain after the rate of ten pounds, upon the 100 pound.

Answer. Say by the Rule of three, if 100 pounds give 100 pounds, what shall 23 $\frac{1}{2}$ s. give? Multiply and divide, and you shall finde $1\frac{1}{2}$ pounds. Then say again, if 100 pound be worth $1\frac{1}{2}$ pounds, what is one pound worth? Multiply and divide, and you shall find 3 d. $\frac{1}{2}$. And so much is the pound worth in gaining ten pounds upon the 100.

Item; A Grocer hath bought C. weight of commodity for 6 li. 10 s. The question is now to know how many pounds thereof he shall sell for 33 s. 4d. to gain 20 s. in C. weight.

Answer. Adde 20 s. unto 6 li. 10 s. and they
L 1 make

make 7 li. 10 s. Then say, if 7 $\frac{1}{2}$ pound yeeld me 112 pound, what shall 1 $\frac{1}{2}$ pounds yeeld? Multiply and divide, and you shall finde 24 $\frac{1}{2}$ li. And so many pound ought he to sell to gain 20 s. in his C. weight.

If one pound weight cost 3 s. 4 d. and I sell the same again for 4 s. what is gained in a hundred pound of mony laid out in that commodity?

Answer. You may say, If 3 $\frac{1}{2}$ s. give 4. what will 100 pound gain? But then when you have found, you must subtract 100 pounds out of the Product, the rest is your neat gain: or else to produce the neat gain in your work at the first, Subtract the just price out of the overprice, as I taught before in the first beginning of Losse and Gain, and your conclusion shall be all one. Multiply and divide, by which of the two wayes you think good, and you shall finde that he gaineth 20 pounds in the 100 pound.

Item, If the pound weight which cost 4 s. be sold again for 3 s. 4 d. I demand what is lost in the 100 pounds of mony.

Answer. Say, If 4 s. lose 3 s. what shall 100 lose? Multiply and divide, and you shall finde 16 li. 13 s. 4 d. and so much is lost upon the 100 of mony.

Item, If C. weight of any commodity cost 45 pounds, and the buyer repening, woulde lose five pounds

pounds in the 100 of money, I demand how the pounds may be sold, but lose to be neither more nor less then after the rate aforesaid of five by the hundred?

Answer. By the Rule of three, if 100 lose 5, what shall 45 lose? Work, and you shall finde $2\frac{1}{2}$ pound, which rebated from the principall 45, resteth 42 l. 15 s. Lastly say, if 112 yeeldeth but 42 li. 15 s. what one pound? Multiply and divide, and you shall finde 7 s. 7 d. 17. And so much is the pound worth after that losse.

A Grocer hath bought three pieces of Raisins, weighing 175 $\frac{1}{2}$ pounds, 182 $\frac{1}{2}$ pounds: 191 pounds: tare for each fraile 2 $\frac{1}{2}$ pounds, as 25 $\frac{1}{2}$ s. the C. weight. The question is, what they amount to in money?

Answer 8 li. $\frac{11}{2}$ s. $\frac{4}{2}$ d.

A Grocer hath bought three sacks of Almonds weighing 267 $\frac{1}{2}$ pound, tare two pound, 257 $\frac{1}{2}$ pound, tare 2 $\frac{1}{2}$ pound, 252 $\frac{1}{2}$ pound, tare 3 pound, at 2 s. 10 $\frac{1}{2}$ d. the pound, what amount they to in money?

Answer 110 li. 12 s. $\frac{3}{2}$ d.

The ninth Chapter intreateth of lengths and breadths of Arras and other Clothes, with other questions incident unto length and breadth.

IF a piece of Arras bee 7 Elles and 1/2 long, and 5 Elles and 1/2 broad, how many Elles square doth the same piece contain?

Answer. Multiply the length by breadth, that is to say, $7\frac{1}{2}$ by $5\frac{1}{2}$; And thereof will come 43 $\frac{1}{2}$ Elles; so many Elles square doth the same piece contain.

Item, more, a piece of Arras doth contain 22 Elles square, and if the same were in length 3 Elles, I demand how many Elles in breadth the same piece doth contain.

Answer. Divide 22 Elles by $3\frac{1}{2}$; and thereof cometh 6 $\frac{1}{2}$; So many Ells doth the same contain in breadth.

Item, more, a Merchant hath $3\frac{1}{2}$ Elles of Arras, at $1\frac{1}{2}$ Elles broad, which he will change with another man for a piece of Arras, that is $2\frac{1}{2}$ Elles square. The question is, how many Elles of that squarenesse ought the first Merchant to have?

Answer.

Answer. Multiply the first Merchants piece, his length by the breadth, and you shall finde it containeth $5 \frac{1}{2}$ Els, which $7 \frac{1}{2}$ Els you shall divide by $1 \frac{1}{2}$ and you shall finde $6 \frac{1}{2}$ Els, and so many Els of that squareness ought the latter Merchant to give the first.

Item, A Student hath bought $3 \frac{1}{2}$ yards of broad cloth, at 7 quarters broad, to make a gown, and should line the same throughout with Lamb as a foot square each skin: the question is how many skins he ought to have?

Answer. Seek first the number of yards square that his cloth containeth, which to doe, multiply $3 \frac{1}{2}$ his length, by $1 \frac{1}{2}$ his breadth, and you shall finde $6 \frac{1}{2}$ yards square: then say by the rule of three, if one yard square give 9 foot, what shall $6 \frac{1}{2}$ Work, and you shall finde $55 \frac{1}{2}$ skins.

Item, more, a Lawyer hath a rich piece of seating come home which is 24 foot and 3 inches long, and 7 foot and $2 \frac{1}{2}$ inches high: the Joyner is to be paid by the yard square: the question is, How many yards this containeth?

Answer. Multiply his length by his breadth, that is to wit $24 \frac{1}{2}$ foot by $7 \frac{1}{2}$ foot, and you shall finde $174 \frac{1}{2}$ foot square, which 174 you shall divide by 9 (for so many foot make a yard square) and you shall finde 19 yards 3 foot

and $\frac{22}{4}$ of a foot, and so many yards doth this piece hold.

Item, bought a piece of Holland cloth containing 36 Ells Flemish. The question is how many Ells English it makes.

Answer. You must note, that five Ells Flemish doth make but three Ells English.

Therefore say by the Rule of three, if five Ells Flemish make but three Ells of English, how many Ells English will 36 $\frac{1}{2}$ Ells Flemish make? Multiply and divide, and you shall finde 21 $\frac{3}{4}$ and so many English doth 36 $\frac{1}{2}$ Ells Flemish contain. The like is to be done of others.

Item, more, I have bought 342 Ells Flemish of Arras work, at two Ells broad Flemish, and I would line the same with Ell broad Canvas of English measure. The question is, how many Ells English will serve my turn?

Answer. For as much as three Ells English are worth five Ells Flemish, therefore put three Ells English into his square, in multiplying three by himselfe, which maketh nine. Likewise multiply the English Ell, which is five quarters, every way into himselfe squarely, and you shall finde 25. Then multiply 342 which is the length of the piece, by 7 which is the breadth, and thereof cometh 684. then say

say by the *Rule of three*, as before, if 25 Ells square of *Flemmish* measure be worth nine Ells square of *English* measure, what are 684 of *Flemmish* measure? Multiply and divide, and you shall finde 246 $\frac{1}{2}$ Ells *English*.

The same is also wrought by the *Backer Rule of three*, in seeking the squares contained in the *Flemmish* Ell of two Ells broad (which are 18) and also in seeking the squares contained in the *English* Ell (which are 25) then say by the *Rule of three* backward. If 18 quarters require 342 Ells, what shall 25 quarters give? Multiply and divide by the *Rule of three* Reverse, and you shall find as before 246 $\frac{1}{2}$ Ells *English*?

Item, more, at three shillings foure pence the *Flemmish* Ell, what is the *English* Ell worth after the rate?

Answer. Say, If three quarters give 3 $\frac{1}{2}$ s. what giveth five quarters? Multiply and divide, and you shall finde 5 s. 6 $\frac{1}{2}$ d.

Item, more, at 8 s. 4 d. the *Flemmish* Ell square, what is the *English* Ell worth after that rate?

Answer. According to the reason of the last Question, consider that a *Flemmish* Ell square is equall to nine quarters of a yard *English*, and

an *English* Ell square is equal to 25 quarters of a yard. Therefore say by the *Rule of three*, if 9 quarters give 1 $\frac{1}{2}$ s. what 25 quarters? Work and find 23 s. 1 $\frac{1}{2}$ pence. And so is the *English* Ell worth.

Item, more, at 6 s. 8 d. the Ell square: what shall a piece of Cloth cost that is 7 $\frac{1}{2}$ Ells long, and 3 $\frac{1}{2}$ Ells broad?

Answer. Multiply the breadth by the length, and you shall finde 24 $\frac{1}{2}$ Ells square cost 6 $\frac{1}{2}$ s. what 24 $\frac{1}{2}$ Ells? Multiply and divide, and you shall find 8 pounds, 2 s. 6 pence, and so much the same piece of cloth cost.

Item, more, a Mercer sold 3 pieces of Silk. To wit 24 $\frac{1}{2}$ 13 $\frac{1}{2}$ and 25 yards, at 9 $\frac{1}{2}$ s. the yard, and was glad to receive in part of payment again, a cloth containing 34 $\frac{1}{2}$ yards at 7 $\frac{1}{2}$ shillings the yard. The question is now, what the Debtor oweth the Creditors debt? Work, and you shall finde he oweth the Mercer 22 pounds, 3 shillings, 2 $\frac{1}{2}$ pence.

The

The tenth Chapter intreateth of reducing of Pawns of Geanes into English yards.



Ote that 100 Pawnes doe make 26 yards, whereupon three Pawnes doe make one yard, and one Pawn after the rate and proportion is $\frac{1}{26}$ of a yard.

In 4563 Pawnes of Geanes, how many yards English?

Answer. Say by the Rule of three, if a hundred Pawnes doe make 26 yards, what will 4563 Pawns make? Multiply and divide, and you shall find 1186 yards $\frac{1}{26}$. So many yards do 4563 Pawns make.

Otherwise, take some other number at your pleasure, as ten pawns, which is the $\frac{1}{10}$ part of 100, then to find his proportion, take the $\frac{1}{26}$ part of 26, which is $2\frac{1}{2}$; and then say also by the Rule of three, if ten Pawns give $2\frac{1}{2}$ yards, what will 4563 Pawns give? Work, and you shall find 1186 $\frac{1}{26}$ yards, as before.

More, at 2 s. 6 d. the Pawns of Geanes, what Will

will the English yard be worth after the rate?

Answer. Say by the Rule of three, if $\frac{3}{4}$ of a yard cost 2 $\frac{1}{2}$ s. what one yard? Multiply and divide, and you shall find 9 s. 7 $\frac{1}{2}$ d.

More, if 346 $\frac{1}{2}$ Pawns cost 30 $\frac{1}{2}$ li. 13 s. 4 d. sterling, what is that the English yard after the rate?

Answer. Say by the Rule of three, if 346 $\frac{1}{2}$ Pawns cost 30 $\frac{1}{2}$ pounds, what are 3 $\frac{1}{2}$ Pawns worth (for 10 many Pawns make a yard) Multiply and divide, and you shall find $\frac{777}{1000}$ parts of a pound, which in known numbers is worth 6 s. 9 d. $\frac{577}{1000}$.

The eleventh Chapter intreateth of Rules of Loan and Interest, with certain necessary questions and proofs incident thereunto, &c.

Sir, I lent my friend 236 pounds for 5 $\frac{1}{2}$ months simply without any Interest, upon condition, to have the like courtesie againe when I need, But when I came to borrow, he could spare me but 149 li. 8 s. 4 d. The question is now how

how long time I ought to have the use thereof, to counterwaile my friendship before time shew'd him?

Answer. Say by the Backer Rule of three, if 326 pounds give 5½ months, what time will 149½ pounds give? Multiply and divide, and you shall finde twelve months, and so long time ought I to use his mony.

The Proofoe.

Item, lent my friend 149 li. 8 s. 4 d. for twelve months. The question is now how much mony he ought to lend me again for 5½ months to recompence my friendship shew'd him.

Answer. Say by the Backer or Reverse Rule of three. If twelve months give 149½, what shall 5½ months give? Work, and you shall find 326 pounds, and so much ought he to lend me to requite my gentlenesse or good turn.

Two other branches, yet more, for proofoe out of the same question.

Item, lent my friend 149 li. 8 s. 4 d. for 12 months, to have the like friendship again when I need. And coming to horror of him, he very courteously took me 326 pounds (for that he could well then spare the same). The question is now, how long I ought to occupy it, not usurping friendship, but in his due time to restore it again.

Answer.

Answer. Say by the Rule of three reverse, if 149 $\frac{1}{2}$ pounds give 12 months, what shall 326 pounds give? Multiply and divide, and you shall finde, that at 5 $\frac{1}{2}$ months terme, I ought to restore it again.

Prooffe.

Item, Lent my friend 326 pounds for 5 $\frac{1}{2}$ months. The question is now, how many pounds he ought to lend me for 12 months to recompence this pleasure again?

Scholar. Work by the Rule of three reverse, as you have done before, and you shall finde 149 li. 8 s. 4 d.

Again, four other selected questions, of Loan and Interest, all out of one branch, and each one also a necessary question, and a particular prooffe to other.

Item, Lent my friend 430 pounds at Interest for three months, to receive after the rate of 8 pounds in the 100 pounds for 12 months. The question is, what the interest cometh to? You may if you please, work it at two workings by the Rule of three direct, in saying, if 12 months

Loan and Interest.

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months give 8 pounds, what giveth three months? Multiply and divide; and it giveth 2 pound.

Then for the second work say: If a hundred pound yeeld 2 pounds, what yeeldeth 430 li? Multiply and divide, and you shall finde 8 li. 12 s. and so much comes the loane of 430 li. to for 3 months after the rate of 8 pounds in the hundred pounds of 12 months.

Otherwise wrought thus by the rule of three at twice also,

If 100 pound give 8 pounds, what giveth 430 pounds? Multiply and divide, and you shall find 34 pounds; Then again for the second work say: If 12 months give 34 pounds; what giveth three months? Work and finde 8 li. 12 s. as before.

Otherwise yet at one working: By the first part of the rule of five numbers forward, in saying, if 100 pounds in 12 months, gain 8 pounds, what shall 430 pounds gain in three months? Multiply the first by the second for your Divisor, and the other three, the one into the other for the Dividend, and you shall find eight pounds 12 shillings, as aforesaid.

Prooffe.

Item, A friend of mine received of me 8. pounds 12 shillings for the Interest and Use of 430 pounds for three months terme: The question is

now, what he took in the 100 pound for 12 months after that rate?

Answer. For most brief, say by the first part or rule of five numbers forward: If 430 pounds in three months did pay 8 li. 12 s. what doth 100 pounds in 12 months take after the rate? Work, and you shall find 8 pounds, and so much he took upon the 100 pounds for 12 months.

**A third Question and proof also by
the Backer Rule of five
Numbers.**

Item, I lent my friend 430 pounds to receive for the interest thereof, after the rate of 8 pounds in the 100 for 12 months. The question is now how long time my friend ought to give the use thereof, that it may be returned with 8 li. 12 s. gains.

You may work it, if you please by the Rule of three direct at twice, in saying: If 100 li. yeeld 8 pounds, what yeeldeth 430 pound? Multiply and divide, and find 34 pound and $\frac{1}{2}$.

Then again for the second work say, if 34 $\frac{1}{2}$ pounds, give twelve months, what giveth 8 $\frac{1}{2}$ pounds? Multiply and divide, and you shall find three months, and so long time ought my friend to use it to return with 8 li. 12 s. gain.

Otherwise at one working by the Backer Rule

Rule of 5 numbers, in saying: if 100 pounds in 12 moneths doe gain 8 pounds; how much time shall 430 pounds be a gaining of 8 pounds 12 s. 7. Multiply the first and the second into the last for your Dividend, and the third and fourth multiply together for your Divisor, and then divide, and you shall find three months, the just time that my friend ought to use it to return it with 8 li. 12 s. gain.

A fourth derived question out of this Branch, which is a proof of this last, and also of the other two going before.

Item, How much money ought a Merchant to deliver after 8 pounds in the 100 for twelve months, that in three months he may gain 8 li. twelve shillings.

Answer. You may also if you please, work it by the Golden Rule of three at twice: first saying, If three months give 8 $\frac{1}{2}$ pound, what 12 months gain? You shall finde 34 $\frac{1}{2}$. Then say again, If 8 pounds be come of 100 pounds, what shall come of 34 li. 8 s. 7. Work, and you shall finde the answer to the question, which is 430 pounds, and so much ought the Merchant to deliver.

But most briefly it is answered by the Backer Rule of 5 numbers, where I argue thus, saying:

If

If 100 li. be 12 months a gaining of 8 li. then but for three months terme onely to take 8 li. 12 s. must needs be a good round summe to work it, set your numbers thus:
 $100 \text{ --- } 12 \text{ --- } 8 \text{ --- } 5 \text{ --- } 8 \frac{1}{2}$ multiply-
 ing the first into the second, and also by 43 the
 product of the fifth, for your dividend, and the
 third and fourth together with 5. the Deno-
 minator of your fraction for your Divisor:
 then divide, and you shall find as before 430
 pounds: the true solution to your question.



The twelfth Chapter intreateth of the
 making of Factors, which is ta-
 ken in two sorts.



He first is, when the estimation of
 the Factor is taken upon the
 sending of the Merchant, as if
 the estimation of his person be
 it is understood that he shall
 have $\frac{1}{2}$ of the gain, the Merchant the other $\frac{1}{2}$.

The other sort is, when the estimation of
 his making is out of the sending of the Mer-
 chant, as if the order and agreement between
 them were such, that the Merchant shall put in
 800 li. and the Factor for his making shall have
 $\frac{1}{2}$: nevertheless he shall have but $\frac{1}{2}$ of the gain

or

or profit, for the $\frac{1}{2}$ of 800 is 400 (for the estimation of his making) which with the 800 pounds in all make 1200 pounds, whereof the 200 pound, is $\frac{1}{3}$

A Merchant doth put in 800 pound into the hands of his Factor, under such condition, that the said Factor shall have the $\frac{1}{3}$. And after certain time they finde in profit 124 li. 6 s. 8 d. I demand how much the Merchant shall have hereof, and how much ought the Factor to have?

Answer. When the estimation of the Factor is out of the sending of the Merchant, it maketh;

| li. | s. | d. | |
|-----|----|----|---------------------|
| 99 | 9 | 4 | } for the Merchant. |
| 14 | 17 | 4 | |
| | | | } for the Factor. |

But if that his estimation be at the sending of the Merchant, then it maketh but

| li. | s. | d. | |
|-----|----|----|---------------------|
| 93 | 5 | 0 | } for the Merchant. |
| 31 | 1 | 8 | |
| | | | } for the Factor. |

For the Merchant is then to have $\frac{1}{2}$, and the Factor $\frac{1}{3}$.

A Merchant doth put into the hands of his Factor 800 pounds, and the Factor 400 li.

M m

to

to have the $\frac{1}{2}$ part of the profit: I demand now for how much his person is esteemed, when the same is counted upon the sending of the Merchant.

Answer, According to the tenour and order before prescribed in the first Rule, that is, if his estimate be $\frac{1}{2}$ he shall have the $\frac{1}{2}$ of the gain. Therefore say by the Rule of three direct: If $\frac{1}{2}$ taken put in 400 pound, what is the estimate, or putting in of $\frac{1}{2}$ taking? Multiply and divide, and you shall finde 320 pounds, and so much is the person of the Factor estimated.

Otherwise,

To finde the estimation of the person of the Factor, you shall consider, that seeing it was agreed between them, that the Factor should take the $\frac{1}{2}$, then the Merchant shall have the residue, which are $\frac{1}{2}$: wherefore the gain of the Merchant unto that of the Factor is in such proportion as 5 unto 4. Then if you will know the estimation of the person of the Factor, say, If 5 give 4, what will 400 give? Multiply and divide, and you shall finde 320 pound. And so much is the person of the Factor esteemed to be worth.

Other conditions then these aforesaid, may also be between Merchants and Factors, without respect either of sending or not sending of the Merchant, where most commonly the estimation

mation of the body of the Factor is in such proportion of the stock which the Merchant layeth in, as the gain of the said Factor is unto the gain of the Merchant. As thus, if a Merchant do deliver into the hands of his Factor 400 pound, and he to have half the profit, the person of the said Factor shall be esteemed to be worth 400 pound; and if the Factor do take but $\frac{1}{4}$ of the gain, he should have but $\frac{1}{4}$ so much of the gain as the Merchant taketh, which must have $\frac{3}{4}$, wherefore the person of the Factor is esteemed but the $\frac{3}{4}$ of that which the Merchant layeth in, that is to say, two hundred pound.

And if the Factor did take the $\frac{1}{3}$ of the gain, then the Merchant shall take the residue which are $\frac{2}{3}$, wherefore the gain of the Merchant unto the Factor is then in such proportion as 3 unto 2; whereupon if you will then know the estimation of the person of the Factor, say, If 3 give 2, what shall 400 give? Work, and you shall finde 266 $\frac{2}{3}$ pounds. And so much is the person of the Factor esteemed to be worth.

And if the Merchant should deliver unto his Factor 400 pound, and the factor would lay in 80, and his person, to the end he might have the $\frac{1}{2}$ of the gain, I demand how much shall his person be esteemed?

Answer, Abate 80 from 400, and there will remain 320. And as so much shall his person be esteemed.

A Merchant hath delivered unto his Factor 900 pounds to govern in the Trade of Merchandize, upon condition that he shall have the $\frac{1}{3}$ of the gain, if any thing be gained, and also to bear the $\frac{1}{3}$ of the losse, if any thing be lost. Now I demand how much his person was esteemed at?

Answer. Seeing that the Factor taketh the $\frac{1}{3}$ of the gain, his person ought to be esteemed as much as $\frac{1}{3}$ of the stock, which the Merchant layeth in: that is to say, the $\frac{1}{3}$ of 900 pound, which is 450. The reason is, because $\frac{1}{3}$ of the gain that the Factor taketh is the $\frac{1}{3}$ of the $\frac{1}{3}$ of the gain that the Merchant taketh, and so the Factor his person is esteemed to be worth 450 pounds.

A Merchant hath delivered unto his Factor 600 li. and the Factor layeth in 250 li. and his person. Now because he layeth in 250 li. and his person, it is agreed between them, that he shall take the $\frac{1}{3}$ of the gain. I demand for how much his person was esteemed?

Answer. For as much as the Factor taketh $\frac{1}{3}$ of the gain, he taketh $\frac{1}{3}$ of that which the Merchant taketh, for $\frac{1}{3}$ are the $\frac{1}{3}$ of $\frac{1}{3}$. And therefore the Factors laying in ought to be 400 li. which is $\frac{2}{3}$ of 600 pound that the Merchant laid in. Then subtract 250, which the Factor did lay in, from 400 pound which should have been his whole stock, and there remaineth 150 pound for the estimation of his person.

More, a Merchant hath delivered unto his Factor 800 pound, upon condition that the
Factor

Factor shall have the gain of 160 li. as though he laid in so much ready money: I demand what portion of the gain the said Factor shall take?

Answer. See what part the 160 (which the Factor laid in) is of 960, which is the whole stock of their company, and you shall finde. And such part of the gain shall the Factor take.

But in case, that in making their Covenants, it were so agreed between them, that the Factor should have the gain of 160 pound of the whole stock which the Merchant layeth in, that is to say, of the 800 pound; then should the Factor take $\frac{1}{5}$ of the gains, for 160 is $\frac{1}{5}$ of 800 pound.

The thirteenth Chapter treateth of Rules of Barter, and exchanging Merchandize, which is distinct into seven Rules, with divers other necessary questions incident thereunto.

The first Rule.

TWO Merchants willing to change their Merchandize the one with the other: The one hath 24 broad clothes at 10 li. 10 s. the piece: The other hath Mace at 12 shillings the pound. The question is, how many pounds of Mace he ought

to give for his Cloth, to save himself harm-
lesse, and be no loser?

Answer. Seek first by the Rule of three what
the 24 Clothes cost at 10 pound 10 shillings the
piece, and you shall finde 252 pound: Then to
finde the quantity of Mace, say again by the
Rule of three, If 12 shillings buy one pound, what
shall 252 pound buy me? Work, and you shall
finde 420 pound of Mace: and so many pound
ought he to give for his Clothes.

The Proove.

Two barter. The one hath 420 pounds of
Mace at 12 s. the pound, to barter or change
broad Clothes, at 10 pounds 10 shillings the
piece. The question is, how many broad
Clothes he ought to give for all his Mace?

Answer. First say, If one cost 12 shillings,
what 420? you shall finde 5040 s. Then say
again, If 10 1/2 pounds give one Cloth, what shall
5040 shillings give? Work, and you shall finde
24 Clothes, your desire.

The second Rule.

Two change merchant for merchant: The
one hath Pepper at two shillings foure
pence the pound, to sell for ready money. But
in barter he will have no lesse then three
shillings the pound. And the other hath Hol-
land

land at five shillings six pence the Ell ready money. The question is now, at what price he ought to deliver the Ell in the barter to save himself harmlesse.

Answer. Say by the Rule of three direct, If $2\frac{1}{2}$ ready money give 3 s. in barter, what shall $5\frac{1}{2}$ give in barter? You shall finde $7\frac{1}{2}$ s. and at this price ought the second Merchant to sell his Holland in barter.

The Proof.

Two barter. The one hath Holland at five s. 6 pence the Ell to sell for ready money. And in barter he will have $7\frac{1}{2}$ s. The other hath Pepper at 2 s. 4 d. the pound, to sell for ready money. The question is now, how he ought to sell in barter?

Answer. Say by the Rule of three direct. If $5\frac{1}{2}$ ready money give $7\frac{1}{2}$ s. in barter, what ought $2\frac{1}{2}$ to take in barter? Multiply and divide, and you shall finde 3 shillings your desire.

The third Rule.

Two barter. The one hath cloth of Arras at 30 s. the Ell ready money, but in barter he will have 33 s. And the other hath white Wines which he delivered in barter for 16 pounds the Tun. The question is now, what his Wines cost the Tun in ready money.

Answer. Say by the Rule of three direct. If 25 s. in barter, give but 20 s. ready money, what did 16 pound in barter cost? Work, and you shall finde 13 li. 10 s. 4 r. And so much cost his Wines for a Tun ready money.

The Proofs.

Two barter Merchandize for Merchandize: The one hath white Wines at 13 li. 10 s. 4 r. the Tun to sell for ready money: But in barter he delivered it for 16 pounds. The other, to make his match good and save himself harmlesse, delivereth Arras at 25 s. the Ell. The question is now, what an Ell of his Arras cost in ready money?

Answer. Say by the Rule of three direct. If 16 pounds in barter give but 23 li. 10 s. 4 r. ready money, what shall 35 s. yeeld in barter? Work, and you shall finde 30 s. your desire.

The fourth Rule.

Two barter: The one hath Kersey at 14 pounds the piece ready money: But in barter he will have 18 pounds: and yet he will have the part of his over-price in ready money. And the other hath Ginger at eight groats the pound to sell for ready money. The question is, how he ought to deliver the Ginger by the pound in barter to save himself harmlesse, and make the barter equall.

Answer.

Answer. *Item*, for the working of this question, and such other the like, you must understand, if the party over-selling his wares, require to have also some portion in ready money, as $\frac{1}{2}$; $\frac{3}{4}$, &c. Then shall you first rebate the same demanded part, whatsoever it be, from the over-price, and also from the just-price. And those two numbers that shall remain after the subtraction is made, shall be the two first numbers in the *Rule of three*. And the just price of the same Merchandize shall be the third number, which by the operation of the *Rule of three direct*, shall yeeld you a true solution, how, and at what price you shall over-sell that your Merchandize, to save your self harmlesse, and make the barter equall.

Example.

Take the $\frac{1}{2}$ (of eighteen) which is the over-price of his Cloth, which $\frac{1}{2}$ of eighteen is six, which you must subtract from 18, there rest 12. And also 14 ——— 18
abate it from 14, which is the 6 ——— 6
just price of the Cloth, and ———
there remaineth 8, which 8 8 ——— 16
and 12 are the two first numbers in the *Rule of three*. Then take eight groats, or 2 $\frac{2}{3}$ shillings for the third number. Then say by the *Rule of three direct*. If eight pounds give 12 pounds, what shall 2 $\frac{2}{3}$ s. give?
Mul-

Multiply and divide, and you shall finde 4 s. And for so much shall the second Merchant sell his Ginger, or his commodity in barter, to ballance the same equall.

The Prooffe.

Two barter; the one hath fine Kerseys at 14 pounds the piece ready money: But in barter he will have 18 pounds: and yet he will have the $\frac{2}{3}$ part of his over-price in ready money. And the other hath Ginger, which he having cunning enough to make the barter equall, delivered in barter for 4 s. the li. The question is now, what his Ginger cost him ready money?

Answer. After you have made the subtraction, abating 6 the $\frac{2}{3}$ part of 18, both from 18 and 14 (as before was taught you:) then will there remain 8 and 12 for your two first numbers in the Rule of three. Then say, If 18 give 8, what shall come of 4 the over-price of the pound of Ginger? Multiply and divide, and you shall finde 2 s. 8 d. your desire.

Two Merchants barter merchandize for merchandize. The one hath Devonshire Wheele at 7 li. 13 s. 4 d. the piece ready money: but in barter he doth them away for 8 li. 3 s. 4 d. and yet he will have the $\frac{2}{3}$ part of his price in ready money. And the other hath Cotons at three pounds the piece ready money. The question is now, at what price he ought to sell or exchange his Cotons in barter

yet he will have the $\frac{1}{2}$ of his over-price in ready money. The other hath flax at 3 d. the pound ready money. The question is now, how he shall sell the pound of his flax in barter?

Answer. See first at 10 pound upon the 100 pounds what the 56 $\frac{1}{2}$ s. commeth to, in saying, (by the Rule of three direct) If 100 pounds give 110 pounds, what 56 $\frac{1}{2}$ s? Multiply and divide, and you shall finde 3 pound 2 shillings 4 pence, of which the $\frac{1}{2}$ that he demandeth in ready money, is 1 pound 12 shillings 2 pence; the same 31 s. 2 d. abated from 40 s. and also from 56 s. 8 d. there will remain 8 s. 10 d. and 25 s. 6 d. for the two first numbers in the Rule of Three, and 3 pence the price of the pound of flax, for the third number. Then multiply and divide, and you shall finde 8 s. 1 d. And for so much shall he sell the pound of flax in barter.

The sixth Rule.

Two are willing to exchange Merchandizes. The one hath Norwich Grograns at 25 s. the piece ready money: and in barter he will have 30 s. and he will have the $\frac{1}{2}$ part of his over-price in ready money. The other hath Norwich Stockings at 40 s. the dozen to sell for ready money. But in as much as the first Merchants Grograns are no better, he would deliver them so to balance the barter that he may gain 10 pounds in the 100 pounds. The question is now, how he shall sell his

his Host: he dozen in barter, according to his re-
quest.

Answer. Say, If 100 give 110 li. what shall
40 s. give, which is the just price of the dozen
of stockings? Multiply and divide, and you
shall finde 44 s. Then take the $\frac{1}{2}$ of 30 s. which
is 15 s. 6 d. and subtract it from 25 s. and also
from 30 s. and there will remain 17 s. 6 d.
and 22 s. 6 d. for the two first numbers in
the Rule of three, and 44 shillings, which is
the just price (with his gain in the dozen of
Stockings) for the third number. Then multi-
ply and divide, and you shall finde 56 s. 6 d.
and for so much he is to sell his dozen of stock-
ings in barter.

The seventh Rule.

Two Merchants will change their Merchan-
dize one with the other: The one hath 720 Ells
of Cambrick at 5 s. the Ell to sell for ready money,
but in barter he requireth 6 s. 8 d. And yet not-
withstanding he loseth by it after 10 pounds upon
the 100 pounds, whereupon he requireth one half
of his overprice in ready money: and the other
Merchant having skill enough to make the barter
equall, delivered English Saffrons at 30 s. the
pound. The question is now, what his Saffrons cost
the pound in ready money.

Answer. You must first seek what is lost
upon the 100 pound, which to doe, you may
say, (if you please) If 100 pound lose 10, what
shall

shall 6 s. lose? Work, and you shall finde 7 s. (or 8 d.) which must be rebated from 6 s. 8 d. so resteth 6 s. still. Or you may say, If 100 pound give me but 90 pounds, what shall 6 s. 8 d. give? Work this way either, and you shall finde also as before directly in your quotient 6 s. your desire. Then are you next to cast up what the 720 Ells of Cambrick cometh to at 6 s. 8 d. the Ell, and you shall finde 240 pounds: the $\frac{1}{2}$ whereof the Cambrick Merchant will have in ready money (which is 120 pounds:). Nextly you must cast what the Cambrick cometh to after his losse in the 100 pound, which as you found, is but 6 s. an Ell, and you shall finde 216 pounds: Now must you subtract his ready money (which is 120 pounds in all) out of 240 pound, and also out of 216 pound, and there will remain 120 pounds, and 96 pounds for your two first numbers in the Rule of three, and 30 shillings is the over-price of your Saffron for the third number: Then multiply and divide, and you shall finde 24 shillings. And so much did his Saffrons cost in ready money.

Two Merchants barter; the one hath 50 clothes to put away for ready money at 11 pounds the cloth, and in barter putteth them away for 22 pounds, taking Holland cloth at 20 d. the Flemish Ell; which was worth no more but 18 d. The question is now, what Holland payeth for the Cloth, and what he winneth or loseth by the bargain?

Answer.

Answer. Fifty Clothes at 11 pounds the Cloth commeth to 550 pounds, and put away at 18 pounds the piece, maketh 600 pound. Then to finde what Holland payeth for the Cloth, say by the Rule of three direct. If 20 d. buy one Ell, what 600 pounds? Work, and you shall finde 7200 Ells. Now to finde the estate of his gain or losse, you must seek what his 7200 Ells commeth to at 18 d. the Ell: Work by the Rule of proportion direct, and you shall finde 540 pounds, which is not so much as his Clothes were worth in ready money by ten pounds: and so much lost the first Merchant by his Exchange.

A Venetian hath in London 100 pieces of silk, to put away for ready money at 3 li. the piece. But in Barter he delivered them for 4 li. the piece, taking Wooll of a Felmonger at 7 li. 10 s. the C. weight, which was worth no more but six pounds the C. ready money. The question is now, what Wooll payeth for the silks, and which of them winneth or loseth by the barter?

Answer. A hundred pieces of Silk at 3 li. is in all 300 li. and at 4 li. is 400 li. Then to find what wooll payeth for the Silk, say by the Rule of three direct: If 7½ buy me 100 weight, what 400 pound? Work, and find 53⅓ C. weight of wooll. Now to finde the estate of their gain, and losse, cast up his Wooll at 6 li. the C. (for so much they were worth ready money) and you shall finde 320 pound, which is 20 pound more then the silks were

to be sold for ready money, whereby the *Portugall* gained 20 pounds by the Barter.

A Merchant hath 43 $\frac{1}{2}$ weight of Wool at 6 pounds the C, to sell for ready money, but in barter he will have 7 pounds 10 s. and another doth barter with him for Silks which are worth three pounds a piece ready money. The question is now, how he ought to deliver his Silks the piece in barter, and how many payeth for the wooll.

Answer. Say by the Rule of proportion, (or by the Rule of three direct) if 6 pounds for C, weight ready money, yeeld me 7 li. 10 s. what will 3 li. yeeld, which is the just price of a piece of Silk in Barter, to make the Truck equal 2 Work, and find 3 li. 15 s. the price of a piece of Silk in Barter: then say, if 3 li. 15 s. acquire one piece of Silk, how many pieces of Silk are bought with 400 pound, which is the value of 53 $\frac{1}{2}$ C. weight of Wool, at 7 li. 10 s. 7 Work by the Rule of three direct, and you shall finde 160 pieces of Silk and $\frac{2}{3}$ of a piece, and so many of Silk pay for the wooll, and neither party hath advantage of other.

Two men Will change Merchandise the one with the other. The one of them hath Beer at 6 s. 8 d. the Barrell, to sell for ready money, but in Barter he will sell the Barrell for 8 s. and yet he will gain moreover after 10 pound upon the 100 pounds. And the other hath White Spanish Wooll at 2 s. the Rove to sell for ready money. The question is now, how he shall deliver the Rove of wooll in Barter to save himself harmlesse.

Answer.

Answer. Say, if $6\frac{1}{2}$ s. which is the just price of the barrell of beer, be sold in barter for 8 shillings: for how much shall 20 shillings (which is the just price of the Rove of Wooll) be sold in barter? Work by the Rule of three direct, and you shall finde 24 s. Then for because the first Merchant will gain after 10 pounds upon the 100 pounds, he maketh his 100 pounds, 110 pounds. And therefore say by the Rule of three, If the second Merchant of 110 pounds do make but 100 pounds, how much shall he make of 24 s? Multiply and divide, and you shall find 21 s. 9 d. $\frac{1}{2}$ of a peny. And for so much shall he sell the Rove of wooll to be delivered in barter, to the end the first Merchant may give 10 in the 100.

Two Merchants will change their Commodities the one with the other. The one of them hath white paper at 4. s. the Ream, to sell for ready mony. And in barter he will doe it away for 5 s. and yet he will gain moreover after the rate of 10 pounds upon the 100 pounds. And the other hath Mace at 14 s. 6 d. the pound weight to sell in barter. Now I demand what the pound did cost in ready mony.

Answer. Say if 5 s. (which is the over price of the Paper in barter) become of 4 s. the just price of how much shall come 14 $\frac{1}{2}$ shillings, which is the surprize of the pound of Mace in barter? Multiply and divide, and you shall find 11 $\frac{1}{2}$ s. Then for because the first Merchant of Paper will gain after 10 upon the 100, Say, if

100 do give 110, what shall 11; shillings give? Work, and you shall finde 12 s. 9 $\frac{1}{4}$ d. and so much did the pound of Mace cost in ready money.

The fourteenth Chapter intreateth of exchanging of money from one place to the other.

EXchange is no other thing, then to take or receive money in one City, to render or pay the value thereof in another City, or else to give money in one place, and receive the value thereof in another, at term of certain dayes, months, or fairs, according to the diversity of the place.

But this practice chiefly consisteth in the knowledge of the money or Coynes in diuers places, of which for thy benefit (after a few examples given to the introduction of this work) I will set down certain notes of the diversity of the common and usuall coynes in most places in Christendom for traffick.

And first I will begin at Antwerp, where they use to make their accounts by Deniers de grosse, that is to say, pence Flemmish, whereof 12 do make 1 s. Flemmish, and 20 s. doe make one pound de grosse.

Item,

Item, a Merchant delivered at Antwerp, 400 pounds Flemmish to receive in London 20 s. sterling, for every 23 s. — 4 d. Flemmish: The question is now, how much sterling money is to be received at London for 400 pounds Flemmish?

Answer. Say by the Rule of three, If 23 $\frac{1}{2}$ Flemmish give 20 s. sterling, what 400 pounds Flemmish? Work, and you shall finde 342 li — 17 s — 1 $\frac{1}{2}$ pence, and so much sterling shall I receive in London for the said 400 pounds Flemmish.

Otherwise also wrought by Rules of practise in taking the $\frac{1}{2}$ of the Flemmish mony delivered, and abating the same from the principall, the rest is English mony, as before.

| | | | | |
|--------|---|----|---|---------------------------|
| 400 li | — | 05 | — | 00 d. |
| 57 | — | 2 | — | 10 $\frac{1}{2}$ |
| <hr/> | | | | |
| 342 | — | 17 | — | 1 $\frac{1}{2}$ sterling. |

A Merchant at London delivered 200 li. sterling for Antwerp, at 23 s — 5 d. Flemmish the pounds sterling: the question is, how much he must receive at Antwerp.

Answer. Say by the Rule of three, if 1 pound sterling give 25 s. 5 d. Flemmish, what 200 li. sterling? Work, and thou shalt find 234 li. — 3 — 4 d. So many pounds Flemmish shall he receive at Antwerp for the said 200 pounds sterling.

Otherwise by practice.

1—13—5—200
 3 s. 4 d. 33—6—8
 1 d. ———16—8
 maketh sterling ———2, 4 li.—3 s.—4 d.

In London 20 pound sterling is delivered by Exchange for Antwerp, at 23 s. 9 d. Flemmish the pound sterling: the question is, at what rate the Flemmish mony ought to be returned to gain 4 pounds upon the 100 pound sterling at London.

Answer. First, say by the Rule of three direct: If 1 pound sterling give 23 $\frac{3}{4}$ Flemmish, what 200 pounds sterling? Multiply and divide, and you shall find 237 pounds 10 shillings. The which to return to gain 8 pounds sterling in London, say by the backer Rule, If 200 pounds sterling require the exchange 23 s. 9 d. Flemmish, what the exchange to make 208 li. sterling? Work by the Rule, and finde 22 s. 10 $\frac{1}{2}$ d. Flemmish, the effect in the question required.

If I take up mony at Antwerp after 19 s. 4 d. Flemmish, to pay for the same at London, 20 shillings sterling, and When the day of payment is come, I am forced to return the same mony again in London, to pay my Bill of Exchange: so that for 20 shillings which I take up here at London, I must pay 19 s. 6 d. at Antwerp, I demand whether

ther I do win or lose, and how much in or upon the 100 pounds of money?

Answer. Say by the Rule of three: If 19 $\frac{1}{2}$ give 19 $\frac{1}{2}$ what will 140 pounds give? Multiply and divide, and you shall find 99 li, 2 $\frac{1}{2}$ s. which being abated from 100 pounds, there will remain 17 shillings $\frac{1}{2}$, and so much I do lose upon the 100 pounds of money.

If I take up at London 20 shillings sterling to pay at Antwerp 22 s. 4 d. and when the day of payment is come, my Factor is constrained to take up money again at Antwerp, wherewith to pay the aforesaid sum, and there he doth receive 23 s. 4 d. Flemmish, for the which I must pay 20 s. at London: The question is now, whether I doe win or lose, and how much upon the 100 li. of money after that rate.

Answer. Say by the Rule of Proportion, If 22 $\frac{1}{2}$ s. give 23 $\frac{1}{2}$ s. what will 100 pounds give? Multiply and divide, and you shall find 104 pounds 9 shillings $\frac{2}{7}$, from the which abate 100 pounds, and there will remain 4 pounds 9 shillings $\frac{2}{7}$, and so much is there gained upon the 100 pounds of money.

In Antwerp is delivered 200 pounds Flemmish by exchange for London, at 20 shillings sterling for every 23 shilling 4 d. Flemmish. The question is, at what rate the same is to be returned to gain 10 pounds upon the 100 pounds Flemmish in Antwerp.

Answer. First, say by the Rule of three, if 23 $\frac{1}{2}$ Flemmish give 20 s, what shall 200 pounds gain? Work, and you shall finde 171 pounds 8 s. 6 $\frac{1}{2}$ d. Then say again by the Rule of three direct, if 171 pounds 8 s. 6 $\frac{1}{2}$ s. sterling, give me 210 pounds Flemmish, what shall 20 s. sterling give? Work, and you shall find 24 s. 6 d. Flemmish. And at the same rate ought the same to be returned at *Antwerp*, to gain 10 pounds upon the 100 Flemmish.

A Merchant of Antwerp delivereth 234 pound 3 s. 4 d. Flemmish, to receive at London 200 pounds sterling: The question is now, how the exchange goeth after this rate?

Answer. Say by the Rule of three direct, if 200 give 20, what 234 $\frac{1}{2}$? Multiply and divide, and you shall find 23 s. — 5 d. And for so much goeth the exchange.

Item, the exchange from London into France, is not like as it is in Flanders, but it is delivered by the French Crown, which is worth 50 Soulx Turnois the piece.

Whereupon also you must note, that in France they make their accounts by Franks, Soulx, and Deniers Turnois, whereof 12 Deniers make one Soulx Turnois, and 20 Soulx maketh one pound Turnois, which they call a Liure or Frank. But the Merchants, to make their accounts, doe use French Crowns, which is current among them for 51 Soulx Turnois. But by exchange it is otherwise, for it is delivered but for 50 Soulx Turnois the Crown, or as the taker

up of the mony can agree with the deliverer. And note that this Δ Character representeth the Crown by exchange, and is ever 50 Soulx Turnois or French mony.

A Merchant delivereth at London 240 pounds sterling, after 5 shillings six pence the Crown, to receive at Paris 50 Soulx Turnois for every Crown. I demand how much Turnois or French mony payeth the Bills for the said 240 pounds sterling.

Answer. Say by the Rule of three, If $5\frac{1}{2}$ s. sterling give me 50 s. Turnois, what shall 240 pounds sterling give? Reduce the pounds into shillings, then multiply and divide, and you shall find 2181 Liures, 16 Soulx, 4 Deniers, and $\frac{1}{11}$ Turnois: and so much payeth the Bills at Paris, for the 240 pound sterling.

A Merchant delivereth at Roan, or elsewhere in France, 1430 pounds or Franks, the which Frank or pound is 20 Soulx, or a pound Turnois, to receive in London 6 s. 4 d. sterling for every Δ of 50 Soulx Turnois. The question is, how much sterling mony I ought to receive at London for my 1430 pound Turnois.

Answer. Say, if $2\frac{1}{2}$ pounds give me $6\frac{1}{2}$ s. what will 1430 give me? Work, and you shall find 3622 $\frac{1}{2}$ shillings sterling, which maketh 181 pounds 2 s. 8 d. and so much mony is to be received at London, for the said 1430 Liure Turnois, after 6 s. 4 d. for every Δ of 50 Soulx.

In London is delivered 200 pound sterling by exchange for Paris, at 5 s. 9 d. the Δ of 50 Soulx

Turnois. The question is, at what price the said Δ is to be returned to gain 6 pounds upon the 100 pounds sterling at London.

Answer. First, say (by the Rule of three direct) if $5 \frac{1}{4}$ s. sterling give 50 Soulx Turnois; what shall 200 pound sterling give? Work, and you shall find 1739 Franks or Liures, $2 \frac{1}{4}$ Soulx. Then the which to return and gain 6 pounds upon the hundred pounds in London, say by the Rule of three direct, if 1739 Franks $2 \frac{1}{4}$ Soulx yeeld 212 pound, what the Δ of 50 Soulx? work and find 6 s. $1 \frac{1}{2}$ d. the effect required in the question.

A Merchant delivered in London 160 pounds sterling, to receive in Biskay for every 5 s. 6 d. one Ducat of 374 Marvides. The question is, how many Marvides ought I to receive at Biskay?

Answer. Say, if $5 \frac{1}{2}$ s. sterling give 374 Marvides: what shall 160 pounds sterling give? Multiply and divide, and you shall find 217600 Marvides, and so many I ought to receive at Biskay for my 160 pounds sterling.

A Merchant delivered in Baion 4000 Marvides, to receive in London 5 s. 8 d. sterling for every Ducat of 374 Marvides. The question is now, how much sterling money payeth the Bills of Exchange for the said 4000 Marvides?

Answer. Say, if 374 Marvides make one Ducat, what 4000 Marvides? Multiply and divide, and find 106 $\frac{1}{4}$.

Then say again, if 1 Ducat give $5 \frac{3}{4}$ s. what gi-
verth 106 $\frac{1}{4}$ Ducats? Work, and find 30 l. 6 s. $\frac{1}{4}$

Other-

Otherwise it is wrought more brief at one working, as in the last question before, in considering that 5 s. 8 d. containeth one Ducat, or 374 Marvides. Therefore say by the Rule of 3, if 374 Marvides give 5 s. what 4000 Marvides? Work, and you shall also finde in your quotient 30 $\frac{1}{4}$ s. And so many pounds sterling is to be received for the 4000 Marvides.

In London 200 pounds delivered by exchange for Vigo, 374 Marvides the Ducat of 5 s. 10 d. sterling, maketh 256457 $\frac{1}{4}$ Marvides: the which to return and gain 10 li. upon the 100 pounds in London, say by the Rule of three direct, if 220 li. require 256457 $\frac{1}{4}$ Marvides, what 5 s. 10 d? Work, and find 340 Marvides, the price of every Ducat in return, which is the effect in the question required.

These may seem sufficient for instructions.

Notwithstanding for thy further aid and benefit, hereafter follow six speciall and most brief Rules of practice, for English, French, and Flemmish money.

- | | | |
|---|----------|--|
| 1 | teacheth | How to turn Flem. to English sterling. |
| 2 | | How to turn English sterling to Flem. |
| 3 | | How to turn Flemmish to French. |
| 4 | | How to turn French into Flemmish. |
| 5 | | How to turn sterling into French. |
| 6 | | How to turn French into sterling. |

The

The fifteenth Chapter intreateth of the said six Rules of brevity, and of valuation of *English*, *Flemmish*, and *French* mony, and how each of them may easily be brought to others value.

How briefly to reduce pounds, shillings, and pence Flemmish into pounds, shillings, and pence English sterling.

Rule 1.



It is to be noted, that 7 pounds *Flemmish* maketh but 6 pounds sterling: 7 s. *Flemmish* maketh 6 s. sterling, and 7 d. *Flemmish* 6 d. sterling: so that 7 yeeldeth but 6. Wherein is evident that then is lost $\frac{1}{7}$, (if it may be so called) when it is reduced into *English* mony: wherefore to know how much 233 l.—13 s.—4 d. *Flemmish* maketh *English*, you must subtract from $17\frac{1}{7}$, beginning with the pounds, &c. and that which resteth after this subtraction, is the sum required: so that 233 li.—13 s.—4 d. *Flemmish*, maketh 200 li. 5 s. 8 $\frac{1}{2}$ d. sterling.

Ex-

Example.

li. s. d.

233—13—4

233—7—7 $\frac{1}{2}$

200 5 8 $\frac{1}{2}$ ster.

Another Example.

li. s. d.

311—0—0

344—8—6 $\frac{1}{2}$

266 11 5 $\frac{1}{2}$

To reduce pounds, shillings, and pence sterling, into pounds, shillings, and pence Flemish.

Note that a pound sterling maketh 1 li. 3 s. 4 d. *Flemish*: that is, 1 $\frac{1}{4}$ li. 1 s. sterling maketh 1 $\frac{1}{2}$ s. *Flemish*, and 1 d. sterling maketh 1 $\frac{1}{2}$ d. *Flemish*. So that there is gained (if it may be so called) $\frac{1}{4}$ of the summe being thus reduced to *Flemish*, for of $\frac{1}{4}$ is made $\frac{1}{2}$ which is one whole and $\frac{1}{2}$. Then to know how much 237 li. 7 s. 6 d. sterling maketh *Flemish*, subtract from your sterling, the $\frac{1}{4}$ of the whole summe, and adde it to the same summe, and it maketh 276 li. 18 s. 4 d. which is the summe required.

Example.

li. s. d.

237—7—6 ster.

 $\frac{1}{4}$ 39—11—3

276—18—9 Flem.

Another Example.

li. | s. d.

337

 $\frac{1}{4}$ 56—3—4

393—3—4

To

Rule 3.

To reduce pounds, shillings, and pence Flemmish, into pounds, shillings, and pence French.

Ye shall note, that the equality of Flemmish and French money is this, that is to say, the pound Flemmish, maketh 7 pound $\frac{1}{2}$ French, or Turnois. 1 s. Flemmish maketh 7 $\frac{1}{2}$ s. French, and a groat Flemmish, maketh 7 $\frac{1}{2}$ d. French.

Wherefore to know how much 143 li. 4 s. 9 d. Flemmish maketh French, ye must multiply the whole number twice by 6; beginning at pence, and so forward, and the product of your second multiplication divide by 5, so the work is finished. Or multiply the said summe by 7, and take out of it $\frac{1}{2}$, adding it to the product of your multiplication by 7, and that is your number required. So that as well by the one as by the other, 143 li. 4 s. 9 d. Flemmish, maketh 103 1 li. 6 s. 2 $\frac{1}{2}$ d. French or Turnois.

Example.

The same otherwise.

| li. | s. | d. | | li. | s. | d. |
|--------------------|----|-----------------|-------|------|----|------------------|
| 143 | 4 | 9 | Flem. | 134 | 4 | 9 |
| | | 6 | | | | 7 |
| 859 | 8 | 6 | | 1002 | 13 | 3 |
| | | 6 | | 28 | 12 | 11 $\frac{2}{3}$ |
| 5156 | 11 | 0 | Fren. | 1031 | 6 | 2 $\frac{2}{3}$ |
| $\frac{1}{2}$ 1031 | 6 | 2 $\frac{2}{3}$ | Fren. | | | |

Ano

Another Example.

Or thus :

143 l. Flem.

143

6

7

858

1001

6

$\frac{1}{2}$ 18—12

$\frac{1}{2}$ 5148

French:

1029 li—12

1029 li, $\frac{1}{2}$ or 12 s. French.

To reduce pounds, shillings, and pence, Rule 4.
French, into pounds, shillings, and pence,
Flemmish.

Multiply 233 li—8 s—4 d. French by 5,
and divide the Product twice by 6, that is, the
said number by 6, and the product or quotient
again by 6, and the quotient of this second
Division is the thing required. So that 233 li—
8 s.—4 d. French, maketh 32 li—8 s.—4 $\frac{1}{2}$ d. Flem-
mish.

Example.

Another Example,

li. s. d.

li. s. d.

233—8—4 Fren.

758 French.

5

5

1167—1—8

3765—

$\frac{1}{2}$ 194—10—3 $\frac{1}{2}$

$\frac{1}{2}$ 627—10—

$\frac{1}{2}$ 32—8—4 $\frac{1}{2}$ Flem,

$\frac{1}{2}$ 104—11—8 Flem.

Rule 5.

To reduce pounds, shillings, and pence, sterling, into pounds, shillings, and pence, French, or Turnois.

828

The pound sterling maketh 8 li. 8 s. French, that is to say, 8 $\frac{2}{3}$ pounds: the shillings, maketh 8 $\frac{2}{3}$ shillings, and the peny 8 $\frac{2}{3}$ d. French. Wherefore to know what 231 li. 13 s. 4 d. sterling maketh French, ye must multiply your whole summe by 42, that is, by 7, and the product of it by 6, and divide this second product by 5, and that is the summe required.

Otherwise, multiply the summe sterling by 8, and adde twice to the product $\frac{1}{3}$, and it shall produce the sum required. So that both wayes 231 li. 13 s. 4 d. sterling, maketh 1946 pound French, as here under followeth.

Example. The same otherwise.

Sterling.

| li. | s. | d. | Ster. | li. | s. | d. |
|-------|----|----|-------|-------|----|----|
| 231 | 13 | 4 | | 231 | 13 | 4 |
| | | 6 | | | | 8 |
| <hr/> | | | | <hr/> | | |
| 1390 | 0 | 0 | | 1853 | 6 | 8 |
| | | 7 | | 46 | 6 | 8 |
| | | | | 46 | 6 | 8 |
| <hr/> | | | | <hr/> | | |
| 9730 | 0 | 0 | | | | |
| <hr/> | | | | <hr/> | | |
| | | | | 1946 | 0 | 0 |

French.

$\frac{2}{3}$ 1946 — 0 — 0 Fren.

Ano-

Another example.

The same.

Sterling.

753

Ster.

753

6

8

4518

6024

7

$\frac{1}{2}$

150—12

31626

$\frac{1}{4}$

150—12

$\frac{1}{4}$ 6325 ——— 4 Fren.

6325 ——— 4 French!

To reduce pounds, shillings, and pence, French, into pounds, shillings, and pence, sterling.

To know how much 1256 li. 12 s. 6 d. French maketh in sterling money: multiply the sum by 5, and divide the product by 7 and 6 at twice, and the last quotient shall be the thing required, that is to say, 1256 li. 12 s. 6 d. maketh 149 pounds, 11 s. 11 $\frac{1}{2}$ d. sterling.

Example.

Another example.

li.

s.

d.

French.

li.

s.

d.

1256—12—6

2531 0 0 French.

5

5

6283—2—6

12655

$\frac{1}{2}$ 1047—3—9

$\frac{1}{2}$ 2109—3—4

$\frac{1}{2}$ 149—11—11 $\frac{1}{2}$ Ster.

$\frac{1}{2}$ 301—6—2 $\frac{1}{2}$ Ster.

Note,

Note, that when any money is given by exchange at *London* for *Roan* at $71 \frac{1}{2} d.$ or rather $71 \frac{1}{4} d.$ for the Crown of 50 s. French, there is neither gain nor losse: for it is one money for another, accounting 8 li. 8 s. French, for one pound sterling. So the giver loseth the time of payment, which is about 15 days, and he that taketh it, hath the gain of the same.

They of *Roan*, that put forth or take money by exchange for *London*, ought to have like consideration.

Item, when any man giveth at *London* 64 pence $\frac{1}{4}$, or rather $64 \frac{1}{2} d.$ to have at one of the Fairs of *Lions* a Crown *de Marc*, he that so giveth the money, loseth the time, and he that taketh it, gaineth the same: for 62 pence $\frac{1}{4}$ is equall in value to 45 s. French. He that putteth or taketh money at *Lions* for *London*, ought to consider the same.

Item, when any deliver in *Antwerp* 75 pence, to receive at *Lions* a Crown *de Marc*, he that putteth it forth, loseth the time, and he that taketh it gaineth the same. For 75 groats Flemish, is equall in value to 45 s. French.

Thus for this time I make an end of the practice of Exchange, and the instructions thereunto belonging, and according to my promise: yet further to gratify such as are desirous to know the common Coyns used for traffick among Merchants in these Cities following, a brief declaration of their Monies, and the reckonings, and account of them.

The firste Chapter containeth a declaration of the valuation and diversity of Coyns of most places of Christendome for Traffick; And the manner of Exchange in those places from one City or Town to another: which known, is right necessary for Merchants, by means whereof they do finde the gain or losse upon the Exchange.



Item, for as much as the greatest diversity of mony of Exchange is at *Lions*; therefore I will begin duly of the money of that place.

At *Lions* they use Franks, Soulx, and Deniers Turnois. A Frank maketh 20 Soulx, and one Soulx 12 Deniers; but the Merchants to keep their Books of Accounts, do use French crowns of the Mark at 45 Soulx the piece, and do divide it into 20 Soulx, one Soulx is 12 Deniers.

Item, a Mark of Gold maketh 65 Δ of the Mark, which serveth for exchange, and divide it into 8 ounces, the ounce into 24 pence or deniers, the denier into 24 grains, and so the summe of whole by imagination or guesse.

Δ This mark standeth for a Crown.

Also at *Lions* there are four Fairs in a year, at the which they do commonly Exchange, which are from 3 moneths to 3 moneths.

At *Genoa* they use the Soulx; one Ducat maketh 3 pound.

At *Naples* they use Ducats, Taries, and Grains; the Ducat maketh five Taries, and one Tary 20 Grains; but they take 6 Ducats which maketh 30 Taries for the ounce.

A Ducat maketh ten Carlins; and a Carlin ten grains, so that 2 carlins make a tary, and 100 grains make a ducat.

At *Rome* they use the Ducats of the Chamber: one Ducat is worth 18 Guillis, and one Guillis ten Souls.

At *Venice* they use Ducats current at 124 Souls a piece, or 24 Deniers, and one tary maketh 32 Picolis.

At *Palermo* and *Messina* they use the ounce, tary, and grains, and one ounce is worth 6 ducats of 30 taries, and 1 tary is 20 grains, and 1 grain 6 picolis, 1 ducat is also worth 24 carlins.

At *Millan* they use li. s. d. of Ducat Imperial, and a of exchange is worth 4 li.

At *Lucques*, *Florance*, and *Ancone*, they use the Δ of Gold: in Gold the French Crown is worth 7 li, but at *Belaigue* 3 li. 10 s.

At *Barcelone* they use the Soulx; the Ducat of Exchange is worth 23 Souls.

At *Valence* and *Saragosse* they use the Liver, Soulx, and Denier: the French Crown of exchange is worth 20 Souls, and one Soulx is 12 Deniers.

At the Fairs of *Castile* they use the Mar-
veides,

veides, the Ducat is worth 75 Maroides.

At *Bidon* they use the *Rayer*, one Ducat of Exchange is worth 400 *Rayer*.

At *Nuremberg*, *Frankford*, and *August* in *Germany*, they use the *Krumpen*, whereof 60 make a *Florand*.

At *Antwerp* they use li. s. d. de *Gron*, and they exchange into the *Denier de Gron*, which is our English penny.

At *London* they use the *li. s. d.* and *d.* sterling, and they exchange in pence sterling.

The Exchange of Lions at sundry places.

At *Lyon* there is exchange in churches, at the Cities and Towns following.

First, they deliver at *Lyon* one Mark to have or receive at *Avignon* almost 41 *Ducats*, at *Venice* 70 *ducats* current, at *Rome* 63 *ducats* of the Chamber, at *Genoa* and *Flower* 65 *sc* of Gold, at *Alger* 82 *sc*.

And contrariwise, at the said Cities, they said they do give so much of money to have a Mark at *Lyon*.

Secondly, they give at *Trieste* one *sc* of Mark of 41 *Souls*, *Turn* is a piece to have at *Genoa* almost 68 *Souls*, at *Palermo* and *Messina* almost 34 *Carlins*, at *Barcelona* 22 *Souls*, at *Naples* 20 *Souls*, at the *Faire* at *Cassida* 350 *Maroides*, at *Lisbon* 360 *Rayer*, in *Armerpe* 57 *Deniers de Gros*, and at *London* 70 *d.* sterling.

And contrarywise, they give in the said City
the most part of their money to have a
French Crown of the Mark of Lyons. Exchange
of thirty they do give at Lyons a sou of the Sun,
to have almost 33 French Crowns at Antwerp,
Augsburg, Noremberge, or other Cities in
Germany. Also at Lyons only they do pay they change
the $\frac{1}{2}$ in Gold, and $\frac{1}{2}$ in mony, or else all in mo-
ny, in giving $\frac{1}{2}$ for the hundred. At London
they exchange in French Crowns and they change

Changes at Naples and other Towns.

Item, at Naples they give or deliver almost
100 Ducats to receive at Rome 100 Ducats of
the Chamber of the old Duke. Through
Florence and Milan, they deliver
100 Ducats to receive there almost 80
of Gold. Through Padua and Messine, one Ducat of
5 Tary, to receive there almost 104 grains. Through
Milan, one Ducat to receive there
almost 90 Souls.

Through Genoa, one Ducat to receive there
almost 69 Souls. The whole summe to be paid
within ten days after the sight of the Bill of
Exchange.

Also at Naples, they deliver one Ducat to re-
ceive in Antwerp almost 67 or Deniers at
Graz, within two moneths. At London almost
60 s. sterling in three moneths. At Bursfelde
almost 20 Souls within two moneths.

At

At

At

At *Valence*, almost 18 Souls within two Months. At *Liabane* 333 Rayes within three Months. At *Sancti Spiritus* 2364 Souls within 300 Murvies, at the same Time.

Change of Venice to other places.

All Swiss then deliver 100 boxes worth
to receive in 4 days almost 19 Florent at 60
Kreuzer the piece. The M. Bernardi de W.

At Jacques and Florence almost 108 of Gold in ten days.

- **L**awyer at **P**aris they deliver a Ducal cur-
 ranee to receive at **P**aris and **M**essins almost
 in **C**adix: **C**adix almost **S**ouls at
Cadix almost **S**ouls the whole he ren-
 dices and his weight

Of the Paicor Pari

As touching the Exchange, it is necessary to understand or know the *Pair*, which the *Italians* call *Pari*, which is no other thing then to make the money of the change of one City or Town, to or with the money of another; by means whereof they do finde the gains or loss upon the Exchange.

Example.

having received Letters of credit of one of Amoy that the of the Sun is their worth Souls. The question is, what the fact is worth at London when the Pair of Exchange is for 33 Shillings?

Q. Answered by J. G. Smith, Esq., of London.

Sold by the *Troy* weight: and so is gold, silver, pearl, precious stones, and Jewels. The least quantity of this *Troy* weight is a grain: 24 of these grains make a penny-weight, twenty penny weights an ounce, and 12 ounces a pound, two pounds or pints of this weight maketh a quart. And so ascending into bigger quantities, is produced the Measures whereby are sold our other naturall sustenance: *viz.* Ale or Beere, with all other necessary commodities, as Butter, Hony, Herings, ~~Fishes~~, Sope, &c. All which last before rehearsed, though their Measures (wherein they are contained) be framed and derived from the *Troy* weight, yet are they in traffique with divers Commodities, as Lead, Tinne, Flax, Wax, with all other commodities, both of this Realm, and of other foreign Countries whatsoever, bought and sold by the *Flower de poyse* weight after sixteen ounces to the pound, and 12 pound to the C. weight. And to every C. is allowed but 12 pound weight at the Common-beam. From hence is also derived the weight of *Suffolk* Cheese, which containeth 32 Cloves, 8 pound to a Clove, and weigheth in all 256 pounds. And also the Barrell of *Suffolk* Butter is, or should be of like weight with the weight of Cheese, *viz.* 256 pounds. More 14 of these pounds make a Stone, and 26 Stone containeth a Sack of *English* Wooll: *Forraine* Woods, to wit, *French*, *Spanish*, and *Estrich* is also sold by the pound, or C. weight, but most

See further
of these
Weights
and Mea-
sures in
Reduction,
beginning,
pag. 133.

commonly by the Royle 35 pound to a Royle: other commodities of Tale, are bought and sold by the C. fivescore to the C. Except headed ware, to wit, Cartell Nail, and Fish, which are sold after sixscore to the C. There are also two other sorts of Measures, to wit, the Ell and the Yard. By the Ell is usually met, Linnen cloth, as Canvas, &c. And by the yard, Silks, woollen clothes, &c.

Antwerp are also two sorts of weights, their gold and silver weight, and their common weight. Gold and silver is weighed by the *Mark*, the *Mark* is 8 ounces, the ounce 20 Esterlings, and the Esterling 23, as our grains. The Goldsmiths divide that into smaller, but not the Merchants. The proof of Gold is made by Karets, whereof 24 maketh a Mark of fine Gold, the Karet is 24 grains: the proof of the money is made by Deniers: 12 Deniers is one fine, that is, a *Mark* of fine silver: the Denier also is divided into 24 grains, and the grain into four quarters.

Item, 100 *Marks* in *Antwerp*. Troy weight maketh at *Lions* 103 *Marks*, 2 ounces, and 20 grains, 23 p. At *Norremberg* 103 *Marks*, 1 ounce, 2 Quints, 3 Deniers: at *Frankford* 105 *Marks*: at *Ausburg* 104 *Marks*, 2 ounces, 1 Quint: at *Venice* 103 *Marks*, 1 ounce, 7 Deniers, 18 grains: at *London* 66 pounds.

The

The Mark of gold or silver at Antwerp, Troy weight, which is 8 ounces, maketh $7\frac{1}{2}$ ounces common weight, with which all other Merchandize is weighed. So that the Troy weight is greater then the common weight by $6\frac{1}{2}$ in the C. By this weight of Troy, they also weigh Musk, Amber, Pearle, &c.

All silks are brought at Antwerp by the Burges Ell, which is greater then the common measure, by which they retails by two in the hundred. Their common Ell is $\frac{1}{4}$ of our yard, and $\frac{1}{2}$ of our Ell.

Lions.

At Lions is used 3 sorts of weight, whereof the first is the common Town weight, with which they weigh all kinde of Spicery, and divers other Merchandize. The second is called Geneva weight, which is 8 in the C. greater then the common weight, with which they weigh Silks, &c. The third is French weight, called commonly the Mark weight, and 100 pounds thereof maketh 106 lb. Geneva, and $114\frac{1}{2}$ of their common weight: with which French weight, is weighed all things that paid custome or toll.

At Lions is also used two sorts of Ells or Aulnes. The one wherewith they measure grosse clothes, as canvasse, and such like. The other is called the French Ell or Aulne, with which they measure all other kinde of Merchandize, whereof seven common Town Ells maketh 11 ordinary French Ells.

Roan

Roan.

At *Roan*, 6 $\frac{1}{2}$ Muides of Salt, being the measure of the place, make a C. at *Armoinden* in *Zeland*, and the C. of *Bronage* measure of *Armoinden*, maketh at *Roan* 11 Muides, 30 Muides make a last of Corn, and 16 a last of Oats, 100 pound weight there, maketh at *London* 114 $\frac{1}{2}$, and 190 $\frac{1}{2}$ at *Antwerp*. And 200 Ells make at *London*, 115 $\frac{1}{2}$.

Noremburge.

A 100 pound weight at *Noremburge* maketh at *London* 111 $\frac{1}{2}$; at *Antwerpe* 107 $\frac{1}{2}$, and 100 Ells at *Noremburge* make at *London* 75 $\frac{1}{2}$, at *Antwerp* 95 $\frac{1}{2}$ &c.

Lisbone.

The C. weight at *Lisbone* maketh 4 Roves, every Rove 32 pounds, so that their C. weight is 128 pounds, and their pound containeth 14 ounces, and 100 pounds of their weight maketh at *London* 113 $\frac{1}{2}$.

Their Silk, Cloth of gold, and Woollen is measured with a measure which they call a cuble, containing about $\frac{1}{4}$ of a Varre of *Castile*. Howbeit their common Measure is called a Varre, which maketh five Palms, and containeth $\frac{1}{4}$ of a Varre of *Castile*, our Ell of *London* is equall with the Varre of *Lisbone*.

All

All kinde of Merchandize brought from *Flanders, Roan, or Brabant*, payeth at *Lisbone*, as a duty or custome to the King, 20 in the C. which they call the renth in Merchandize, and the other renth in money.

Note also, that all kinde of Merchandize comming to *Lisbone* by land, payeth lesse in custome then that that commeth by water.

Civill.

The Rove of *Civill* is 30 pound, 4 Roves make their C. weight, which is 120 pounds. The 100 pounds of *Civill* maketh at *London* 102 pounds. Their other common measure is a *Varr*, whereof 100 maketh at *London* 74 Ells, and at *Rome* 40 Canes, &c.

Venice.

At *Venice* be two sorts of weight, the one called *la Grosse*, the other *la Suttle*; with the grosse is weighed all kinde of great wares, and with the small all kinde of spicery, and such like. 98 pounds of grosse weight there, maketh at *London* 100 pound, and 100 pounds of spicery there, without any tare or allowance, make at *London* 94, and with tare 65.

Their own common Measure are Braces, whereof 100 make at *London* 55 Ells, at *Antwerp* 93, &c.

All kinds of Merchandise brought from
Flouence, *Rome*, or *any other place*, as
 At *Flouence* the 100 li. weight maketh at
Aquila, for Saffron 110, and 145 pounds of
Flouence, make at *Rome* but 100 pounds, the
 weight of *Flouence*, and that of *Lube* is all
 one.

Their other measures are Braces, whereof
 100 maketh at *Antwerp*, *Burges* measure, 81 $\frac{1}{2}$
 Els, 100 Braces there, make at *London* 49 Els,
 &c.

The *Lucque* Sattens commonly sold at *Lions*
 by weight, and 133 $\frac{1}{2}$ pounds maketh at *Lions*
 100 pound, so that 1 pound $\frac{1}{2}$ maketh at *Lions*
 but one pound.

Their other measures are Braces, whereof
 100 of them make at *London* 50 Els; at *Ant-*
werp 83 $\frac{1}{2}$ Els, &c.

Aquila
 At *Aquila* their 100 pounds maketh at *Lon-*
don 71 $\frac{1}{2}$ their 136 $\frac{1}{2}$ pounds of Saffron maketh
 at *Geneva* but 100, and 11 li. of *Geneva* ma-
 keth 15 li. at *Aquila*.

Valencia
 At *Valencia* be two sorts of weights, a great
 and a small, The C. weight or great weight
 con-

Weights and Measures.

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containeth four Rovers, the Rove is sold to the
 great weight is 144 lb and the C. weight
 small weight is but 100 pounds, and is also
 parted into four Rovers, which is 30 pounds
 to a Rove. By the small is sold the dearest
 grain, with all other kind of Spices, and by
 the great is sold wheat, with all such like grosse
 wares. The 12 pounds of Silk at *Antwerp*
 maketh 100 lb at one pound *Gravet* weight.
 The change of great Merchandise at *Antwerp*
 containeth 432 pound, and in small *Antwerp*
 pounds.

The weight here used at *Antwerp* is all one.
 Their 100 pound weight maketh at *London*
 78 pound, as is shewed in the Table of the
 divers Countries, the one with the other
 being reduced to an *English* as followeth.

At *Danish* or *Swedish* the rule is, that
 whosoever buyeth any Merchandise there
 buyeth it by the ship pound, which is 320 li-
 20 Lifpounds make a ship pound, and the Lif-
 pound containeth 16 pound, which ship pound
 of *Danish* maketh at *Antwerp* 266 2/3 lb. Their
 108 lb. weight maketh at *London* 86, &c.

Their other common measures are Ells,
 whereof 108 maketh at *London* 72 1/2, and at
Antwerp 82 1/2 Ells.

At *Toulouse* 6 Cabes of Wood maketh a
 Charge, two Cisterns of Corn-measure, and all
 kind

kinde of grain maketh a Charge, the Giltens
weigheth 100 lb weight of that place. Their 100
in weight maketh at London but 91 1/2 pound

At Genoa or Graue, 100 lb of their weight
maketh at London 71 lb and at Antwerp 68 1/2
190 lb weight at Genoa maketh at Antwerp 100
wt. Surle 196 lb of 100 lb of Antwerp

Their other common Measures are Palmes
whereof 190 make at London 20 Ells, and at
Antwerp 24 Ells

The rest are supplied in two Tables, which
hereof the followeth, whereby the ingenious may
gather his desire

The Table of the agreement of the Weights
of divers Countries, the one with the other,
being reduced to an equality, as followeth.

| 100 pounds weight at London, make at | 100 pounds weight at | 100 pounds weight at | 100 pounds weight at |
|--------------------------------------|----------------------|----------------------|----------------------|
| Antwerp 100 | 100 | Venice 100 | 100 |
| Frankford 100 | 100 | Weight | 100 |
| Cole 100 | 100 | 100 | 100 |
| 1400 lb | 100 | 100 | 100 |
| Nuremberg 100 | 100 | 100 | 100 |
| Rome 100 | 100 | 100 | 100 |
| Paris 100 | 100 | 100 | 100 |
| Lions 100 | 100 | 100 | 100 |
| Deer 100 | 100 | 100 | 100 |
| Geneva 100 | 100 | 100 | 100 |
| Toulonse 100 | 100 | 100 | 100 |
| Rochell 100 | 100 | 100 | 100 |
| Marseilles 100 | 100 | 100 | 100 |
| Sigill 100 | 100 | 100 | 100 |

The

The other Table of agreement of Measures of diverse Countries reduced unto an equality; by the aid whereof you may with the use of the *Rule of three*, convert either more or lesse of any one Measure unto the other.

by number.

| | |
|-----|-------------------|
| 100 | Antwerp |
| 101 | Nuremberg |
| 102 | Frankford |
| 103 | Lipsig |
| 104 | Prissaw |
| 105 | Danzick |
| 106 | Kennoin Austria |
| 107 | Lione in France |
| 108 | Paris in France |
| 109 | Rouen in Normandy |
| 110 | Brabant |
| 111 | Seville in Spain |
| 112 | Castile in Spain |
| 113 | Andalusia |
| 114 | Valencia |
| 115 | Seville |
| 116 | Barcelona |
| 117 | Malaga |
| 118 | Rosario |
| 119 | Granada |
| 120 | Seville |
| 121 | Seville |
| 122 | Seville |
| 123 | Seville |
| 124 | Seville |
| 125 | Seville |
| 126 | Seville |
| 127 | Seville |
| 128 | Seville |
| 129 | Seville |
| 130 | Seville |

The other Table of agreement of Measures
by the aid whereof you may with the rule of the

The eighteenth Chapter treateth of
Sports, and Pastimes, done
by number.



If you would know the number that any man doth think or imagine in his minde, as though you could divine, bid them triple it, or put twice so much more to it as it is, which done, ask him whether it be even or odde; if he say odde, bid him take one to it, to make it even, and for that one keep one in your mind. Now after he hath taken one to it, to make it even, bid him give away half, and keep the other half for himself, which when he hath done, bid him triple that half, and again after he hath tripled it, ask him whether it be even or odde; if he say odde, then bid him take one to make it even again, and for that one, keep two in your mind: now after he hath made his number even, bid him call away the one half, and keep the other still, from which half that he keepeth, cause him subtilly to put away or give you nine out of his number, as oft as he can, and for each 9 that he giveth you, keep 4 in your mind, and thereunto joyn the 3 which I bad you keep, and you shall have your desire.

Exam-

Example.

Imagine he thought 7, the triple whereof is 21, and because it is odde; he is to take 1 to make it even, which first 1 given, is for you to keep in mind. Then the half of his 22 being cast away, he reserveth still 11, which after you have bid him triple, it maketh 33: then in giving of him one again to make it even, upon that last 1 reserve 2 in your minds, then his half of 34 maketh 17; from whence he can give you 9 but once. Therefore that yeelding to you 4, and the 3 that you keep, make 7 your desire.

Another kind of Divination, to tell your friend how many pence or single pieces, reckoning them one with another, he hath in his purse, or should think in his mind.

Which to do, first bid him double the pieces he hath in his purse, or the number he thinketh, (if he participate his number or secrecy unto some one friend that sitteth by him that can but multiply, and adde never so little: if their number be great, then shall they work as you bid them so much the surer.)

Now after he hath doubled his number, bid him adde thereunto 5 more; which done, bid him multiply that his number by 5 also; which done, bid him tell you the just summe of his last multiplication, which summe the giver thinketh it nothing available, because it is so great above his pretended imagination: yet thereby shall you presently with the help of Subtraction tell his proposed number.

The Rule is this.

Imagine he thought 17, Double 17, 34
 and it maketh 34, whereunto if you
 adde 5, it maketh 39: which multipli-
 ed by 5, as here is practised, is yeelded
 195, which 195 is the summe delivered
 you in the work: then for a generall
 Rule you shall evermore cut off the last
 figure toward your right hand, with a
 dash of your pen as here is performed, as
 a figure nothing available unto your
 work, and then rebate 2 from your first
 figure, after 5 is cut off, and the rest
 shall evermore be your desire, as by this
 example doth appear.

Another of a Ring.

If in any company you are disposed to make
 them merry by manner of divining, in deli-
 vering a Ring unto any one of them, which af-
 ter you have delivered it unto them, that you
 will absent your self from them, and they to
 devise after you are gone, which of them shall
 have the keeping thereof, and that you at your
 return will tell them what person hath it,
 upon what hand, upon what finger, and what
 joynt: Which to do, cause the persons to sit
 down all in a row, and to keep likewise an or-
 der of their fingers: now, after ye are gone

out from them to some other place, say unto one of the lookers on, that he double the numbers of him that hath the Ring, and unto the double bid him adde 5, and then cause him to multiply the Addition by 5, and unto the product, bid him adde the number of the finger of the person that hath the Ring. And lastly, to end the work, beyond that number towards his right hand, let him set down a figure signifying upon which of the joynts he hath the Ring, as if it be upon the second joynt, let him put down 2. Then demand of him what number he keepeth, from the which you shall abate 250, and you shall have three figures remaining at the least. The first toward your left hand, shall signifie the number of the person which hath the Ring, the second or middle number shall declare the number of the finger, and the last figure towards your right hand shall betoken the number of the joynt.

Example.

Imagine the seventh person is determined to keep the Ring upon the fifth finger, and the third joynt: first double 7, it maketh 14, thereto adde 5, it maketh 19, which multiplied by 5, yeldeth 95, unto which 95, adde the number of the finger, and it maketh 100: and beyond 100 toward the right hand, I set down 3 the number of the joynt, all maketh 1003, which is the number

that is to be delivered you, from which abating 205, there resteth 753, which prefigureth unto you the seventh person, the first finger, and the third joynt.

But note, that when you have made your subtraction, if there do remain 0, in the place of tens, that is to say, in the second place, you must then abate 1, from the figure which is in the place of the hundreds, that is to wit, from the figure which is next your left hand, and that shall be worth 10 tenths, signifying the tenth finger, as if there should remain 803, you must say, that the seventh person upon his tenth finger, and upon his third joynt, hath the Ring.

Another of three Dice.

If a man do cast 3 Dice, you may know the points of one of every of them. For if you cause him to double the points of one Die, and to the double to adde 5, and the same summe to multiply by 5, and unto the product adde the points of one of the other Dice; and behinde the number towards the right hand, to put the figure which signifieth the points of the last Die, and then to ask what number he keepeth, from which abate 250, and there will remain 3 figures, which do note unto you the points of every Die.

Another of things hidden.

If three divers things are to be hidden of three

three divers persons, and you to divine, which of the three persons hath the three divers things, do thus: imagine the three things to be represented, *A*, *B*, *C*. Then secondly, keep well in your mind which of the persons you mean to be the first, second, and third. Then take 24 Counters or Stones, and your three things, and give *A* to the party whom you imagine to be your first man, and therewithall give him one of your 24 Counters in his hand, and *B* unto your second man, and therewithall 2 Counters, and *C* unto your third man, and therewithall 3 Counters: and leave the rest, which are 18, still among them: which done separate your self from them; and afterwards bid them change the things among them as they shall think good: which done, after they are agreed, bid him that hath such a thing, as before you have represented by *A*, for every Counter that he hath in his hand, to take up as many more. And for him that hath *B*, for every one in his hand to take up two. And for him that hath *C*, for every one in his hand to take up 4, and the rest of them to leave still upon the board. These 3 things, and the three persons being fully printed in your mind, come to the Table, and you shall evermore find one of these 6 numbers, 1, 2, 3, 4, 5, 6, or 7. If therefore one remain still upon the board, then have they made no exchange, but keep them still as they were delivered unto them. So that the first man hath *A*, the second

B, and the third man C, but if 2 remain, then the first man hath B, your second man A, and your third man C. The rest of the work and the order thereof are here apparent by the Table following.

| | | | |
|----|---|----|---|
| 1 | A | 1 | B |
| 2 | B | 2 | C |
| 3 | C | 3 | A |
| 4 | A | 4 | B |
| 5 | B | 5 | C |
| 6 | C | 6 | A |
| 7 | A | 7 | B |
| 8 | B | 8 | C |
| 9 | C | 9 | A |
| 10 | A | 10 | B |
| 11 | B | 11 | C |
| 12 | C | 12 | A |

Another divination of a number upon the casting of two Dice.

First let the Caster cast both the Dice, and mark well the number: then let him take up one of them, it maketh no matter which, and look what number it hath in the bottom, and adde all together: then cast the Dice again, and keep in his mind what all together maketh: then let the Dice stand, and bring seven with you, and thereunto adde the rest of the pirs that you see upon the upper side of the Dice, and to many did the caster cast in all.

F I N I S.

An

An Appendix concerning the Resolution
of the Square and Cube in Numbers, to
the finding of their side, by Ro. Hartwel.



*Figurate Number is a number made by
the multiplication of one number or
more by another.*

A figurate
number
what.

*The sides of a figurative number, are
the numbers by whose multiplication it is made.*

The sides
of a figu-
rate num-
ber what.

A Figurate number is two-fold, a

{ Plain.
Solid.

*Of one Multiplica-
And tion,
it is. Or consequently of
many.*

{ Plain.
Solid.

*Both Equilater.
And in each
And Inaquilater.*

*A figurate number made of one multiplication,
by two sides or numbers multiplied together, is
called a plain figurate number.*

For every number made by the mutuall mul-
tiplication of two numbers, may be called a
Plaine, because it bringeth forth a right-
angled parrallogramme, according to his
unities disposed in *length* and *breadth*, the sides
whereof are the two multiplying numbers. As
the number 20, made by the mutuall multi-
plication of 4 and 5 is called a *Plain*, and

A plain
figurate
number.

the *sides* thereof are 4 and 5 as * * * * *
here. * * * * *

Because the unities thereof dis- * * * * *
posed in *length* and *breadth*, as * * * * *
the *sides* do expresse, do bring forth an *inequi-*
later Parallelogram, for that the numbers, or
sides are inequall.

By like reason 36 made by multiplication
of 6 by 6, is called an *Equilater plain*, for the
sides thereof 6 and 6 are equall.

Moreover one and the same *plain number*
may have many *sides*, as the *plain number* 24,
hath *sides* 4 and 6 : 3 and 8 : 2 and 12. For
it is produced from the mutuall multiplication
of these numbers : whereupon for the inventi-
on of the *sides*, to wit, in *inequilater Plains*, it
is needfull to give one of the *sides*, by which
the *plain* it self divided, the other *side* is made
known. As the *plain* 48 being divided by the
side 8, the *quotient* 6 is the remaining *side*.
Notwithstanding another resolution and in-
quisition doth happen in the *sides* of the *E-*
quilater plains.

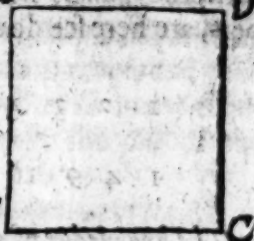
An Equi-
later Plain
or quadrat
whar.

An *Equilater plain* is a number made by two
equall *sides*, or by any number multiplied by it
self. It is vulgarly called a *square* or *quadrat* ;
by the *Arabians* *Zensus*, it is commonly expres-
sed by this note \square , by us q .

A *quadrat* or *square* in *Geometry* is called a
right lined *plain figure*, made by four equall
right lines, and so many right Angles, and every
one of the lines is called the *side* of the *qua-*
drat,

drat, as this figure *abcd*
whose side is *ab*, or *bc*, *a*
as also *cd*, and *ad*.

To the similitude here-
of, that number is called
a *Quadrat*, which is
made by the multiplica-
tion of two equal num-
bers, or of one in it self
of which manner 36 is



made, by 6 multiply in it self, or by the mu-
tuall multiplication of 6 and 6. * * * * *
For if 36 unites be placed in * * * * *
plain form, it bringeth forth * * * * *
a perfect Geometricall Qua- * * * * *
drat, having in every side fixe * * * * *
unities as here. * * * * *

The number whereof the *Quadrat* is produced
by multiplication in it self, is called the side or
root of the *Quadrat*.

The side
or root of
a number
what.

Concerning the extraction of the *Quadrat* or Square Root.

Therefore to find the *Quadrat* root, or the
side of any *Quadrat* number, is to search a
number, which brought or multiplied in it
self, maketh the number propounded: concer-
ning the finding whereof, as it is requisite that
the sides (being lesser then 10) of the squares
under an hundred should be gathered by the
Table of Multiplication: so the sides of the
grea-

greater Squares are to be sought out by. *Art.*
First, the Squares whose sides are simple num-
bers, are here set down as you see.

The roots.

1 2 3 4 5 6 7 8 9 10 11 12

The
Squares.

1 4 9 16 25 36 49 64 81 100 121 144

The knowledge of a square is by finding out his
side expressed by a whole number.

Although the finding out of the side of a
square be applied to each number given, as to
a square; yet square numbers only have a side to
be expressed by a certain number of unites, or
by rational numbers, the other are to be ex-
pressed but only in power. The sides are com-
monly called Roots by a Metaphoricall phrase.

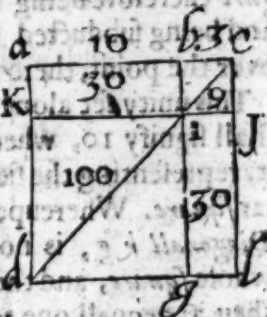
576
30 100 121
25 36 49 64 81 100 121

The Root or side of a square is to be found by
the Theorems following.

1. If the odde degrees of a square number being
marked from the right toward the left hand
with points, you subduct from the number gi-
ven, the particular square of the last period, set-
ting the side thereof alone by it self.
2. Then going on, if you divide the remainder
(if there be any) with the figure going before
it, by the double of the side set alone by it
self.
3. And multiply the quotient, found out (being
placed by the side, which was first set alone by
it self, and also before the doubled number
on

on the right hand) by both the numbers (namely by the double number, and the Figure set by it self) being counted as one divisor, subtracting the products from the given number, and then renew this last work of division so many times as there are pricks remaining, the side of the square shall be found out.

This artificiall device is taken out of the 4 P. 1. of Euclide, where by demonstration it is proved, that if a right line be cut into two segments, howsoever the square of the whole line is equal to the squares of the segments, and the two right-angled figures made of the segments as in the figure annexed, the two Diagonals, $h g$, and $b f$, are the squares of the segments, $a b$, and $b c$. Also the complements $b k$, and $f c$ are the right-angled figures made by multiplying the line $a b$ by $b c$.



To extract the square root

The self-same parts are to be found in any square number. As for example, let the number be 169, whose side is 13. This side being divided into two pieces, 10 and 3, multiplying each piece by it self once, namely, 10 by 10, and 3 by 3: then multiply one by another, as 10 by 3, and 3 by 10, so shall you have four plain numbers, whereof two are square, as here you see.

The first example.

There-

Therefore as the *square* 169 is made by adding together of these four *plain numbers*, so by subtracting them severally it is resolved.

First, therefore I mark each odde place with points, because the *particular squares* are to be found in the odde places. Then for so much as the unity standing under the first point next the left hand, and representing the last period, is both a *square* and the *side* of a *square*: that figure therefore being set alone in the *quotient*, and being subducted from the unity standing over the point, there remaineth nothing,

This unity set alone by it self in the *quotient*, shall signify 10, when another figure is set by it, representing the *side* of some other particular *square*. Whereupon I say, that the greater *Diagonall* *k g*, is now subducted from the whole *square*, and the *side* of it *k i*, or *a b*, (for they are equall one to another) and also the *side* of the *complement* is found out.

This is the first step to this resolution.

Moreover, I double the figure found out, because being doubled, it is the *side* of both the *complements* taken joyntly together, namely, *k i*, and *g i*. Then setting the doubled number under 6, I divide 6 (which in this place is as much

much as 60, and representeth both the complements) by 2, the quotient is 3, representing the other side remaining of the complement, namely, $1f$, for bc , which number I set in the quotient, and count it for the segment remaining of the right line given. Wherefore because this number 3 is the side of the remaining Diagonal, that is to say, of the lesser square $b f$, therefore being set by the divisor on the right hand, and multiplied by it self, and also by the divisor, it bringeth forth three plain numbers, namely, the square $b f$, and the two complements $a i$, and $i f$, which being subducted from the numbers standing over them, there remaineth nothing.

The example is thus.

| | | | |
|--|---|---|---|
| $\begin{array}{r} 169 \text{ (12 which is all one,)} \\ \hline 223 \\ \hline 3 \\ \hline 69 \end{array}$ | <i>as if you had put down the numbers found out in this manner.</i> | $\begin{array}{r} 169 \\ \hline 100 \\ \hline 60 \\ \hline 9 \\ \hline 169 \end{array}$ | $\left\{ \begin{array}{l} \text{The greater Diagonal.} \\ \text{The complements twofold.} \\ \text{The lesser Diagonal.} \end{array} \right.$ |
|--|---|---|---|

The subtilty of this invention is illustrated by many examples. The second example.

Let the square given be 1764. This number being marked with two points, telleth us, that the side thereof is to be written with two Figures.

First,

First therefore beginning at the point on the left hand, I seek the side of the last period, namely, 17. But for so much as it is no square number, I take 4 the side of the next lesser square, which I set alone by it self in the quotient, and then multiply it by it self, the product is 16, which being subducted from 17, there resteth 1. Moreover I double the side found out, the product is 8, I place this doubled number under 6, and by it divide 16 standing above it, the quotient is 2, which must be set by 4. This quotient 2 must be set before the Divisor 8, on the right hand under the point, and then must it be multiplied both by it self, and into 8, the product is 164, which being subducted from the figures standing over them, there remaineth nothing: whereby I gather that the number given is a just square.

The Example standeth thus:

$$\begin{array}{r} 1764 \quad (42 \\ \hline 1682 \\ \hline 2 \\ \hline 164 \end{array}$$

The Collection.

The same manner of working is to be followed in greater square numbers given, saving that the former part of the work is to be used but once,

once, but the latter part is to be followed so many times as there are points remaining, excepting the last.

As in 5 47 56, I say, that the *side* of the square next unto 5 is 2: therefore 2 being set in the *quotient*, and multiplied by it self, makes 4, and taken from 5, the remainder is 1. Moreover I double the *quotient*, the product is 4, which I set under the next figure toward the right hand, and thereby divide 14, the *quotient* is 3, which three being set both in the *quotient*, and also before the *Divisor* toward the right hand, I multiply both the numbers by it, the product is 129: this being subducted from 147 standing above it, the remainder is 18. But because there is yet one point remaining, with which I have not medled; I therefore again double all the whole *quotient*, for in this case I must take 23 for the *side* of one former square, and generally in great numbers, when I light upon more particular squares then two, I must esteem them but as two, and take the *sides* which are first found out, but as the *sides* of one only square. Therefore twice 23 is 46: by this I divide 185, the number to be set in the *quotient* is 4, which number also must be set before the *Divisor* on the right hand: then must 464 be multiplied by 4: the product is 1856 this product being subtracted from the numbers standing over it, there remaineth nothing. The example standeth thus.

The third example.

Note.

The

228

94736 (234

44364

129

4

1836

54736

*The Collection.**See also the Example following.*

10942864 (3308.

Therefore out of this invention is this con-
fessary.

4 Exam-
ple of a
furd num-
ber.

*The number whose side cannot be expressed by
whole numbers, is not a square number.*

Such are all prime numbers, and (the squares
themselves excepted) all other compound num-
bers. For if in them you desire to find out the
square side, you shall labour in vain, because
they are not squares, for to the whole numbers
arising in the *quotients*, there will be some *fra-*
ction adjoyned, whereby it commeth to passe,
that the number of the *side* is not to be expres-
sed by a true number, and it is commonly cal-
led a *furd number*.

Notwithstanding, if you adjoyn to the *side*
found out, the number remaining, taking his
denomination from the double of the *side aug-*
mented

mented by an unity, you shall finde the next side that may be like to the *side of a square*.

As if from 40 you take the nearest *square*, to wit, 36, the remainder is 4. Here therefore the side sought for of the *square* exceedeth not the side found out by an unity, but either by one, or more parts of some whole number : wherefore I double 6, the side found out, and adde an unity to it being doubled, the totall is 13, this number I set under 4 the remainder, and say that the side of 40 demanded as near as may be, is $6\frac{1}{13}$: the *Denominator* of the *fraction* being added to the greatest *square* in the number given, namely unto 36, maketh the next greatest *square* above it, namely, 49, whose side is 7. But this surd side, to wit, $6\frac{1}{13}$, multiplied by it self, maketh $39\frac{1}{169}$, which are not just equall to 40, the given number.

Judge the like concerning the rest which are not *squares*.

Thus much concerning plain-figurate numbers, but especially such as are *square numbers*.



Concerning solid figurate Numbers.

A Solid figurate Number is made of two multiplications by three numbers, or sides, multiplied together, admitting length, breadth, and thicknesse.

Qq

There-

A solid figurate number.

Therefore every number made by the mutuall multiplication of three numbers, may be called a *solid*, because it bringeth forth a *right angled parallelipedon*, disposed according to his unities in *length*, *breadth*, and *thicknesse*, the *sides* whereof are the three multiplying numbers. As the number 30 made by the mutuall multiplication of 2, 3, and 5, is called an *Inequilater solid number*, and the sides thereof are 2, 3, and 5; because the unites thereof disposed by a certain distance one from another, in *length*, *breadth*, and *depth*, as the sides do expresse, do bring forth resemblance an *Inequilater parallelipedon*, for that the numbers or sides are inequall.

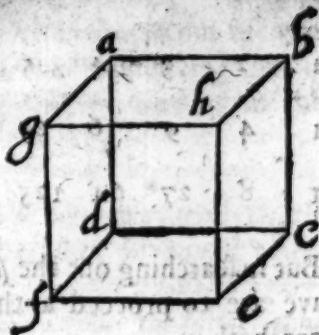
By like reason 216 made by multiplication of 6 by 6, and the product thereof by 6, is called an *Equilater solid*, for the sides thereof 66, and 6 are equall.

An Equilater, Solid, or Cube.

An *Equilater*, is a number made by three equall sides, or by any number multiplied by it selfe, and that product again by the aforesaid number. And it is called an *Equilater* and *Equi-angled Parallelipedon* or *Cube*, and is commonly represented by us thus C.

A *Cube* in Geometry is a right-angled Parallelipedon having six equall surfaces, and 8 solid

Solid angles, and 12 sides, as this figure a. b. c. d. e. f. g. h. whose side is a b, or a d, also b c, or c d, either c e, or e f, likewise c b, or b g, also g f, or d f, or d a, and g a.



The number whereof the Cube is produced by Multiplication in it self twice, is called the side or root of the Cube, which being found out in whole numbers, the Cube is known.

The side or root of Cube.

Concerning the extraction of the Cubick Root.

Therefore every Cube in numbers hath such a side as may be expressed in whole numbers, but in magnitudes it is not always so, as indeed in magnitudes there are many things not to be expressed in whole number. Now for as much as the side of any Cube under 1000, is a simple figure, it is necessary, before we undertake to find out the side of any great number, to know what Cube is made of each simple figure, and what is the side of any lesser then 1000, as I have here set them down.

Qq 2

Roots

| | | | | | | | | | |
|-----------------|---|---|----|----|-----|-----|-----|-----|-----|
| <i>Roots.</i> | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| <i>Squares.</i> | 1 | 4 | 9 | 16 | 25 | 36 | 49 | 64 | 81 |
| <i>Cubes.</i> | 1 | 8 | 27 | 64 | 125 | 216 | 343 | 512 | 729 |

But in searching out the *sides* of greater *Cubes*, we are to proceed as the *theorem* following teacheth us.

If you distinguish with *points* as it were into periods, the given *Cube* beginning at the first figure on the right hand, and omitting each two figures continually, and first of all subtract the *particular Cube* of the last period from the given number, setting the *side* thereof in the *quotient*: and then set triple of the *quotient* under the figure next following the former point on the right hand, and the *square* of the *quotient* being tripled beneath it one degree more toward the left hand: and afterward divide the number above written by the triple of the *square*, setting the *quotient* by it self, and then multiply the *divisor* by the *quotient* found out, and the tripled *square* by the *square* of the *quotient*, and the *quotient* *cubicall*y, subtracting the *products* (so orderly added together, that each figure may answer the *numbers* whereof it was multiplied) from the number given, and renue this last manner of Division so many times as there are *points* remaining, the *side* of the *Cube* shall be found out.

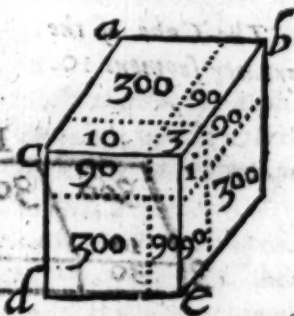
This

This artificiall device is drawn out of that theorem, which *Ramus* made, imitating that of *Euclide*, concerning square numbers in this manner.

If a right line be cut into two segments, the Cube of the whole line shall be equall to the Cubes of the segments, and the two solid figures comprehended three times under the square of his segment, and the segment remaining.

The extraction of the Cubick side or root.

As the line *ci*, which is 13, is cut into two segments, 10 and 3, therefore the Cube of the whole line, namely, 2197, is equall unto the Cubes of the Segments, namely unto 1000, and 27 also to the two-fold Solids or Parallelipipedons thrice taken,



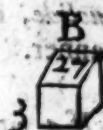
whereof three have like solidity, the solidity of each of the three lesser is 90, being made of the square of the segment, 3, that is to say of 9, multiplied by the other segment 10. These three Parallelipipedons joyntly taken together, make 270. But of the three greater Parallelipipedons each containeth 300, being made of 100, the square of the greater segment 10, multiplied by the lesser segment 3,

Qq 3

and

and they being taken joyntly together, make 900,

*The Cube of
the lesser seg-
ment 3.*



*The Cube of the
greater segment 10.*

*The 3 lesser Paral-
lelipedons.*



*The three greater Paralleli-
pipedons.*

The Cube therefore hath eight particular solids in number, which are made of the parts of the number given, namely, of 10 and 3 in this manner: First, let there be four plain numbers made, each part being multiplied by it self; and one by another.

10 10 10 3
10 10 10 3

9
30
30
100

If again I multiply the *Plains* by the same parts, there will arise 8 *solids*, as you see here.

9 9
30 30
30 30
100 100
3 10

27 90 All those being added
90 300 together, are equall to
90 300 the Cube of the whole,
300 1000 to Wit, 2197.

Therefore the same way that is kept in making the Cube, is also to be followed in resolving the Cube.

As for example, I mark the *Cube* given points in this manner, 2197.

The first
example
to extra^t
the Cu-
bick root.

Then I subduct the particular *Cube* of the number set under the last point: but for so much as that number is no *Cube*, I take the nearest to it, namely, an unity, which also I set in the *quotient*. This unity in the number given, is 100, but in the *quotient* it is but 20, the unite subducted from 2, the remainder is 1, which must be written over the number gi-

Qq 4

ven

ven. So that the greater *Cube A*, is to be supposed to be subducted from the number given.

This is the first step of this work.

$$\begin{array}{r} 1 \\ 2197 \quad (1 \\ \times \end{array}$$

After I triple the *quotient* found out (that is to say, I multiply it by 3) this triple representeth the three *sides* (joyntly taken together) of the three lesser *solids* marked with *C*, I place the tripled number under 9. Again, I multiply the *quotient* square-wise, and triple the *product*, which maketh likewise 3. This *product* resembleth the three *square sides* (taken joyntly together) of the three greater *solids*, marked with *D*, I place the *product* on a degree lower toward the left hand underneath 1. With it I divide 11, which written above it, the *quotient* is 3. This *segment* or *quotient* 3, being multiplied by 3, the *divisor* maketh 9, which in respect of the place wherein it standeth, is 900, and representeth the three greater *solids* marked with *D*, taken joyntly together. Furthermore the same *quotient* being multiplied square-wise, maketh 9, and multiplied afterward by the *tripled number* standing under 9, it maketh 27, which in respect of the place wherein it standeth, is 270, and representeth the 3 lesser *solids* marked with *C*. Last of all, the same

same *quotient* multiplied *cubically*, breedeth the lesser *Cube B*. These 3 *products* therefore being added together, and the totall subducted from the *numbers* standing over it, there remaineth nothing, which importeth the given number is a *Cube*.

The Example is as you see.

$$\begin{array}{r}
 2197 \text{ (13)} \\
 1000 \text{ The greater Cube.} \\
 27 \text{ (3)} \\
 27 \text{ (3)} \\
 \hline
 9 \text{ Or thus : } 900 \text{ The 3 greater Parallelepipedes.} \\
 27 \text{ (3)} \\
 27 \text{ (3)} \\
 \hline
 2197 \text{ (13)}
 \end{array}$$

The matter may be explained by many examples.

The second example of the Cubick root.

Let the *side* of the given *Cube* 16387064, be sought out, contrive it therefore (as it were) into certain periods with points. Then first of all, search out the *side* of the *Cube* next to the left hand: But for as much as 16 is no *Cube*, take 2 the *side* of the next *Cube* under it, that is to say, of 8, and set in the *quotient*, and subduct 8 the *Cube* thereof from 16, there remaineth 8. The first work is not to be renewed throughout the whole *number*, but the *rules* following must be repeated as often as there are *points* remaining.

The

*The first step to finde out the root, is
in this manner.*

$$\begin{array}{r} 8 \\ 16387064 \quad (2 \\ \underline{8} \end{array}$$

Moreover, triple the *quotient* now found out, and the *product* is 6, which is to be placed under 8, namely, under the figure following the next prick toward the right hand. Then multiply the *quotient* by this tripled number (or which is all to one purpose, square the *quotient* and then triple the *product* it maketh 12, set that number in a lower place one degree nearer the left hand, and make it the *divisor*: divide 83 by 12, observing this rule in choosing your *quotient*, that it be no greater, then that the numbers afterward produced by multiplication may not exceed the numbers standing over it. So that here you shall take 1 in 8, but 5 times. Afterward by this number 5, multiply the *divisor* 12, and by the square of 5, multiply the tripled number 6, and last of all multiply 5 cubically: so shall you produce three numbers, namely, 60, 150, 125, to be described in such sort as you see. These numbers added together, and subducted from 8387, the remainder is 762.

*The second step to finde out the root,
in this manner.*

8762

8762

16387064 (25

6

12

60

150

125

7625

And because there is yet one point remaining, this last manner of Division must be wrought again.

First, therefore I triple the quotient, the product is 75, which must be so placed, that the first figure thereof, namely 5, may stand under 6, the second under the 0. Again, multiply the quotient by this tripled number, (or which is all one, square the quotient, and triple the product) it maketh 1875, which must be the Divisor, whose first figure, namely 5, must be placed under 7, the last figure of the tripled number. Then see that 1 may be contained in 7, many times, but I can take it but 4 times, I set 4 in the quotient, and multiply the Divisor by 4, the product is 7500, afterward I square 4, it maketh 16, which I multiply by the tripled number 75, the product is 1200. Last of all, I multiply 4 cubically, it maketh 64, these products added all
toget-

together, make 762064, which number being subducted from the *Cube* given, there remaineth nothing, whereby I gather that the number given is exactly *cubicall*.

The third step to finde out the side is in this manner.

$$\begin{array}{r} 762 \\ 16387064 \end{array} (254$$

$$\begin{array}{r} 75 \\ 1875 \end{array}$$

$$\begin{array}{r} 7500 \\ 1200 \end{array}$$

$$64$$

$$762064$$

The third
example of
the Cubick
root.

Behold also the example following.

$$6141250000 (850$$

Another manner of working.

Hitherto the Princely high-way to find out the side of the *Cube* hath been declared.

But there are moreover certain other ways also bending thereto, and leaning to the same principles, whereof this is one.

The second form.

Having found out in the Table of simple *cubes*, the first figure representing the side of the *cube* contained in the number standing under the first point on the left hand, set it in the quotient,

and

and subduct the particular *Cube* of that figure as you did before: then *square* that figure, and triple that *square*, the *product* shall be the *Divisor*, the first figure whereof shall be set under that figure which is on the right hand next of all to the point (now examined) before going.

See how many times the *Divisor* is contained in the *number* written over it, and multiply the *Divisor* in the *quotient*, and subduct the *product* from the *dividend*: yet here you must take heed, that you take not a greater *quotient* then that the *product* made afterward thereby may be subducted from the *number* given.

The subduction being done, triple the first figure which was set in the *quotient*, and adde to the triple the last *number* which was set in the *quotient* on the right hand of the *product*.

This totall multiplied by the *square* of the figure last found out, and set down the *product* so, that the first figure thereof toward the right hand may stand under the *point* next before going on the same hand, and finally, subduct the same from the *number* given.

As in 804357. the particular *Cube*, namely, 729 being taken from the *number* standing under the last *period* upon the left hand, there remaineth 75357, the *side* of that particular *cube* being 9, I set in the *quotient*. Then I *square* that *side*, it maketh 81, and triple the *square*, the *product* 243 is my *Divisor*, which I set under the given *number*, so that 3 may stand under 3 with

2.

3.

4.

The fourth
example of
the Cubick
root.

with this *Divisor*, divide the number standing over it, you shall find 3 to be contained in 7 three times. Therefore I set 3 in the quotient, and multiply the *Divisor* by it, the *product* is 729, which being subducted from 753 the remainder 24.

The induction is thus:

753
 729
 24
 3
 729
 24
 3
 729
 24
 3

Moreover I triple 9, the product is 27, by which on the right hand I set 3 the quotient last found out, the total is 273.

This number I multiply by 9 the square of the quotient last found out, the product shall be 2457, which being subducted from the superior number, there remaineth nothing.

The induction is thus:

24
 804357 (93)
 732
 9
 457

Another

Another manner.

The self same work may be dispatched another way, a little differing from the former, in this manner.

The figure in the *quotient*, being found out by subducting the particular *Cube*, and also the second figure in the *quotient* being found by division, let the totall *quotient* be tripled, and let the tripled number be multiplied by the former figure in the *quotient*. Then let the product be multiplied again, by the latter figure found out, and let a cypher be set on the right hand of that product. Last of all, let the *Cube*, of the latter figure found out, be added to this product, and let the totall sum be subducted from the number given: As in 373248.

The third form.

The first induction is in this manner.

30
373248 (7
343

Moreover I square the side found out, it maketh 49, and triple the square, the product is 147, which shall be the *divisor*, by this I divide 302, the number written over it, the *quotient* is 2. Now I triple the totall *quotient* 72, it maketh 216, and multiply this triple by 7, the former figure in the *quotient*, the product is 1512. I multiply this product also by 2, the latter figure of the *quotient*, and set a cypher on the right hand of it, so as it maketh 30240, unto this number last of all I adde 8, the *Cube*

The fifth example.

of

of the latter *figure* found out, the totall is 30248 which being subducted from the *figure* above it, there remaineth nothing.

The second Induction is thus.

$$\begin{array}{r} 3^{\circ} \\ 378248 \end{array} \quad (72)$$

147

30248

To finde
the nea-
rest Cu-
bicke root
in a surd
number.

All the points of the number given being examined, if any thing remain, it signifieth the number given is no Cube: wherefore the true side of it cannot be exactly given in numbers. Yet if it please you to list out the nearest side that may be, by the first kinde of reduction of mixt numbers, you shall reduce the number given unto a cubickall fraction of a greater denomination, and afterward seek out the cubickall side of that fraction.

For example sake, because 120 is no Cube, therefore let it be reduced into sixty cubickall parts, after this manner. Multiply 60 cubickally in it self, it maketh 216000, by this being taken for the denominator of the fraction, multiply 120 the number given, the product is 2592000 whose cubickall side is $14\frac{17}{17}$, that is, 14 $\frac{17}{17}$, the nearest to the true side that can be.

For the extraction of all sorts of roots, the table of Logarithmes set forth by M. Briggs are most excellent, and ready.

FINIS.

A Table of Board and Timber measure, more perfect then ever hath been made; shewing also the Squares between 4 and 37 from quarter to quarter, calculated by Robert Hartwell.

| Board
measure | Inches &
quarters | Squares | Timber
measure | Board
measure | Inches &
quarters | Squares | Timber
measure |
|------------------|----------------------|---------|-------------------|------------------|----------------------|---------|-------------------|
| 36.0.0 | 4 | 16 | 08.0.2 | 16.0.0 | 9 | 81 | 21.3.3 |
| 33.8.8 | 1 | 18 | 06.0.0 | 15.5.6 | 1 | 85 | 20.3.3 |
| 32.0.0 | 2 | 2 | 86.4.0 | 15.1.6 | 2 | 90 | 19.2.0 |
| 30.3.1 | 3 | 2 | 78.5.4 | 14.7.7 | 3 | 95 | 18.1.8 |
| 28.8.0 | 5 | 30 | 69.1.2 | 14.4.0 | 10 | 100 | 17.2.8 |
| 27.4.3 | 1 | 27 | 64.0.0 | 14.0.5 | 1 | 105 | 16.4.6 |
| 26.1.8 | 2 | 35 | 57.6.0 | 13.7.5 | 2 | 110 | 15.7.1 |
| 25.0.4 | 3 | 38 | 52.3.6 | 13.3.9 | 3 | 115 | 15.0.2 |
| 24.0.0 | 6 | 36 | 48.0.0 | 13.0.0 | 11 | 121 | 14.2.8 |
| 23.0.4 | 1 | 39 | 44.3.0 | 12.8.0 | 1 | 126 | 13.7.1 |
| 22.1.5 | 2 | 42 | 41.1.4 | 12.5.3 | 2 | 132 | 13.0.9 |
| 21.3.3 | 3 | 45 | 38.4.1 | 12.2.7 | 3 | 138 | 12.5.2 |
| 20.5.7 | 7 | 49 | 35.2.6 | 12.0.0 | 12 | 144 | 12.0.0 |
| 19.8.6 | 1 | 52 | 33.2.3 | 11.7.5 | 1 | 150 | 11.5.1 |
| 19.2.0 | 2 | 56 | 30.8.6 | 11.5.2 | 2 | 156 | 11.0.7 |
| 18.5.8 | 3 | 60 | 28.8.0 | 11.2.9 | 3 | 162 | 10.6.6 |
| 18.0.0 | 8 | 64 | 27.0.0 | 11.0.7 | 13 | 169 | 10.2.2 |
| 17.4.6 | 1 | 68 | 25.4.1 | 10.8.7 | 1 | 175 | 9.8.7 |
| 16.9.4 | 2 | 73 | 24.0.0 | 10.6.7 | 2 | 182 | 9.4.6 |
| 16.4.6 | 3 | 76 | 22.7.5 | 10.4.7 | 3 | 189 | 9.1.4 |

R r

| Road
measure | Inches &
quarters | Squares | Timber Board
Measure mea-
sure | Inches &
quarters | Squares | Timber
measure |
|-----------------|----------------------|---------|--------------------------------------|----------------------|---------|-------------------|
| 10.2.8 | 14 | 169 | 8.8.1 | 6.8.6 | 21 | 4413.2.2 |
| 10.1.1 | 1 | 203 | 8.5.1 | 6.7.7 | 1 | 4513.8.2 |
| 9.9.3 | 2 | 210 | 8.2.3 | 6.6.6 | 2 | 4623.7.3 |
| 9.7.6 | 2 | 217 | 7.9.6 | 6.6.4 | 2 | 4733.6.5 |
| 9.6.0 | 13 | 225 | 7.6.8 | 6.5.4 | 22 | 4843.5.7 |
| 9.4.5 | 1 | 232 | 7.4.3 | 6.4.7 | 1 | 4953.4.9 |
| 9.2.9 | 2 | 240 | 7.2.0 | 6.4.0 | 2 | 5063.4.1 |
| 9.1.4 | 3 | 248 | 6.9.7 | 6.3.3 | 3 | 5173.3.8 |
| 9.0.0 | 16 | 256 | 6.7.5 | 6.2.6 | 23 | 5293.2.7 |
| 8.8.8 | 1 | 267 | 6.5.4 | 6.1.9 | 1 | 5403.2.0 |
| 8.7.3 | 2 | 272 | 6.3.5 | 6.1.2 | 2 | 5523.1.3 |
| 8.6.0 | 3 | 280 | 6.1.6 | 6.0.6 | 3 | 5643.0.6 |
| 8.4.7 | 17 | 289 | 5.9.8 | 6.0.0 | 24 | 5763.0.0 |
| 8.3.5 | 1 | 297 | 5.8.1 | 5.9.4 | 1 | 5882.9.4 |
| 8.2.3 | 2 | 306 | 5.6.4 | 5.8.8 | 2 | 6002.8.8 |
| 8.1.1 | 3 | 315 | 5.4.8 | 5.8.2 | 3 | 6122.8.2 |
| 8.0.0 | 18 | 324 | 5.3.3 | 5.7.6 | 25 | 6252.7.6 |
| 7.8.9 | 1 | 333 | 5.1.8 | 5.7.0 | 1 | 6372.7.1 |
| 7.7.8 | 2 | 342 | 5.0.5 | 5.6.5 | 2 | 6502.6.5 |
| 7.6.6 | 3 | 351 | 4.9.2 | 5.5.8 | 3 | 6622.6.0 |
| 7.5.8 | 19 | 361 | 4.7.8 | 5.5.4 | 26 | 6762.5.5 |
| 7.4.8 | 1 | 370 | 4.6.7 | 5.4.8 | 1 | 6892.7.0 |
| 7.3.9 | 2 | 380 | 4.5.5 | 5.4.3 | 2 | 7022.4.7 |
| 7.2.9 | 3 | 390 | 4.4.3 | 5.3.3 | 3 | 7152.4.1 |
| 7.2.0 | 20 | 400 | 4.3.2 | 5.3.8 | 27 | 7292.3.8 |
| 7.1.1 | 1 | 410 | 4.2.1 | 5.2.8 | 1 | 7422.3.2 |
| 6.0.2 | 2 | 420 | 4.1.1 | 5.2.3 | 2 | 7562.2.7 |
| 6.9.3 | 3 | 431 | 4.0.1 | 5.1.8 | 3 | 7671.2.4 |

| Board
measure | Inches
quarter | Square
measure | Board
measure | Inches
quarter | Square
measure | Board
measure |
|------------------|-------------------|-------------------|------------------|-------------------|-------------------|------------------|
| 5.1.4 | 28 | 784 | 2.2.9 | 4.3.6 | 33 | 1089 |
| 5.0.9 | 1 | 798 | 2.1.6 | 4.3.3 | 4 | 1104 |
| 5.0.5 | 2 | 812 | 2.1.9 | 4.3.0 | 2 | 1120 |
| 5.0.0 | 3 | 826 | 2.0.9 | 4.2.7 | 3 | 1136 |
| 4.9.6 | 29 | 841 | 2.0.5 | 4.2.3 | 34 | 1156 |
| 4.9.2 | 1 | 855 | 2.0.2 | 4.2.0 | 1 | 1174 |
| 4.8.8 | 2 | 871 | 1.9.8 | 4.1.7 | 2 | 1190 |
| 4.8.4 | 3 | 885 | 1.9.5 | 4.1.4 | 3 | 1210 |
| 4.8.0 | 30 | 900 | 1.9.2 | 4.1.1 | 35 | 1225 |
| 4.7.6 | 1 | 914 | 1.8.9 | 4.0.8 | 1 | 1237 |
| 4.7.2 | 2 | 930 | 1.8.6 | 4.0.5 | 2 | 1247 |
| 4.6.8 | 3 | 945 | 1.8.3 | 4.0.2 | 3 | 1280 |
| 4.6.4 | 31 | 961 | 1.7.9 | 4.0.0 | 36 | 1296 |
| 4.6.1 | 1 | 974 | 1.7.7 | 3.9.7 | 1 | 1313 |
| 4.5.7 | 2 | 987 | 1.7.5 | 3.9.4 | 2 | 1331 |
| 4.5.3 | 3 | 1000 | 1.7.2 | 3.9.1 | 3 | 1350 |
| 4.5.0 | 32 | 1024 | 1.6.9 | 3.8.8 | 37 | 1369 |
| 4.4.6 | 1 | 1040 | 1.6.6 | 3.8.7 | 1 | 1388 |
| 4.4.2 | 2 | 1056 | 1.6.3 | 3.8.4 | 2 | 1416 |
| 4.4.0 | 3 | 1072 | 1.6.1 | 3.8.2 | 3 | 1425 |

finding the column of numbers for 200, which I find not, but I find 280 the nearest number to 200, to stand against 17: therefore I lay 17 under 280, will make a sum equal to such number as I like, then looking in the column of number against 17, you shall find that 2 inches 9 parts, or 2 and 8 fourths.



The use of this former Table.

IF upon a Scale or Ruler you divide one inch into ten equall parts or primes, and again by diagonals, and parallel-lines, you subdivide each of them into ten equall parts or seconds, with your compasses, you may take a more exact running measure for board and timber, then by any other means whatsoever, and so place the same, or this Table if you will, upon any Ruler.

Also by means of the columnes of Squares, you may readily finde a square equall to any Parallelepipedon, or piece of timber, which is thicker then it is broad. As for example, suppose a piece of timber to be ten inches thick, and 9 inches broad: if I multiply those sides one by another, they will produce 290, then seeking the columnne of squares for 290, which I finde not, but I finde 280 the nearest number to 290, to stand against 17: therefore I say 17 inches fere, will make a square equall to such an unlike squared piece, then looking in the columnne of timber measure against 17, you shall find that 5 inches, 9 primes, or $\frac{9}{10}$, and 8 seconds,

you, if of an inch in length of the piece will
make a foot of timber. (obdew refers to summer)

Likewise for board measure, you may find how much in length of board must be in one foot.

By the like means, suppose for example that a board appointed to be measured, is 5 inches

~~And~~ if I desire to know how much in length
thereof will make a foot, I feel in the columns

that stand under *unites* and *quarters*, for $15 \frac{1}{4}$.
and also against the same in the *columnne* under

the title of board measure, where I finde 9 inches a prime, or tenth of an inch, and 4 seconds,

or hundreds of an inch will make a foot at that breadth. The like may be practised for any other breadth of land, whether four or

the Principal only.

for the Principal together with the Arrears.

the Principal.

RECEIVED

Rt 3

Cer-

(Faint mirrored bleed-through from the reverse side of the page)

**Item Certain Table shewing the Interest of any Summe of money whatsoever unto 40 years: that hath bin resorted unto by many com-
men men. And for buying or selling of work-
nities for the said time; and also the same in
1600 for after any number of years unto 30.
What they may be worth in present ready ma-
ney by Act and now diligently corrected
and amended by Robert Harrington.**

Definition of Interest.

Prin cipall is the summe from which the In-
terest is reckoned. **I**nterest is the summe added for the bor-
rowing or forbearance of the Principall for any
terms or time.

3 Interest simple is that which is counted from
the Principall only.

4 Interest compound is that which is counted
for the Principall together with the Arrerage.

5 Interest profitable is that which is added to
the Principall.

6 Interest Damageable is that which is to be
subtracted from the Principall.

| | | | |
|-----------|-------------|------|---------------------------------|
| The use | { 1 li. | } is | { 2 s. |
| | { 10 s. | | { 12 d. |
| per annum | { 5 s. | | { 6 d. |
| of | { 2 s. 6 d. | | { 3 d. |
| | { 12 | | { 1 d. $\frac{1}{2}$ of a peny. |

In the former Table, if you desire to know
 a Table showing what 1 li. with interest, and
 interest upon interest after 10 in the 100 comes
 to every year under 41 years. As followeth.

(over which is written years) and

| Years | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | 1 | 4 | 7 | 10 | 13 | 16 | 19 | 22 | 25 | 28 | 31 | 34 | 37 | 40 | 43 | 46 | 49 | 52 | 55 | 58 | 61 | 64 | 67 | 70 | 73 | 76 | 79 | 82 | 85 | 88 | 91 | 94 | 97 | 100 | 103 | 106 | 109 | 112 | 115 | 118 | 121 | 124 | 127 | 130 | 133 | 136 | 139 | 142 | 145 | 148 | 151 | 154 | 157 | 160 | 163 | 166 | 169 | 172 | 175 | 178 | 181 | 184 | 187 | 190 | 193 | 196 | 199 | 202 | 205 | 208 | 211 | 214 | 217 | 220 | 223 | 226 | 229 | 232 | 235 | 238 | 241 | 244 | 247 | 250 | 253 | 256 | 259 | 262 | 265 | 268 | 271 | 274 | 277 | 280 | 283 | 286 | 289 | 292 | 295 | 298 | 301 | 304 | 307 | 310 | 313 | 316 | 319 | 322 | 325 | 328 | 331 | 334 | 337 | 340 | 343 | 346 | 349 | 352 | 355 | 358 | 361 | 364 | 367 | 370 | 373 | 376 | 379 | 382 | 385 | 388 | 391 | 394 | 397 | 400 | 403 | 406 | 409 | 412 | 415 | 418 | 421 | 424 | 427 | 430 | 433 | 436 | 439 | 442 | 445 | 448 | 451 | 454 | 457 | 460 | 463 | 466 | 469 | 472 | 475 | 478 | 481 | 484 | 487 | 490 | 493 | 496 | 499 | 502 | 505 | 508 | 511 | 514 | 517 | 520 | 523 | 526 | 529 | 532 | 535 | 538 | 541 | 544 | 547 | 550 | 553 | 556 | 559 | 562 | 565 | 568 | 571 | 574 | 577 | 580 | 583 | 586 | 589 | 592 | 595 | 598 | 601 | 604 | 607 | 610 | 613 | 616 | 619 | 622 | 625 | 628 | 631 | 634 | 637 | 640 | 643 | 646 | 649 | 652 | 655 | 658 | 661 | 664 | 667 | 670 | 673 | 676 | 679 | 682 | 685 | 688 | 691 | 694 | 697 | 700 | 703 | 706 | 709 | 712 | 715 | 718 | 721 | 724 | 727 | 730 | 733 | 736 | 739 | 742 | 745 | 748 | 751 | 754 | 757 | 760 | 763 | 766 | 769 | 772 | 775 | 778 | 781 | 784 | 787 | 790 | 793 | 796 | 799 | 802 | 805 | 808 | 811 | 814 | 817 | 820 | 823 | 826 | 829 | 832 | 835 | 838 | 841 | 844 | 847 | 850 | 853 | 856 | 859 | 862 | 865 | 868 | 871 | 874 | 877 | 880 | 883 | 886 | 889 | 892 | 895 | 898 | 901 | 904 | 907 | 910 | 913 | 916 | 919 | 922 | 925 | 928 | 931 | 934 | 937 | 940 | 943 | 946 | 949 | 952 | 955 | 958 | 961 | 964 | 967 | 970 | 973 | 976 | 979 | 982 | 985 | 988 | 991 | 994 | 997 | 1000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | 1 | 6 | 7 | | | | | 8 | 19 | 1 | 23 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

in the time commencing at 1 li. Then must
 be added the sum of the years which
 By

By the former Table, if you desire to know what 1 li. commeth to with interest, and interest upon interest after 10 in the 100, for any number of years unto 40. Look in the row, or margin (over which is written years) and against it on the right hand close unto it in the row or margin of pounds, shillings, and pence, (which is titled thus, li. s. d.) you shall finde your desire.

Example.

I would know what 1 li. with interest, and interest upon interest commeth to in 7 years?

I look in the row of years for the number 7. and against it on the right hand I finde 1 li. 18 s. 11 d. Also what it commeth unto in 13 years. I seek among the years for 13, and against it I finde 3 li. 9 s.

Again, for 21 years. I look for 21 among the years, and I finde 7 li. 8 s. 0 d. But if you would know for a greater sum then 1 li. Then multiply your summe by that summe of 1 li. in the Table for any of those years, and you shall easily finde it. As thus, I would know what 10 li. commeth to for 7 years with interest, &c. I see that 1 li. commeth to 1 li. 18 s. 11 d. in that time. Then say I that 10 li. must be 10 times as much in that space, which is 19 li. 9 s. 2 d. Also of 10 li. in 13 years. I see that 1 li. in that time commeth unto 3 li. 9 d. Then must 10 li. be ten times as much in that space, which is

Interest upon Interest.

867

is 34 li. 10s. Also what 10 li. commeth to in 21 years. I finde first that 1 li. in that space commeth to 7 li. 8s. Then I say 10 must be 10 times as much, which is 74 li. Lastly, I would know what 100 li. commeth to in 7 years. I see it must be 100 times as much as 1 li. commeth to in that space, which is 104 li. 11s. 8d. Hereby you see the common saying is not true, that 100 li. doth double it self in 7 years, for it wants thereof 5 li. 8s. 4d. But in 8 years 100 li. commeth to 310 li. 8s. 4d. which you see is more then double it self by 10 li. 8s. 4d. And in this sort may any that can but cast with Counters, or indeed by memory, finde the increase of any summe whatsoever for any of the number of years in the foresaid Table, after they have found what 1 li. commeth unto for that time, as before is specified.

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|-----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

A Table shewing if 1 li. annuity to endure for any number of years, under 41 be all respited on forborn, untill the last payment grow due, and then all be received together, with interest, and interest upon interest after 10 in the 100 per annum.

when they will amount due by any of the
said number of years. As follows

| Years | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 1 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 2 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 3 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 4 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 5 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 6 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 7 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 8 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 9 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 10 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 11 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 12 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 13 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 14 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 15 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 16 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 17 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 18 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 19 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 20 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |

for any number of years, when it shall be repaid
by the last payment, with the last interest, and
the interest upon interest after 20 years.

By this Table you may know what any Annuity being respited or forboren for any number of years unto 41, with interest upon interest, shalbe in the 100, will come unto. First looking in the Table, what it shalbe come unto, in that time; and that being found, multiply it by the summe you desire to knowe, for

Example.

First, I would knowe what 1 li. Annuity being respited for 21 years, will come unto. I look in this last Table (which is for 100) and I find 164 li. 9 s. 10 d. for 21 years, and I find 64 li. Also the like for 1 li. for 30 years respited. I look, and find it to be 164 li. 9 s. 10 d. as by the said Table may appear. Now for greater Annuities, as 30 li. per annum, respited or forboren, what it amounteth to in 16 years, I seek first for 1 li. in this last Table before for 16 years; and against it I find 35 li. 18 s. 11 d. Then say I, that 30 li. per annum being respited for that time, will come to 30 times as much, which is 1078 li. 7 s. 6 d. Also if there be an annuity of 4 li. per annum, and unpaid for 10 years, I look in the said Table where 1 li. amounteth to 10 years, being respited, and I find it is 20 li. 7 s. 8 d. Then I conclude that

5 li.

Annuities in present

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annum abating interest, and interest upon interest. As followeth.

| years | li. | s. | d. | years | li. | s. | d. |
|-------|-----|----|----|-------|-----|----|----|
| 1 | 0 | 18 | 2 | 8 | 12 | 11 | 21 |
| 2 | 1 | 14 | 8 | 8 | 15 | 5 | 22 |
| 3 | 2 | 9 | 8 | 8 | 17 | 7 | 23 |
| 4 | 3 | 3 | 4 | 8 | 19 | 8 | 24 |
| 5 | 3 | 15 | 9 | 9 | 1 | 6 | 25 |
| 6 | 4 | 7 | 1 | 9 | 3 | 0 | 26 |
| 7 | 4 | 18 | 4 | 9 | 4 | 8 | 27 |
| 8 | 5 | 6 | 8 | 9 | 6 | 1 | 28 |
| 9 | 5 | 15 | 2 | 9 | 7 | 4 | 29 |
| 10 | 6 | 4 | 10 | 9 | 8 | 6 | 30 |
| 11 | 6 | 9 | 9 | 9 | 9 | 7 | 31 |
| 12 | 6 | 16 | 3 | 9 | 10 | 6 | 32 |
| 13 | 7 | 2 | 0 | 9 | 11 | 4 | 33 |
| 14 | 7 | 7 | 14 | 9 | 12 | 2 | 34 |
| 15 | 7 | 12 | 11 | 9 | 12 | 10 | 35 |
| 16 | 7 | 16 | 5 | 9 | 13 | 6 | 36 |
| 17 | 8 | 0 | 5 | 9 | 14 | 1 | 37 |
| 18 | 8 | 4 | 0 | 9 | 14 | 7 | 38 |
| 19 | 8 | 7 | 3 | 9 | 15 | 1 | 39 |
| 20 | 8 | 10 | 3 | 9 | 15 | 6 | 40 |

This

This Table before last specified is very necessary and commodious for all Gentlemen or others, that shall have cause to buy or sell Annuities or such like, for by this they shall know what they do, whether they demand, or take too little or too much, after the rate of ten in the 100, by which proportion all these Tables are ruled.

As for example, I am to buy an Annuity of 16 li. per annum, for 12 years, and am demanded for ready money 120 li. I would know, if I give this rate, whether I give too much or too little, according to the proportion of 10 in the 100 per annum, &c.

I look in the Table last before what 1 li. is worth for 12 years, and I find against it this summe 6 li. 16 s. 3 d. Now I say that 16 li. Annuity for that time, and after that proportion commeth to 16 times as much, which is 100 li. So that I see the party demanded of me 11 li. too much after the rate of 10 in the 100 per annum, and therefore I must draw him to a lower price, or leave it.

Again, I am offered an Annuity of 20 li. per annum for 14 years for 130 li. I would know if I give it, whether I give too much or too little; according to the proportion aforesaid.

I seek first what 1 li. Annuity is worth for 14 years, and I find in the said last Table 7 li. 7 s. 4 d. Then say that the Annuity of 20 li. per annum, will come to 20 times as much, and will be worth 147 li. 6 s. 8 d. according to the

the proportion before mentioned: and is more then he demand by 17 li. 6 s. 8 d. So that I see if I accept of it, I shall have a good bargain. And thus may you know readily by looking in your Table, and finding what 1 li. is worth for any time therein contained, how much any greater summe will come unto, if you multiply it by that summe of 1 li. as before is sufficiently shewed.

But suppose this I have 300 li. ready money, and would bestow the same for a valuable Annuity any wayable thereunto according to the proportion aforesaid. I would know what Annuity to endure 21 years this 300 li. will buy?

I look in the former Table what 1 li. Annuity will cost for that time, and I find 8 li. 12 s. 11 d. Then I say by the Rule of proportion. If 8 li. 12 s. 11 d. will buy 1 li. Annuity for 21 years: what Annuity shall 300 li. buy or be worth for that time? I reduce the summes to the least denomination (which is pence) and I find 34 li. 10 s. 9 d. And after this manner (by the help of this rule) may you find all other summes for any time contained in the foresaid last Table.

A Table shewing what 1 li. in reversion for any number of years under 31 is worth in ready money, the buyer staying untill the thing be fallen in hand.

| years | li. | s. | d. | years | li. | s. | d. |
|-------|-----|----|----|-------|-----|----|----|
| 1 | 0 | 15 | 2 | 16 | 0 | 4 | 4 |
| 2 | 0 | 16 | 6 | 17 | 0 | 3 | 11 |
| 3 | 0 | 15 | 0 | 18 | 0 | 3 | 7 |
| 4 | 0 | 13 | 7 | 19 | 0 | 3 | 3 |
| 5 | 0 | 12 | 3 | 20 | 0 | 2 | 11 |
| 6 | 0 | 11 | 3 | 21 | 0 | 2 | 8 |
| 7 | 0 | 10 | 3 | 22 | 0 | 2 | 5 |
| 8 | 0 | 9 | 3 | 23 | 0 | 2 | 2 |
| 9 | 0 | 8 | 3 | 24 | 0 | 1 | 0 |
| 10 | 0 | 7 | 8 | 25 | 0 | 1 | 10 |
| 11 | 0 | 7 | 0 | 26 | 0 | 1 | 8 |
| 12 | 0 | 6 | 4 | 27 | 0 | 1 | 6 |
| 13 | 0 | 5 | 9 | 28 | 0 | 1 | 4 |
| 14 | 0 | 5 | 3 | 29 | 0 | 1 | 3 |
| 15 | 0 | 4 | 9 | 30 | 0 | 1 | 1 |

This

This last Table differeth, and is contrary to the other three before mentioned. For whereas the others increased more and more according to the number of years specified, this doth grow and diminish less and less, as the number of years increased. As for example,

I have a Tenement the fee simple whereof after 7 years will be worth 40 li. what is it now worth for it is ready money, now staying untill it fall in hand?

To know this I look in this last Table for 7 years, and against it I find 10 s. 3 d. So that a thing that after 7 years will be worth 1 li. is worth now in ready money but 10 s. 3 d. Then say I, that the foresaid Tenement (which after 7 years will be worth 40 li) is now worth 40 times 10 s. 3 d. which is 20 li. 10 s.

Again, there is a Farm which after 9 years will be worth the Fee-simple 420 li. what is it now worth in ready money, staying untill it fall in hand?

I look in the said Table what 1 li. is worth in Reversion after 9 years; and I find 8 s. 5 d. Then say I, that the Farm of 420 li. so long in Reversion; will be now worth in ready money, 420 times as much, which is 176 li. 15 s.

Lastly, there is a Lordship to be sold, the Fee-simple whereof after 14 years will be worth 7500

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li. I would know what the same is now worth in ready money for the Reversion.

I look in this last Table for 14 years, and against it I find 5 s. 3 d. so much 1 li. is worth in reversion after 14 years. Then say I, that 7500 li. is worth no more in reversion for that time then 7500 times 5 s. 3 d. which is 3968 li. 15 s. And after this manner may you finde out any other summe whatsoever. And though some men of their own experience can aime (as they think) near enough the mark to serve their own turns: yet I dare undertake they shall never so exactly doe it, nor justify what they doe, as if they did it by Art.

FINIS.

I look in the said Table what 1 li. is worth in Reversion after 9 years, and find 8 s. 7 d. Then say I, that the sum of 420 li. so long in reversion, will be now worth in ready money,

420 times as much, which is 1764 li. 15 s.

New Tables of Interest at 8 per centum per annum, exactly calculated for 30 years by Robert Hartwell, with necessary questions for the use of them.

The first Table expressing the increase of one pound principal put out and forborne for any number of years under 31 at 8 per centum per annum.

| year. | l. | s. | d. | q. | year. | l. | s. | d. | q. |
|-------|----|----|----|----|-------|----|----|----|----|
| 1 | 1 | 0 | 0 | 0 | 16 | 3 | 8 | 6 | 0 |
| 2 | 1 | 0 | 8 | 3 | 17 | 3 | 14 | 0 | 0 |
| 3 | 1 | 1 | 3 | 3 | 18 | 3 | 19 | 6 | 0 |
| 4 | 1 | 1 | 7 | 2 | 19 | 4 | 6 | 3 | 3 |
| 5 | 1 | 1 | 9 | 4 | 20 | 4 | 13 | 2 | 2 |
| 6 | 1 | 1 | 11 | 8 | 21 | 5 | 0 | 8 | 0 |
| 7 | 1 | 1 | 14 | 3 | 22 | 5 | 8 | 8 | 3 |
| 8 | 1 | 1 | 17 | 0 | 23 | 5 | 17 | 0 | 0 |
| 9 | 1 | 1 | 19 | 11 | 24 | 6 | 6 | 2 | 3 |
| 10 | 1 | 2 | 3 | 0 | 25 | 6 | 16 | 1 | 2 |
| 11 | 1 | 2 | 6 | 7 | 26 | 7 | 7 | 11 | 0 |
| 12 | 1 | 2 | 10 | 4 | 27 | 7 | 19 | 9 | 0 |
| 13 | 1 | 2 | 14 | 4 | 28 | 8 | 12 | 6 | 3 |
| 14 | 1 | 2 | 18 | 8 | 29 | 9 | 6 | 4 | 0 |
| 15 | 1 | 3 | 3 | 5 | 30 | 10 | 1 | 3 | 0 |

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The description and use of the Tables of Interest at 8 per annum, being profitable.

The first of them.

These Tables consist of four Columns, in the first and fourth whereof is written over the head, years, and under the first number of years descending from 1 to 15, likewise in the fourth the number of years descending from 16 to 30. And against every year in the second Column, toward the right hand the pounds, shillings, pence, and farthings; which one pound, or 20 s. principall will amount unto being put forth and forborn for the number of years set against it; but the pounds, shillings, pence, &c. in the third Column, belongeth to the years set in the last Column,

Example.

Let it be required what one pound or 20 shillings, being put forth and forborn for 12 years, ariseth to at 8 per centum, per annum, interest upon interest.

Seek in the first Column under the title of years, for 12 the number of years proposed in the question, and right against it toward the right hand in the second Column, you shall find 2 li.—10 s.—4d.—1q. which is the principall and increase thereof due for the time required,

2 Example.

If 100 li. be put forth for 17 years according

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to the same interest, I demand what it will amount to in that time?

Look in the Colimne under the title of years for 17, and right against it towards the left hand in the Table is found 3 li—14s—0d.—0q, which is the increase of 1 li. by which you may thus gather

| | | | |
|-------------------------|-----|---|---|
| li | s | d | q |
| the increase of 100 li. | 300 | 0 | 0 |
| or any other summe; | 70 | 0 | 0 |
| a hundred times 3 li. | | | |
| is 300 li. then 100 | 370 | 0 | 0 |

times 14 shillings is 70 li. both which added together do make 370 li.—0s—0d. which is the increase of 100 li. put forth and forborne 17 years the solution to the question.

3 Example.

Suppose 60 li. be put forth for 19 years according to that rate, what will it increase to in that time?

Seek 19 under the title of years, and against it toward the left hand is found 4 li—6s—3d—3q. now say 60 times 4 li. is 240 li—s—d—q and 60 times 6 shillings is 360 shillings, or 18 li. and 60 times 3 d. is 180 d. or 15 shillings, and 60 times 3 farthings is 3 shillings

| | | | | |
|--|-----|----|---|---|
| 9 d. all which added together make 258 li. 18 s. 9 d. the increase thereof demanded. | 258 | 18 | 9 | 0 |
|--|-----|----|---|---|

The second Table showing what one pound annuity or yearly rent is worth at the end of any number of years under 31, being forborne at 8 per centum, per annum.

| years | li. | s. | d. | q. | li. | s. | d. | q. | years |
|-------|-----|----|----|----|-----|----|----|----|-------|
| 1 | 1 | 0 | 0 | 0 | 30 | 6 | 5 | 3 | 16 |
| 2 | 2 | 1 | 7 | 0 | 33 | 15 | 0 | 0 | 17 |
| 3 | 3 | 4 | 1 | 0 | 37 | 9 | 0 | 0 | 18 |
| 4 | 4 | 10 | 1 | 1 | 41 | 8 | 11 | 0 | 19 |
| 5 | 5 | 17 | 3 | 3 | 45 | 15 | 2 | 3 | 20 |
| 6 | 7 | 6 | 8 | 0 | 50 | 8 | 5 | 12 | 21 |
| 7 | 8 | 18 | 5 | 1 | 55 | 9 | 1 | 2 | 22 |
| 8 | 10 | 12 | 8 | 3 | 60 | 17 | 10 | 1 | 23 |
| 9 | 12 | 9 | 9 | 0 | 66 | 15 | 3 | 3 | 24 |
| 10 | 14 | 9 | 8 | 3 | 73 | 2 | 1 | 1 | 25 |
| 11 | 16 | 12 | 10 | 3 | 79 | 19 | 1 | 9 | 26 |
| 12 | 18 | 19 | 0 | 2 | 87 | 7 | 0 | 0 | 27 |
| 13 | 21 | 9 | 10 | 3 | 95 | 6 | 1 | 8 | 28 |
| 14 | 24 | 4 | 3 | 2 | 103 | 19 | 3 | 3 | 29 |
| 15 | 27 | 3 | 0 | 2 | 111 | 5 | 7 | 3 | 30 |

The use of the second Table, (whose disposition is altogether like the former), according to the title thereof, being practicable.

Example 1

There is a Lease worth 28 li. per annum, to endure 14 years, I demand what it will rise unto at the end of those years, being all forborne with the interest upon interest at the rate prescribed in this Table.

Look in the third Table for 14 years, against which toward the right hand, you shall finde 24 li. — 4 s. — 3 d. — 2 q. Now multiply 28 li. by 24, there ariseth 672 li. then 28 li. by 4 s. yeeldeth

112 s. or 5 li. 12 s. li. — s. — d. — q. Again 28 li. by 3 d. 672 — 0 — 0 — 0

produceth 84 d. or 5 — 12 — 0 — 0

7 s. finally, 28 by 2 farthings yeeldeth 7 — 0 — 0 — 0

56 farthings or 1 s. 1 — 3 — 0 — 0

2 d. All which added together make

678 — 0 — 2 — 0

678 li. 0 s. 2 d. to be received at the end of

14 years, the same rent or annuity being respited.

Example 2

If 60 li. yearly rent or annuity be forborne 20 years: I demand how much it will increase at the end of the said term

314 — 4 — 0 — 0

In

In the Table I find that 1 pound in 20 years will rise to 45 li. 15 s. 2 d. 3 q. therefore 60 li. in the like term will yeeld 60 times so much; which I will

reckon thus: 60 times $\begin{array}{r} \text{li} \quad \text{s} \quad \text{d} \quad \text{q} \\ 45 \text{ li. is } 2700 \text{ li. } 60 \quad 2700 \text{—} 0 \text{—} 0 \text{—} 0 \\ \text{times } 15 \text{ s. is } 900 \text{ s. } 45 \text{—} 0 \text{—} 0 \text{—} 0 \\ \text{or } 45 \text{ l. } 60 \text{ times } 2 \text{ d. } 100 \text{—} 0 \text{—} 0 \text{—} 0 \\ \text{is } 100 \text{ d. or } 10 \text{ s. last } 3 \text{—} 9 \text{—} 0 \\ \text{of all } 60 \text{ times } 3 \text{ q. is } 180 \text{ farthings, or } 30 \quad 2745 \text{—} 13 \text{—} 9 \text{—} 0 \\ \text{—} 2 \text{ d. all which together amount unto } 2745 \text{ li. } 13 \text{ s. } 9 \text{ d. the value thereof to be received at the end of the term.} \end{array}$

Example.

The yearly rent of 1 li. 13 s. 4 d. being behind and unpaid the space of 7 years at the end of which term the Tenant is compelled to pay the same with the Interest thereof according to the above named rate. I demand what then payment ought to be.

The increase of 1 li. yearly being answering to 7 years, is 8 li. 18 s. 5 d. 1 q. which for 8 li. rent is to be taken 8 times, which ariseth to 32 li. 10 s. 7 d. 1 q. now because 13 s. 4 d. is two third parts of 1 li. therefore I take $\frac{2}{3}$ of 8 li. 18 s. 5 d. 1 q. which is the increase of 1 li. for 7 years, that is 11 li. 11 d. 2 q. which together make 43 li. 2 s. 6 d. 3 q. the summe to be received, as was required.

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The third Table declaring what one pound due at the end of any number of years under 31 is worth ready money at 8 per centum, per annum.

| years | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
|-------|---|----|----|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 1 | 0 | 18 | 7 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2 | 0 | 17 | 10 | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 3 | 0 | 15 | 1 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4 | 0 | 14 | 8 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 5 | 0 | 13 | 7 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 6 | 0 | 12 | 7 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 7 | 0 | 11 | 8 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 8 | 0 | 10 | 9 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 9 | 0 | 10 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 10 | 0 | 9 | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 11 | 0 | 8 | 6 | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 12 | 0 | 7 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 13 | 0 | 7 | 4 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 14 | 0 | 6 | 9 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 15 | 0 | 6 | 3 | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

The Table to be paid before it fall in hand.
 11. 12. 4. d. the value of
 added together is 291
 13. 13. 4. d. which
 maketh 400 d. which
 10. 13. 4. d.
 11. 12. 4. d.
 12. 13. 4. d.
 13. 14. 4. d.
 14. 15. 4. d.
 15. 16. 4. d.
 16. 17. 4. d.
 17. 18. 4. d.
 18. 19. 4. d.
 19. 20. 4. d.
 20. 21. 4. d.
 21. 22. 4. d.
 22. 23. 4. d.
 23. 24. 4. d.
 24. 25. 4. d.
 25. 26. 4. d.
 26. 27. 4. d.
 27. 28. 4. d.
 28. 29. 4. d.
 29. 30. 4. d.

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This third Table is disposed as the first, the use according to the Title thereof, being damageable.

1 Example.

Suppose there is 750 li. due to be payed at the end of 9 years, the Creditor would sell this debt for present money, what ought that money to be at the rate described in the Table?

Seek in this third Table for 9 years at the left side of the Table, and right against it toward the right hand, you shall finde 18 shillings; which multiplied or taken 750 times, yeeldeth 7500 shillings, which is 375 li. the value of that debt in present money.

2 Example.

There is a Lease worth 500 li. after the end of 7 years; what is it worth present money, according to the rate described in the Table staying till it fall?

I seek in the Table for the 7 years, and right against it I finde 11 s—8 d; now I multiply 500 by 11, it yeeldeth 5500 shillings, or 275 li—s—d—q
 li. then 500 times 8 d. 275—0—0—0
 maketh 4000 d, which 16—13—4—0
 is 16 li. 13 s. 4 d, which added together is 291 291—13—4—0
 li. 13 s. 4 d. the value of the Lease to be paid before it fall in hand.

The

The fourth Table expressing what one pound yearly rent or annuity for any number of years not exceeding 30 is worth ready money at 4 per centum, per annum.

| years | ll. | s. | d. | q. | years | ll. | s. | d. | q. |
|-------|-----|----|----|----|-------|-----|----|----|----|
| 1 | 0 | 18 | 6 | 0 | 8 | 17 | 0 | 1 | 16 |
| 2 | 1 | 15 | 7 | 2 | 9 | 15 | 1 | 0 | 17 |
| 3 | 2 | 11 | 6 | 3 | 10 | 13 | 1 | 1 | 18 |
| 4 | 3 | 6 | 2 | 3 | 11 | 11 | 1 | 2 | 19 |
| 5 | 3 | 19 | 10 | 1 | 12 | 10 | 4 | 1 | 20 |
| 6 | 4 | 12 | 5 | 1 | 13 | 9 | 4 | 0 | 21 |
| 7 | 4 | 4 | 1 | 2 | 14 | 8 | 0 | 0 | 22 |
| 8 | 5 | 14 | 13 | 0 | 15 | 7 | 5 | 0 | 23 |
| 9 | 6 | 4 | 11 | 1 | 16 | 6 | 4 | 3 | 24 |
| 10 | 6 | 14 | 1 | 1 | 17 | 5 | 3 | 3 | 25 |
| 11 | 7 | 2 | 9 | 1 | 18 | 4 | 2 | 1 | 26 |
| 12 | 7 | 10 | 8 | 1 | 19 | 3 | 1 | 1 | 27 |
| 13 | 7 | 18 | 0 | 3 | 20 | 2 | 0 | 0 | 28 |
| 14 | 8 | 4 | 10 | 2 | 21 | 1 | 10 | 2 | 29 |
| 15 | 8 | 11 | 2 | 1 | 22 | 1 | 0 | 3 | 30 |

is 120 and 140 times 7. 2.
is 90 and 100 times 7. 2.
is 60 and 70 times 7. 2.
is 30 and 40 times 7. 2.
is 10 and 20 times 7. 2.
is 5 and 10 times 7. 2.
is 2 and 5 times 7. 2.
is 1 and 2 times 7. 2.
is 0 and 1 times 7. 2.
is 0 and 0 times 7. 2.

The fourth Table is disposed altogether as the former, and the use thereof is like fore. being demisable from

1 Example.

There is an annuity or rent of 20 s. per annum to endure 25 years, it is required what it is worth ready money?

Look in the Table for 25 years, and right against it you shall find 10 li. 13 s. 5 d. 3 q. which is the solution.

2 Example.

What is the Lease of certain Land valued at 140 li. per annum, to begin presently and endure 18 years, worth ready money?

Search in the Table for 18 years, the term named in the question, and right against it toward the left hand you shall find 9 li. 7 s. 5 d. 1 q. which expresseth that one pound rent to be bought for that term is worth so much; therefore that summe 140 times is the value required. Now 140 times 9 li.

| | | | | |
|--------------------------------|--------------------|------|------|-----|
| is 1260, | and 140 times 7 s. | li | s | d |
| is 980 s. or 49 li; | likewise | 1260 | — 0 | — 0 |
| 140 times 5 d. is 700 d. or | | 49 | — 0 | — 0 |
| 2 li. 18 s. 4 d. and 140 far- | | 2 | — 18 | — 4 |
| things is 2 s. 11 d. all which | | 2 | — 11 | |
| added together make 1312 | | — | — | — |
| li. 1 s. 3 d. for the value of | | 1312 | — 1 | — 3 |
| the said Lease paying no rent. | | | | |

3 Ex-

Example. In T. 16. of T.
 a lease taken for 21 years at 12 li. 6 s. 8 d.
 per annum, which after 5 years expired the Ten-
 ant is desirous to give a fine, and bring the rent
 down to 8 li. per annum, for the rest of the term,
 the demand is what fine is to be payed?

Subtract 5 years from 21, the remain 16, is
 the time unexpired: likewise from the present
 rent abate 8 li, the rest will be 5 li. 6 s. 8 d. now
 the drift of the question is, what 5 li. 6 s. 8 d.
 yearly rent or annuity to endure 16 years is
 worth present money.

The value of 1 li. rent or annuity answering
 to 16 years is, 8 li. 17 s. 0 d. 1 q. Now 9 times
 8 li. is 40 li. and 9 times 17 s. 4 d. is 5 s. and 5
 times one farthing, is 1 d. 1 q. and because
 6 s. 8 d. is $\frac{5}{8}$ of 1 li. I take $\frac{5}{8}$ of 8 li. 17 s. 0 d.
 1 q. which is 2 li. 19 s. 0 d. all which added
 together, make 4 li. 4 s. 1 d. 1 q. which is the
 fine that ought to be paid to bring the rent to
 8 li. per annum.

| | | | |
|-----|----|----|----|
| li. | s. | d. | q. |
| 40 | 0 | 0 | 0 |
| 4 | 5 | 0 | 0 |
| 2 | 19 | 1 | 1 |
| 47 | 4 | 1 | 1 |

23 Purchase of Annuities.

The fifth Table declaring what yearly rent or annuity of one pound ready money will purchase for any number of years under 31, at 8 per centum per annum.

| years | li. | s. | d. | q. | years | li. | s. | d. | q. |
|-------|-----|----|----|----|-------|-----|----|----|----|
| 1 | 0 | | 17 | 0 | 16 | 0 | 2 | 9 | 3 |
| 2 | 0 | | 14 | 0 | 17 | 0 | 2 | 8 | 3 |
| 3 | 0 | | 9 | 0 | 18 | 0 | 2 | 8 | 0 |
| 4 | 0 | | 7 | 6 | 19 | 0 | 2 | 7 | 0 |
| 5 | 0 | | 6 | 3 | 20 | 0 | 2 | 6 | 1 |
| 6 | 0 | | 5 | 4 | 21 | 0 | 2 | 5 | 3 |
| 7 | 0 | | 4 | 9 | 22 | 0 | 2 | 5 | 1 |
| 8 | 0 | | 4 | 0 | 23 | 0 | 2 | 4 | 3 |
| 9 | 0 | | 4 | 0 | 24 | 0 | 2 | 4 | 1 |
| 10 | 0 | | 3 | 8 | 25 | 0 | 2 | 4 | 0 |
| 11 | 0 | | 3 | 6 | 26 | 0 | 2 | 3 | 0 |
| 12 | 0 | | 3 | 3 | 27 | 0 | 2 | 3 | 1 |
| 13 | 0 | | 3 | 1 | 28 | 0 | 2 | 3 | 0 |
| 14 | 0 | | 3 | 0 | 29 | 0 | 2 | 2 | 8 |
| 15 | 0 | | 2 | 11 | 30 | 0 | 2 | 2 | 12 |

As the value of the annuity is the same as the value of the purchase money, so the value of the purchase money is the same as the value of the annuity.

In the fifth Table the Numbers and Columns

are all disposed as the former Tables, and needeth
no further explanation but only Examples.

1 Example.

The Table declareth at first sight what yearly
rent or annuity one pound ready money will pur-
chase for any years in the Table expressed.

But if the ready money be above one pound,
then if any value or rent set down in this Ta-
ble, be multiplied by the number belonging to
the years in question, the product will shew
what yearly rent or annuity that ready money will
purchase for the time proposed.

2 Example.

A certain man hath 750 li. to purchase an An-
nuity to endure 27 years, so as it may yeeld him
the like profit, as if it were put out according to
the rate in the Table expressed, it is required
what that annuity ought to be?

Because the annuity is to endure 27 years,
seek out the value or rent set against 27 years,
in this fifth Table, which is 2 s — 3 d — 1 q. now
this

This being the *Annuity* of 20 s. ready money
 which may be for the
 year, it must be multiplied
 by 750 li. as for 750 li. for
 month, because 2 s. is 9—7—6
 the tenth part of 20 s. 15—7—2
 therefore take the tenth
 part of 750 li. which is 85—3—1
 75 li. which set first
 down, then 74 li. 10 s. 10 d. which
 for under the former, but at 10 s. 10 d.
 is 15 s. 7 d. ob. which added together, pro-
 duce 85 li. 3 s. 1 d. ob. the yearly *Annuity*
 required no more be above
 at this in now set out or value of
 or gaining by the number belonging to
 the year in which the annuity is to be paid
 what yearly rent or annuity this purchase

*Deo soli Deo, omnia honor
 & gloria tribuatur.*

Ammon.

This is the *Annuity* of 20 s. ready money
 which may be for the
 year, it must be multiplied
 by 750 li. as for 750 li. for
 month, because 2 s. is 9—7—6
 the tenth part of 20 s. 15—7—2
 therefore take the tenth
 part of 750 li. which is 85—3—1
 75 li. which set first
 down, then 74 li. 10 s. 10 d. which
 for under the former, but at 10 s. 10 d.
 is 15 s. 7 d. ob. which added together, pro-
 duce 85 li. 3 s. 1 d. ob. the yearly *Annuity*
 required no more be above
 at this in now set out or value of
 or gaining by the number belonging to
 the year in which the annuity is to be paid
 what yearly rent or annuity this purchase

Because the annuity is to endure 27 years,
 seek out the value of rent for against 27 years
 in this file Table, which is 2—3—4—1 d. now
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